

Computer Vision - Lecture 17

Epipolar Geometry & Stereo Basics

13.01.2015

Bastian Leibe
RWTH Aachen
<http://www.vision.rwth-aachen.de>
leibe@vision.rwth-aachen.de

Announcements

- Seminar in the summer semester
 - “Current Topics in Computer Vision and Machine Learning”
 - Block seminar, presentations in 1st week of semester break
 - Registration period: 14.01.2015 - 28.01.2015
 - <http://web-info8.informatik.rwth-aachen.de/apse>
- Quick poll: Who would be interested in that?

Course Outline

- Image Processing Basics
- Segmentation & Grouping
- Object Recognition
- Local Features & Matching
- Object Categorization
- 3D Reconstruction
 - Epipolar Geometry and Stereo Basics
 - Camera calibration & Uncalibrated Reconstruction
 - Multi-view Stereo
- Optical Flow

Topics of This Lecture

- Geometric vision
 - Visual cues
 - Stereo vision
- Epipolar geometry
 - Depth with stereo
 - Geometry for a simple stereo system
 - Case example with parallel optical axes
 - General case with calibrated cameras
- Stereopsis & 3D Reconstruction
 - Correspondence search
 - Additional correspondence constraints
 - Possible sources of error
 - Applications

Geometric vision

- Goal: Recovery of 3D structure
 - What cues in the image allow us to do this?



Visual Cues

- Shading




Merle Norman Cosmetics, Los Angeles

Computer Vision WS 14/15

RWTH AACHEN UNIVERSITY

Visual Cues

- Shading
- Texture



The Visual Cliff, by William Vandivert, 1960

Slide credit: Steve Seitz

B. Leibe


8

Computer Vision WS 14/15

RWTH AACHEN UNIVERSITY

Visual Cues

- Shading
- Texture
- Focus



From *The Art of Photography*, Canon

Slide credit: Steve Seitz

B. Leibe


9

Computer Vision WS 14/15

RWTH AACHEN UNIVERSITY

Visual Cues

- Shading
- Texture
- Focus
- Perspective



Slide credit: Steve Seitz

B. Leibe


10

Computer Vision WS 14/15


RWTH AACHEN UNIVERSITY

Visual Cues

- Shading
- Texture
- Focus
- Perspective
- Motion



Figures from L. Zhang



Slide credit: Steve Seitz, Kristen Grauman

<http://www.brainconnection.com/teasers/2main-illusion/motion-shape>

B. Leibe

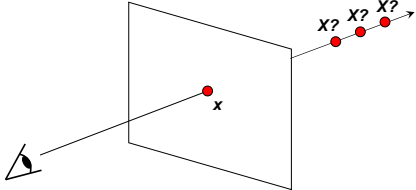
11

Computer Vision WS 14/15

RWTH AACHEN UNIVERSITY

Our Goal: Recovery of 3D Structure

- We will focus on perspective and motion
- We need *multi-view geometry* because recovery of structure from one image is inherently ambiguous



Slide credit: Svetlana Lazebnik

B. Leibe

12

Computer Vision WS 14/15

RWTH AACHEN UNIVERSITY

To Illustrate This Point...

- Structure and depth are inherently ambiguous from single views.



Slide credit: Svetlana Lazebnik, Kristen Grauman

B. Leibe

13

RWTH AACHEN UNIVERSITY

Stereo Vision







http://www.well.com/~jim/stereo/stereo_list.html

Computer Vision WS 14/15 Slide credit: Kristen Grauman

RWTH AACHEN UNIVERSITY

What Is Stereo Vision?

- Generic problem formulation: given several images of the same object or scene, compute a representation of its 3D shape

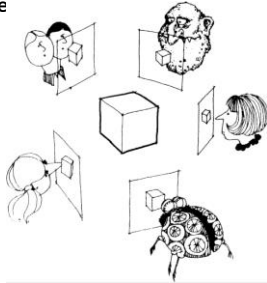




Computer Vision WS 14/15 Slide credit: Svetlana Lazebnik, Steve Seitz, B. Leibe

RWTH AACHEN UNIVERSITY

What Is Stereo Vision?

