

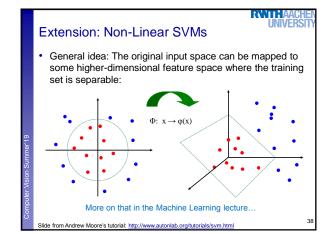
# Finding the Maximum Margin Line

- Solution:
- Classification function:

$$\begin{split} f(\mathbf{x}) &= \operatorname{sign}(\mathbf{w}^T\mathbf{x} + b) & \text{if } f(\mathbf{x}) < 0, \ \text{classify as neg.}, \\ &= \operatorname{sign}\left(\sum_{n=1}^N a_n t_n \mathbf{x}_n^T \mathbf{x} + b\right) & \text{if } f(\mathbf{x}) < 0, \ \text{classify as pos.} \end{split}$$

- > Notice that this relies on an inner product between the test point  ${\bf x}$ and the support vectors  $\mathbf{x}_n$
- (Solving the optimization problem also involves computing the inner products  $\mathbf{x}_n^T \mathbf{x}_m$  between all pairs of training points)

C. Burges, A Tutorial on Support Vector Machines for Pattern Recognition, Data Mining and Knowledge Discovery, 1998



## Nonlinear SVMs

The kernel trick: instead of explicitly computing the lifting transformation  $\varphi(\mathbf{x})$ , define a kernel function K such that

$$K(\mathbf{x}_i, \mathbf{x}_j) = \varphi(\mathbf{x}_i) \cdot \varphi(\mathbf{x}_j)$$

This gives a nonlinear decision boundary in the original feature space:

$$\sum_{n} a_n t_n K(\mathbf{x}_n, \mathbf{x}) + b$$

Since the optimization formulation uses the data points only in the form of inner products  $\varphi(\mathbf{x}_n)^T \varphi(\mathbf{x}_m)$ , we never need to actually compute the lifting transformation  $\varphi(\mathbf{x})$ .

C. Burges, A Tutorial on Support Vector Machines for Pattern Recognition,

# Some Often-Used Kernel Functions

· Linear:

$$K(\mathbf{x}_i, \mathbf{x}_i) = \mathbf{x}_i^T \mathbf{x}_i$$

· Polynomial of power p:

$$K(x_i, x_i) = (1 + x_i^T x_i)^p$$

· Gaussian (Radial-Basis Function):

$$K(\mathbf{x_i}, \mathbf{x_j}) = \exp(-\frac{\|\mathbf{x_i} - \mathbf{x_j}\|^2}{2\sigma^2})$$

Slide from Andrew Moore's tutorial: http://www.autonlab.org/tutorials/sym.htm

# Summary: SVMs for Recognition

- 1. Define your representation for each example.
- 2. Select a kernel function.
- 3. Compute pairwise kernel values between labeled examples
- 4. Pass this "kernel matrix" to SVM optimization software to identify support vectors & weights.
- 5. To classify a new example: compute kernel values between new input and support vectors, apply weights, check sign of output.

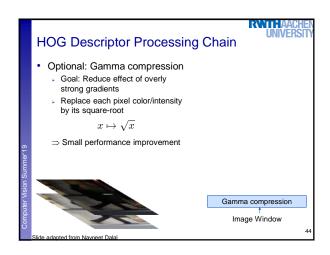


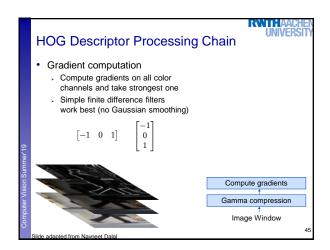
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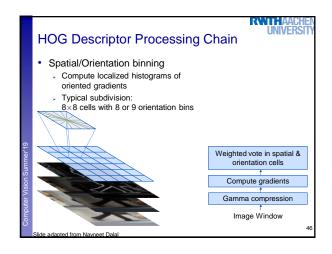
# Topics of This Lecture

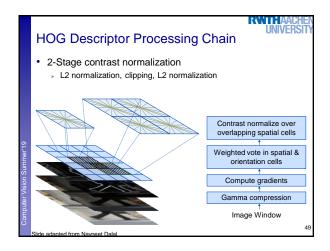
- Object Categorization
  - Problem Definition
- Sliding-Window based Object Detection
  - Detection via Classification
  - Global Representations
  - Classifier Construction
- Classification with SVMs
  - Support Vector Machines
  - **HOG Detector**
- Classification with Boosting
  - AdaBoost
  - Viola-Jones Face Detection

