

Computer Vision - Lecture 6

Segmentation

09.11.2016

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Course Outline

- Image Processing Basics
 - Structure Extraction
- Segmentation
 - Segmentation as Clustering
 - Graph-theoretic Segmentation
- Recognition
 - Global Representations
 - Subspace representations
- Local Features & Matching
- Object Categorization
- 3D Reconstruction



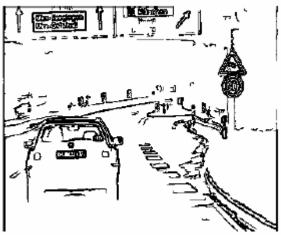
Recap: Chamfer Matching

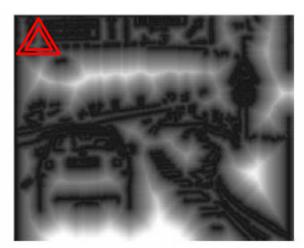
- Chamfer Distance
 - Average distance to nearest feature

$$D_{chamfer}(T, I) \equiv \frac{1}{|T|} \sum_{t \in T} d_I(t)$$

This can be computed efficiently by correlating the edge template with the distance-transformed image







Edge image

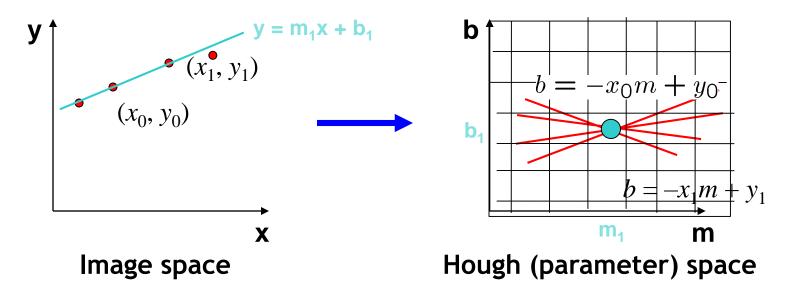
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Distance transform image 3

[D. Gavrila, DAGM'99]



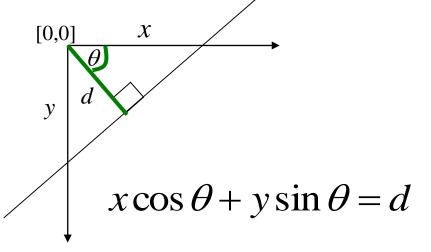
Recap: Hough Transform



- How can we use this to find the most likely parameters (m,b) for the most prominent line in the image space?
 - Let each edge point in image space vote for a set of possible parameters in Hough space
 - Accumulate votes in discrete set of bins; parameters with the most votes indicate line in image space.

Recap: Hough Transf. Polar Parametrization

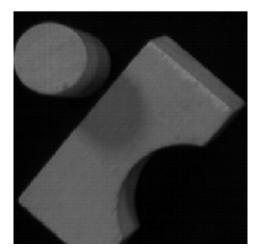
• Usual (m,b) parameter space problematic: can take on infinite values, undefined for vertical lines.



Point in image space
 ⇒ sinusoid segment in
 Hough space

d: perpendicular distance from line to origin

 θ : angle the perpendicular makes with the x-axis





Slide credit: Steve Seitz



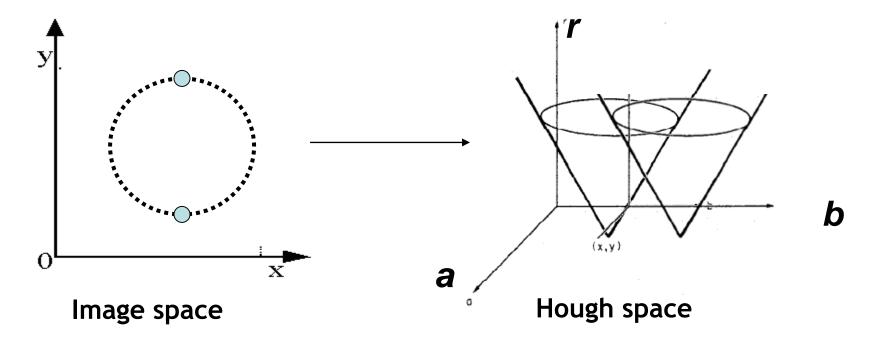


Recap: Hough Transform for Circles

• Circle: center (a,b) and radius r

$$(x_i - a)^2 + (y_i - b)^2 = r^2$$

• For an unknown radius r, unknown gradient direction

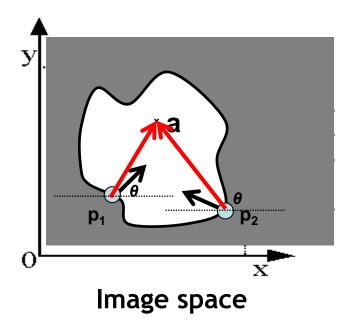


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Generalized Hough Transform

 What if we want to detect arbitrary shapes defined by boundary points and a reference point?