- Generic problem formulation: given several images of the same object or scene, compute a representation of its 3D shape



Computer Vision WS 14/15 Slide credit: Svetlana Lazebnik, Steve Seitz, B. Leibe

RWTH AACHEN UNIVERSITY

What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image

Image 1






Image 2



Dense depth map



Computer Vision WS 14/15 Slide credit: Svetlana Lazebnik, Steve Seitz

RWTH AACHEN UNIVERSITY

What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
 - Humans can do it





Stereograms: Invented by Sir Charles Wheatstone, 1838

Computer Vision WS 14/15 Slide credit: Svetlana Lazebnik, Steve Seitz, B. Leibe

RWTH AACHEN UNIVERSITY

What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
 - Humans can do it



Autostereograms: <http://www.magiceye.com>

Computer Vision WS 14/15 Slide credit: Svetlana Lazebnik, Steve Seitz

RWTH AACHEN UNIVERSITY

What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
 - Humans can do it



Autostereograms: <http://www.magiceye.com>



20

Computer Vision WS 14/15

Slide credit: Svetlana Lazebnik, Steve Seitz

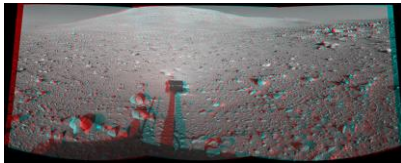
RWTH AACHEN UNIVERSITY

Application of Stereo: Robotic Exploration

Nomad robot searches for meteorites in Antarctica

Real-time stereo on Mars



21

Computer Vision WS 14/15

Slide credit: Steve Seitz

RWTH AACHEN UNIVERSITY

Topics of This Lecture

- Geometric vision
 - Visual cues
 - Stereo vision
- Epipolar geometry
 - Depth with stereo
 - Geometry for a simple stereo system
 - Case example with parallel optical axes
 - General case with calibrated cameras
- Stereopsis & 3D Reconstruction
 - Correspondence search
 - Additional correspondence constraints
 - Possible sources of error
 - Applications

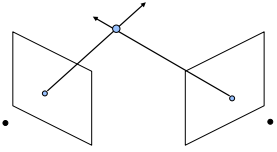
22

Computer Vision WS 14/15

B. Leibe

RWTH AACHEN UNIVERSITY

Depth with Stereo: Basic Idea



- Basic Principle: Triangulation
 - Gives reconstruction as intersection of two rays
 - Requires
 - Camera pose (calibration)
 - Point correspondence

23

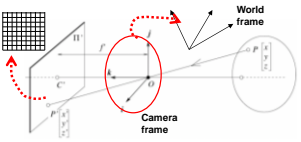
Computer Vision WS 14/15

Slide credit: Steve Seitz

B. Leibe

RWTH AACHEN UNIVERSITY

Camera Calibration



Extrinsic parameters: Camera frame ↔ Reference frame

Intrinsic parameters: Image coordinates relative to camera ↔ Pixel coordinates

- Parameters
 - Extrinsic: rotation matrix and translation vector
 - Intrinsic: focal length, pixel sizes (mm), image center point, radial distortion parameters

We'll assume for now that these parameters are given and fixed.

24

Computer Vision WS 14/15

Slide credit: Kristen Grauman

B. Leibe

RWTH AACHEN UNIVERSITY

Geometry for a Simple Stereo System

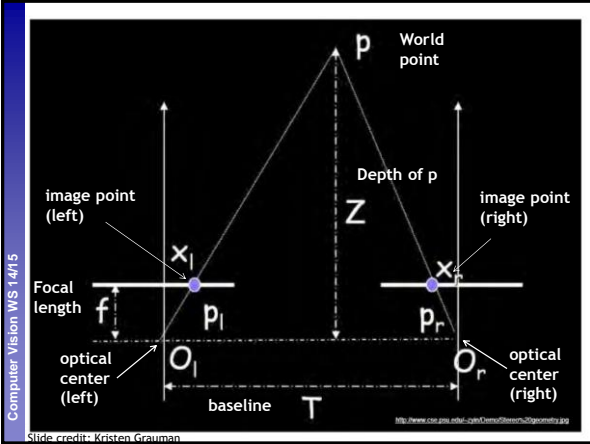
- First, assuming parallel optical axes, known camera parameters (i.e., calibrated cameras):