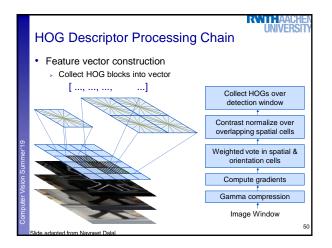


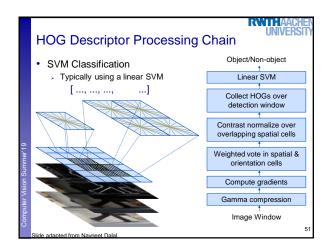


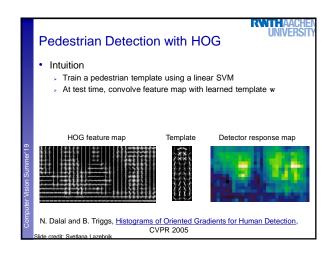


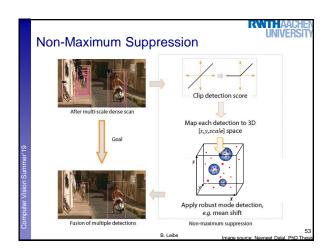


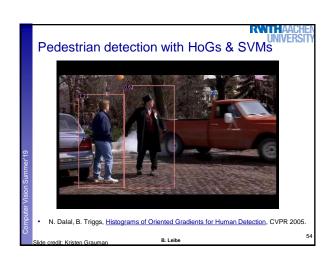


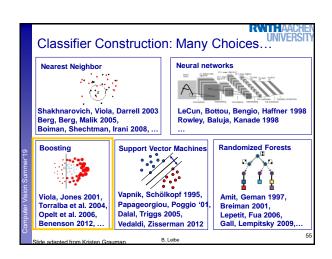


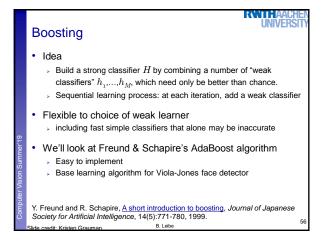


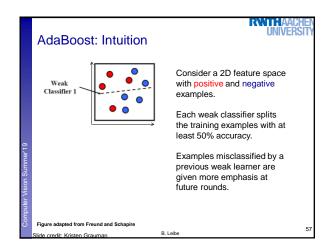


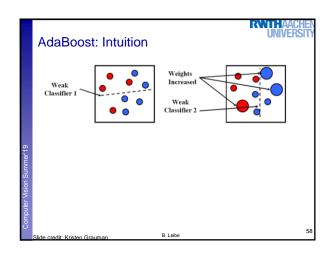


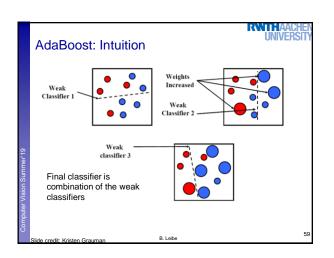


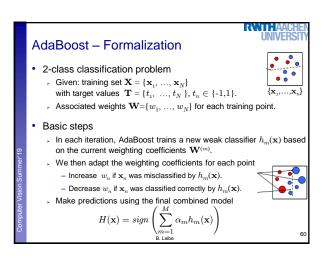


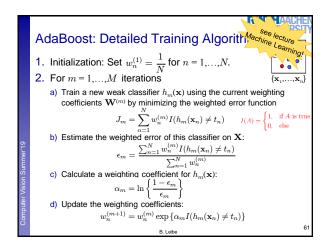


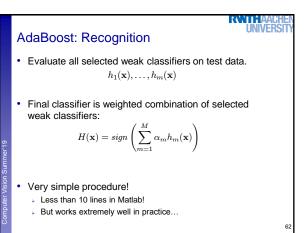


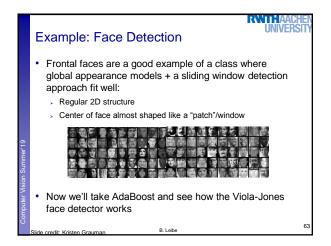


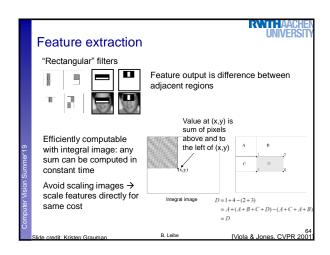


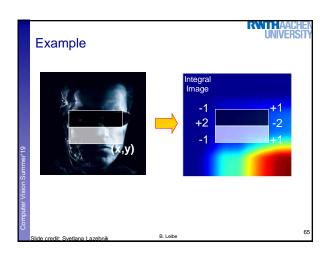


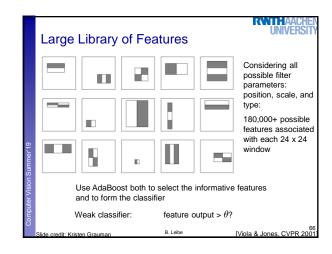