At each boundary point, compute displacement

vector: $r = a - p_i$.

For a given model shape: store these vectors in a table indexed by gradient orientation θ .

[Dana H. Ballard, Generalizing the Hough Transform to Detect Arbitrary Shapes, 1980]



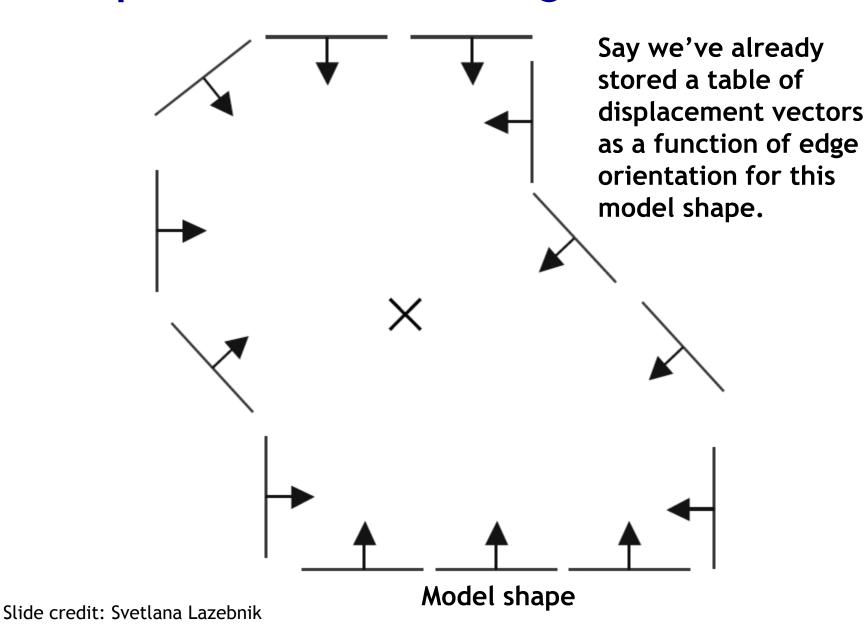
Generalized Hough Transform

To detect the model shape in a new image:

- For each edge point
 - \succ Index into table with its gradient orientation heta
 - > Use retrieved r vectors to vote for position of reference point
- Peak in this Hough space is reference point with most supporting edges

Assuming translation is the only transformation here, i.e., orientation and scale are fixed.