25

Computer Vision WS 14/15

Slide credit: Kristen Grauman

B. Leibe



Geometry for a Simple Stereo System

- Assume parallel optical axes, known camera parameters (i.e., calibrated cameras). We can triangulate via:

Similar triangles (p, P, p_r) and (O_l, P, O_r) :

$$\frac{T - (x_r - x_l)}{Z - f} = \frac{T}{Z}$$

$$Z = f \frac{T}{x_r - x_l}$$

"disparity" $x_r - x_l$

Computer Vision WS 14/15

Slide credit: Kristen Grauman

B. Leibe

27

Depth From Disparity

Image $I(x, y)$ Disparity map $D(x, y)$ Image $I'(x', y')$

$$(x', y') = (x + D(x, y), y)$$

Computer Vision WS 14/15

B. Leibe

28

General Case With Calibrated Cameras

- The two cameras need not have parallel optical axes.

Computer Vision WS 14/15

Slide credit: Kristen Grauman, Steve Seitz

B. Leibe

29

Stereo Correspondence Constraints

- Given p in the left image, where can the corresponding point p' in the right image be?

Computer Vision WS 14/15

Slide credit: Kristen Grauman

B. Leibe

30

Stereo Correspondence Constraints

- Given p in the left image, where can the corresponding point p' in the right image be?

Computer Vision WS 14/15

Slide credit: Kristen Grauman

B. Leibe

31

RWTH AACHEN UNIVERSITY

Stereo Correspondence Constraints

Computer Vision WS 14/15

Slide credit: Kristen Grauman B. Leibe

32

RWTH AACHEN UNIVERSITY

Stereo Correspondence Constraints

- Geometry of two views allows us to constrain where the corresponding pixel for some image point in the first view must occur in the second view.

- Epipolar constraint: Why is this useful?
 - Reduces correspondence problem to 1D search along conjugate epipolar lines.

Computer Vision WS 14/15

Slide adapted from Steve Seitz B. Leibe

33

RWTH AACHEN UNIVERSITY

Epipolar Geometry

- Epipolar Plane
- Baseline
- Epipoles
- Epipolar Lines

Computer Vision WS 14/15

Slide adapted from Marr-Pollefeys

34

RWTH AACHEN UNIVERSITY

Epipolar Geometry: Terms

- **Baseline**
 - Line joining the camera centers
- **Epipole**
 - Point of intersection of baseline with the image plane
- **Epipolar plane**
 - Plane containing baseline and world point
- **Epipolar line**
 - Intersection of epipolar plane with the image plane
- **Properties**
 - All epipolar lines intersect at the epipole.
 - An epipolar plane intersects the left and right image planes in epipolar lines.

Computer Vision WS 14/15

Slide credit: Marr-Pollefeys B. Leibe

35

RWTH AACHEN UNIVERSITY

Epipolar Constraint

- Potential matches for p have to lie on the corresponding epipolar line l' .
- Potential matches for p' have to lie on the corresponding epipolar line l .

Computer Vision WS 14/15

Slide credit: Marr-Pollefeys B. Leibe

<http://www.ai.sri.com/~luong/research/Meta3DViewer/EpipolarGeo.html>

36

RWTH AACHEN UNIVERSITY

Example

Computer Vision WS 14/15

Slide credit: Kristen Grauman B. Leibe

37

RWTH AACHEN UNIVERSITY

Example: Converging Cameras

As position of 3D point varies, epipolar lines "rotate" about the baseline

Computer Vision WS 14/15

38

Slide credit: Kristen Grauman B. Leibe Figure from Hartley & Zisserman

RWTH AACHEN UNIVERSITY

Example: Motion Parallel With Image Plane

Computer Vision WS 14/15

39

Slide credit: Kristen Grauman B. Leibe Figure from Hartley & Zisserman

RWTH AACHEN UNIVERSITY

Example: Forward Motion

- Epipole has same coordinates in both images.
- Points move along lines radiating from e: "Focus of expansion"

Computer Vision WS 14/15

40

Slide credit: Kristen Grauman B. Leibe Figure from Hartley & Zisserman

RWTH AACHEN UNIVERSITY

Let's Formalize This!