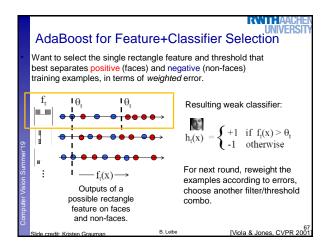


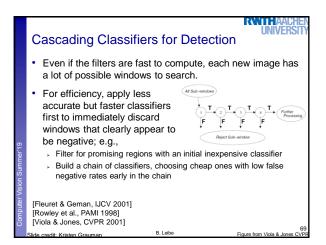


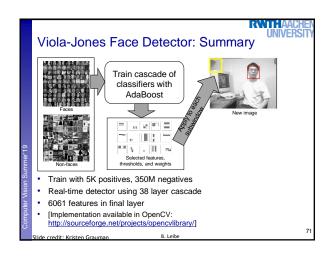


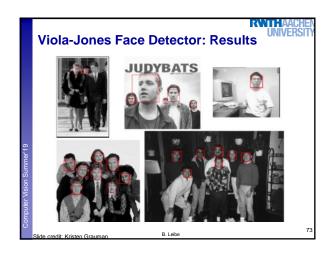


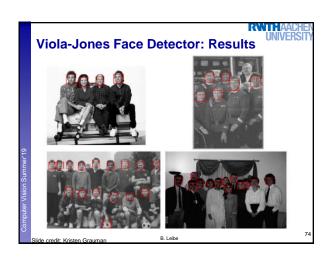


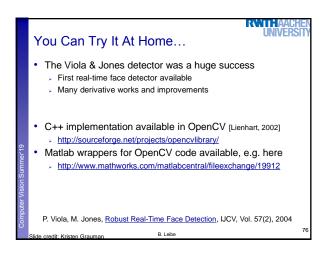


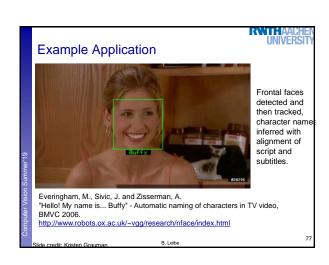


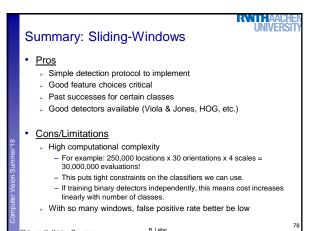


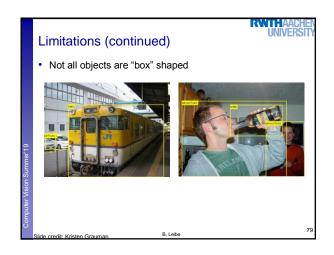


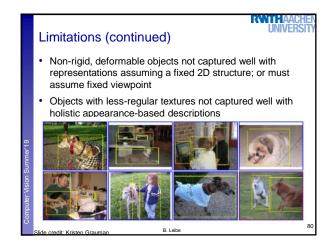


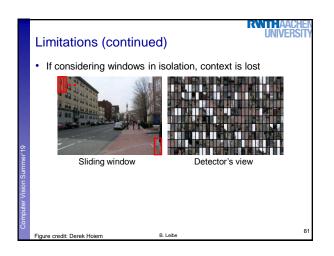


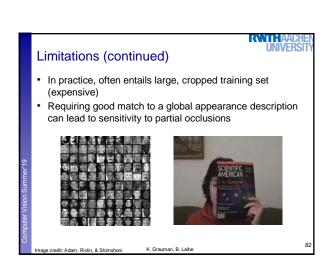












# References and Further Reading • Read the HOG paper • N. Dalal, B. Triggs, Histograms of Oriented Gradients for Human Detection, CVPR, 2005. • HOG Detector • Code available: http://pascal.inrialpes.fr/soft/olt/