















Value Function
<ul> <li>Idea</li> <li>Value function is a prediction of future reward</li> <li>Used to evaluate the goodness/badness of states</li> <li>And thus to select between actions</li> </ul>
<ul> <li>Definition         <ul> <li>The value of a state s under a policy π, denoted v<sub>π</sub>(s), is the expected return when starting in s and following π thereafter.</li> <li>v<sub>π</sub>(s) = E<sub>π</sub>[G<sub>t</sub> S<sub>t</sub> = s] = E<sub>π</sub>[∑<sup>k=0</sup><sub>k=0</sub> γ<sup>k</sup>R<sub>t+k+1</sub>  S<sub>t</sub> = s]</li> </ul> </li> </ul>
- The value of taking action <i>a</i> in state <i>s</i> under a policy $\pi$ , denoted $q_{\pi}(s, a)$ , is the expected return starting from <i>s</i> , taking action <i>a</i> , and following $\pi$ thereafter.
$q_{\pi}(s, a) = \mathbb{E}_{\pi}[G_t S_t = s, A_t = a] = \mathbb{E}_{\pi}[\sum_{k=0}^{\infty} \gamma^k R_{t+k+1}   S_t = s, A_t = a]$



















# Model-based vs Model-free

### Model-based

- Has a model of the environment dynamics and reward
- Allows agent to plan: predict state and reward before taking action
- Pro: Better sample efficiency
- Con: Agent only as good as the environment Model-bias

## Model-free

- No explicit model of the environment dynamics and reward
- Less structured. More popular and further developed and tested.
- Pro: Can be easier to implement and tune
- Cons: Very sample inefficient













# **Policy Evaluation** · If we do not know the model, then we have to approximate it using observations One option: Monte-Carlo methods - Play through a sequence of actions until a reward is reached, then backpropagate it to the states on the path. - Update after whole sequence (episodic) $V(S_t) \leftarrow V(S_t) + \alpha[G_t - V(S_t)]$ Target: the actual return after time t • Or: Temporal Difference Learning (TD Learning) – $TD(\lambda)$ - Directly perform an update using the estimate $V(S_{t+\lambda+1})$ . - Bootstraps the current estimate of the value function - Can update every step $V(S_t) \leftarrow V(S_t) + \alpha[R_{t+1} + \gamma V(S_{t+1}) - V(S_t)]$ Target: an estimate of the return (here: TD(0)) ٦ **RWTH**AACHEN Prof. Dr. Bastian Leibe







# References and Further Reading • More information on Reinforcement Learning can be found in the following book Richard S. Sutton, Andrew G. Barto Reinforcement Learning: An Introduction MT Press, 1998 • The complete text is also freely available online https://webdocs.cs.ualberta.ca/~sutton/book/ebook/the-book.html