- For a given stereo rig, how do we express the epipolar constraints algebraically?
- For this, we will need some linear algebra.
- But don't worry! We'll go through it step by step...

Computer Vision WS 14/15

41

B. Leibe

RWTH AACHEN UNIVERSITY

Stereo Geometry With Calibrated Cameras

- If the rig is calibrated, we know:
 - How to rotate and translate camera reference frame 1 to get to camera reference frame 2.
 - Rotation: 3 x 3 matrix; translation: 3 vector.

Computer Vision WS 14/15

42

Slide credit: Kristen Grauman, Steve Seitz B. Leibe

RWTH AACHEN UNIVERSITY

Rotation Matrix

$$\mathbf{R}_x(\alpha) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{bmatrix}$$

Express 3D rotation as series of rotations around coordinate axes by angles α, β, γ

$$\mathbf{R}_y(\beta) = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix}$$

Overall rotation is product of these elementary rotations:

$$\mathbf{R} = \mathbf{R}_x \mathbf{R}_y \mathbf{R}_z$$

$$\mathbf{R}_z(\gamma) = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Computer Vision WS 14/15

43

Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

3D Rigid Transformation

$$\begin{bmatrix} X' \\ Y' \\ Z' \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} + \begin{bmatrix} T_x \\ T_y \\ T_z \end{bmatrix}$$

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

44

Computer Vision WS 14/15
Slide credit: Kristen Grauman
B. Leibe

RWTH AACHEN UNIVERSITY

Stereo Geometry With Calibrated Cameras

• Camera-centered coordinate systems are related by known rotation \mathbf{R} and translation \mathbf{T} :

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

45

Computer Vision WS 14/15
Slide credit: Kristen Grauman
B. Leibe

RWTH AACHEN UNIVERSITY

Excursion: Cross Product

$$\vec{a} \times \vec{b} = \vec{c} \quad \begin{array}{l} \vec{a} \cdot \vec{c} = 0 \\ \vec{b} \cdot \vec{c} = 0 \end{array}$$

- Vector cross product takes two vectors and returns a third vector that's perpendicular to both inputs.
- So here, c is perpendicular to both a and b , which means the dot product is 0.

46

Computer Vision WS 14/15
Slide credit: Kristen Grauman
B. Leibe

RWTH AACHEN UNIVERSITY

From Geometry to Algebra

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

$$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{X}') = \mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X})$$

$$\mathbf{T} \times \mathbf{X}' = \mathbf{T} \times \mathbf{R}\mathbf{X} + \mathbf{T} \times \mathbf{T}$$

$$0 = \mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X})$$

Normal to the plane
 $= \mathbf{T} \times \mathbf{R}\mathbf{X}$

47

Computer Vision WS 14/15
Slide credit: Kristen Grauman

RWTH AACHEN UNIVERSITY

Matrix Form of Cross Product

$$\vec{a} \times \vec{b} = \vec{c} \quad \begin{array}{l} \vec{a} \cdot \vec{c} = 0 \\ \vec{b} \cdot \vec{c} = 0 \end{array}$$

"skew symmetric" matrix

$$[a_{\times}] = \begin{bmatrix} 0 & -a_z & a_y \\ a_z & 0 & -a_x \\ -a_y & a_x & 0 \end{bmatrix} \quad \boxed{\vec{a} \times \vec{b} = [a_{\times}] \vec{b}}$$

48

Computer Vision WS 14/15
Slide credit: Kristen Grauman

RWTH AACHEN UNIVERSITY

From Geometry to Algebra

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

$$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{X}') = \mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X})$$

$$\mathbf{T} \times \mathbf{X}' = \mathbf{T} \times \mathbf{R}\mathbf{X} + \mathbf{T} \times \mathbf{T}$$

$$0 = \mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X})$$

Normal to the plane
 $= \mathbf{T} \times \mathbf{R}\mathbf{X}$

49

Computer Vision WS 14/15
Slide credit: Kristen Grauman

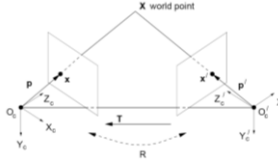
RWTH AACHEN UNIVERSITY

Essential Matrix

$$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X}) = 0$$

$$\mathbf{X}' \cdot (\mathbf{T}_x \mathbf{R}\mathbf{X}) = 0$$

Let $\mathbf{E} = \mathbf{T}_x \mathbf{R}$

$$\mathbf{X}'^T \mathbf{E} \mathbf{X} = 0$$


- This holds for the rays p and p' that are parallel to the camera-centered position vectors X and X' , so we have: $\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$
- \mathbf{E} is called the **essential matrix**, which relates corresponding image points [Longuet-Higgins 1981]

Computer Vision WS 14/15 50
Slide credit: Kristen Grauman B. Leibe

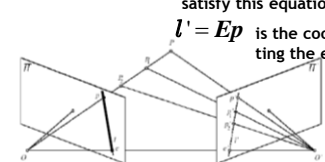
RWTH AACHEN UNIVERSITY

Essential Matrix and Epipolar Lines

$$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$$

Epipolar constraint: if we observe point p in one image, then its position p' in second image must satisfy this equation.

$\mathbf{l}' = \mathbf{E} \mathbf{p}$ is the coordinate vector representing the epipolar line for point p
(i.e., the line is given by: $\mathbf{l}'^T \mathbf{x} = 0$)



$\mathbf{l} = \mathbf{E}^T \mathbf{p}'$ is the coordinate vector representing the epipolar line for point p'

Computer Vision WS 14/15 51
Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

Essential Matrix: Properties

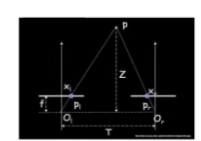
- Relates image of corresponding points in both cameras, given rotation and translation.
- Assuming intrinsic parameters are known

$$\mathbf{E} = \mathbf{T}_x \mathbf{R}$$

Computer Vision WS 14/15 52
Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

Essential Matrix Example: Parallel Cameras



$$\mathbf{R} = \mathbf{I}$$

$$\mathbf{T} = [-d, 0, 0]^T$$

$$\mathbf{E} = [\mathbf{T}_x] \mathbf{R}$$

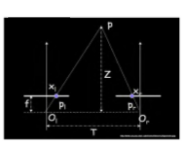
$$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$$

For the parallel cameras, image of any point must lie on same horizontal line in each image plane.

Computer Vision WS 14/15 53
Slide credit: Kristen Grauman

RWTH AACHEN UNIVERSITY

Essential Matrix Example: Parallel Cameras



$$\mathbf{R} = \mathbf{I}$$

$$\mathbf{T} = [-d, 0, 0]^T$$

$$\mathbf{E} = [\mathbf{T}_x] \mathbf{R} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & d \\ 0 & -d & 0 \end{bmatrix}$$

$$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$$

$$\begin{bmatrix} x' & y' & f \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & d \\ 0 & -d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ f \end{bmatrix} = 0$$

$$\Leftrightarrow \begin{bmatrix} x' & y' & f \end{bmatrix} \begin{bmatrix} 0 \\ df \\ -dy \end{bmatrix} = 0$$


$$\Leftrightarrow y = y'$$

For the parallel cameras, image of any point must lie on same horizontal line in each image plane.

Computer Vision WS 14/15 54
Slide credit: Kristen Grauman

RWTH AACHEN UNIVERSITY

More General Case

Image $I(x,y)$




Disparity map $D(x,y)$


Image $I'(x',y')$


$$(x', y') = (x + D(x, y), y)$$

What about when cameras' optical axes are not parallel?

Computer Vision WS 14/15 55
Slide credit: Kristen Grauman B. Leibe

Computer Vision WS 14/15

Stereo Image Rectification

- In practice, it is convenient if image scanlines are the epipolar lines.

- Algorithm**
 - Reproject image planes onto a common plane parallel to the line between optical centers
 - Pixel motion is horizontal after this transformation
 - Two homographies (3×3 transforms), one for each input image reprojected

56
Slide adapted from Li Zhang, C. Loop & Z. Zhang, *Computing Rectifying Homographies for Stereo Vision*, CVPR'09

Computer Vision WS 14/15

Stereo Image Rectification: Example

57
Source: Alvosha Efros

Computer Vision WS 14/15

Topics of This Lecture

- Geometric vision**
 - Visual cues
 - Stereo vision
- Epipolar geometry**
 - Depth with stereo
 - Geometry for a simple stereo system
 - Case example with parallel optical axes
 - General case with calibrated cameras
- Stereopsis & 3D Reconstruction**
 - Correspondence search
 - Additional correspondence constraints
 - Possible sources of error
 - Applications

58
B. Leibe

Computer Vision WS 14/15

Stereo Reconstruction

- Main Steps**
 - Calibrate cameras
 - Rectify images
 - Compute disparity
 - Estimate depth

59
Slide credit: Kristen Grauman, B. Leibe

Computer Vision WS 14/15

Correspondence Problem

Multiple match hypotheses satisfy epipolar constraint, but which is correct?

- Hypothesis 1
- Hypothesis 2
- Hypothesis 3

60
Slide credit: Kristen Grauman, B. Leibe, Figure from Gao & Cindola 1999

Computer Vision WS 14/15

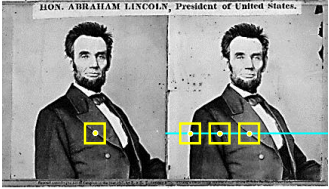
Correspondence Problem

- To find matches in the image pair, we will assume
 - Most scene points visible from both views
 - Image regions for the matches are similar in appearance

61
Slide credit: Kristen Grauman, B. Leibe

RWTH AACHEN UNIVERSITY

Dense Correspondence Search



HON. ABRAHAM LINCOLN, President of United States.

- For each pixel in the first image
 - Find corresponding epipolar line in the right image
 - Examine all pixels on the epipolar line and pick the best match (e.g. SSD, correlation)
 - Triangulate the matches to get depth information
- This is easiest when epipolar lines are scanlines
 - ⇒ Rectify images first

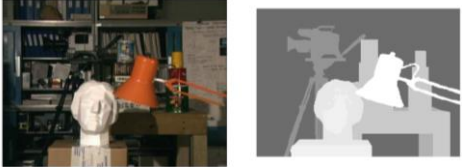
Computer Vision WS 14/15 62

adapted from Svetlana Lazebnik, Li Zhang

RWTH AACHEN UNIVERSITY

Example: Window Search

- Data from University of Tsukuba



Scene Ground truth

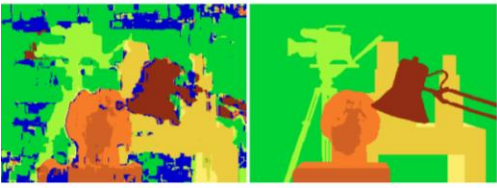
Computer Vision WS 14/15 63

Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

Example: Window Search

- Data from University of Tsukuba



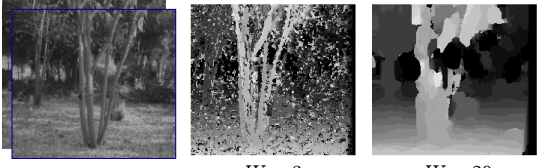
Window-based matching (best window size) Ground truth

Computer Vision WS 14/15 64

Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

Effect of Window Size



$W = 3$ $W = 20$

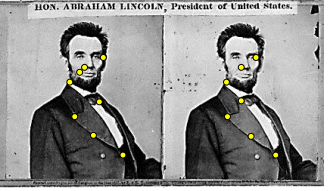
Want window large enough to have sufficient intensity variation, yet small enough to contain only pixels with about the same disparity.

Computer Vision WS 14/15 65

Slide credit: Kristen Grauman B. Leibe Figures from Li Zhang

RWTH AACHEN UNIVERSITY

Alternative: Sparse Correspondence Search



HON. ABRAHAM LINCOLN, President of United States.

- Idea: Restrict search to sparse set of detected features
- Rather than pixel values (or lists of pixel values) use *feature descriptor* and an associated *feature distance*
- Still narrow search further by epipolar geometry

What would make good features?

Computer Vision WS 14/15 66

Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

Dense vs. Sparse

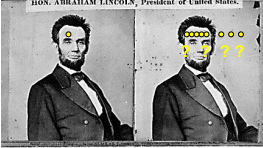
- Sparse
 - Efficiency
 - Can have more reliable feature matches, less sensitive to illumination than raw pixels
 - But...
 - Have to know enough to pick good features
 - Sparse information
- Dense
 - Simple process
 - More depth estimates, can be useful for surface reconstruction
 - But...
 - Breaks down in textureless regions anyway
 - Raw pixel distances can be brittle
 - Not good with very different viewpoints

Computer Vision WS 14/15 67


Slide credit: Kristen Grauman

RWTH AACHEN UNIVERSITY

Difficulties in Similarity Constraint



Untextured surfaces



Occlusions

Computer Vision WS 14/15 68

Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

Possible Sources of Error?

- Low-contrast / textureless image regions
- Occlusions
- Camera calibration errors
- Violations of *brightness constancy* (e.g., specular reflections)
- Large motions

Computer Vision WS 14/15 69

Slide credit: Kristen Grauman B. Leibe

RWTH AACHEN UNIVERSITY

Application: View Interpolation




Right Image

Computer Vision WS 14/15 68

Slide credit: Svetlana Lazebnik

RWTH AACHEN UNIVERSITY

Application: View Interpolation




Left Image

Computer Vision WS 14/15 69

Slide credit: Svetlana Lazebnik

RWTH AACHEN UNIVERSITY

Application: View Interpolation



Disparity

Computer Vision WS 14/15 68

Slide credit: Svetlana Lazebnik

RWTH AACHEN UNIVERSITY

Application: View Interpolation



Computer Vision WS 14/15 69

Slide credit: Svetlana Lazebnik

RWTH AACHEN
UNIVERSITY

Application: Free-Viewpoint Video



<http://www.liberovision.com>

74


Computer Vision WS 14/15

B. Leibe


RWTH AACHEN
UNIVERSITY

Summary: Stereo Reconstruction


- Main Steps
 - Calibrate cameras
 - Rectify images
 - Compute disparity
 - Estimate depth
- So far, we have only considered calibrated cameras...
- Next lecture
 - Uncalibrated cameras
 - Camera parameters
 - Revisiting epipolar geometry
 - Robust fitting




Left



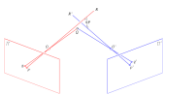
Right



Left



Right



75

Computer Vision WS 14/15


Slide credit: Kristen Grauman
B. Leibe

RWTH AACHEN
UNIVERSITY

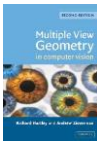
References and Further Reading

- Background information on epipolar geometry and stereopsis can be found in Chapters 10.1-10.2 and 11.1-11.3 of

D. Forsyth, J. Ponce,
Computer Vision - A Modern Approach.
Prentice Hall, 2003


- More detailed information (if you really want to implement 3D reconstruction algorithms) can be found in Chapters 9 and 10 of

R. Hartley, A. Zisserman
Multiple View Geometry in Computer Vision
2nd Ed., Cambridge Univ. Press, 2004



76

Computer Vision WS 14/15

B. Leibe