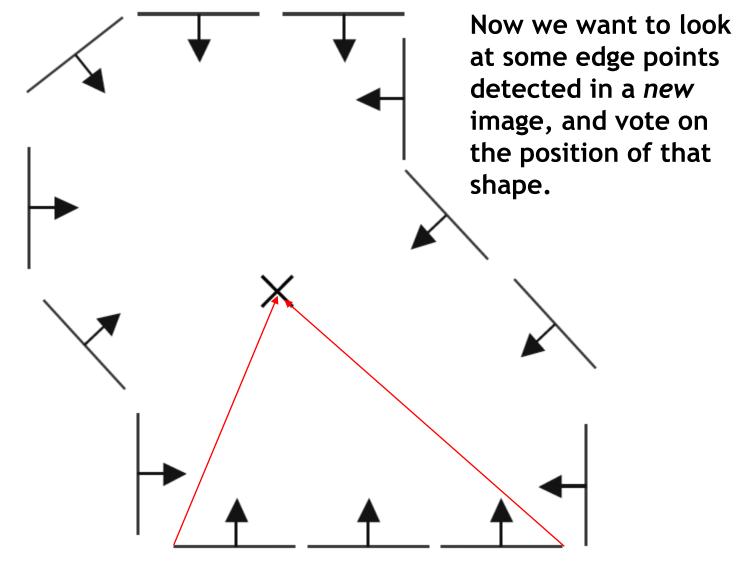




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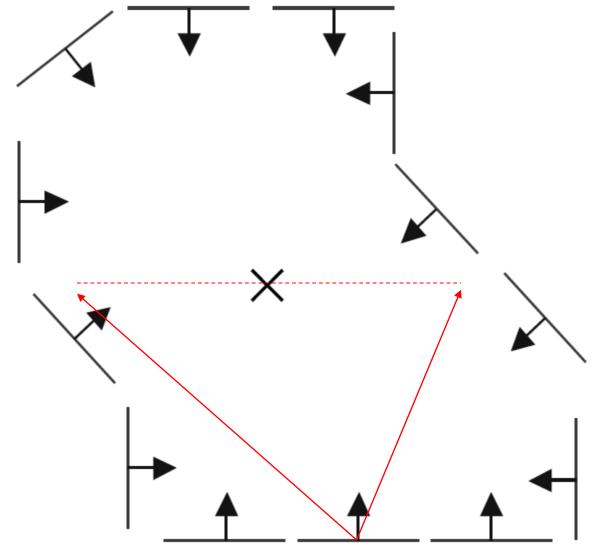
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Example: Generalized Hough Transform

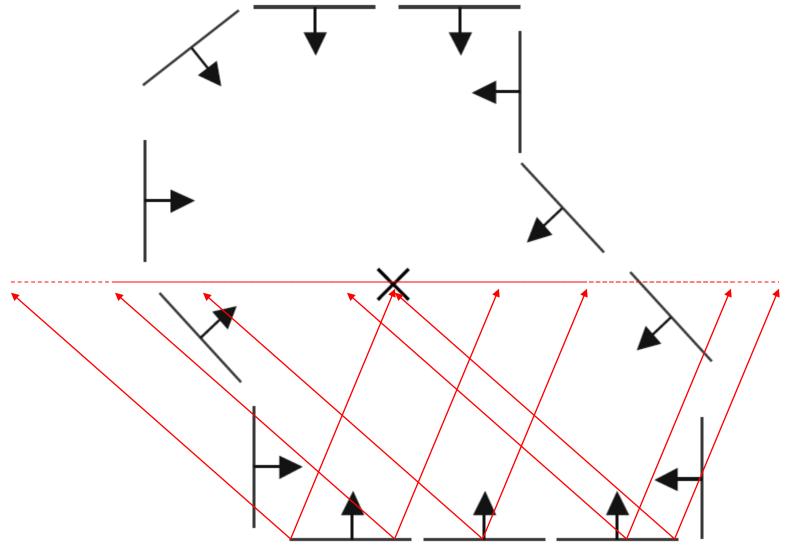


Displacement vectors for model points
Slide credit: Svetlana Lazebnik



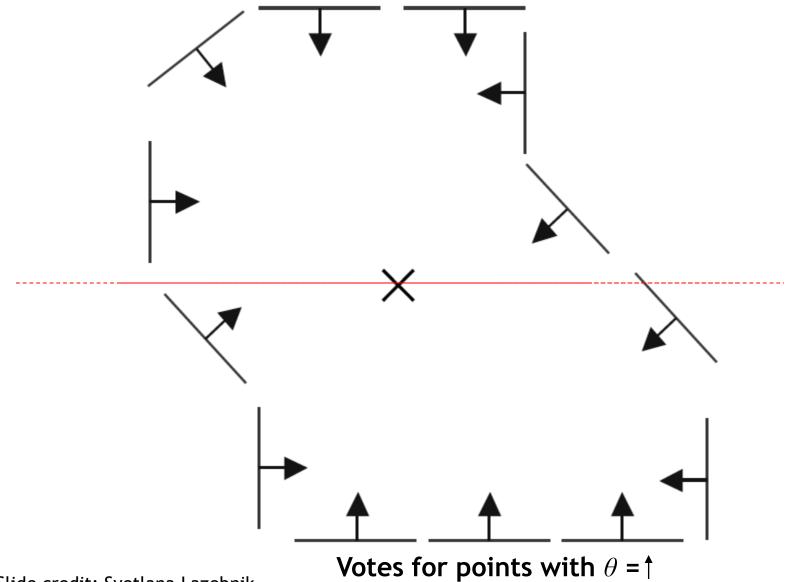


Range of voting locations for test point Slide credit: Svetlana Lazebnik



Range of voting locations for test point Slide credit: Svetlana Lazebnik

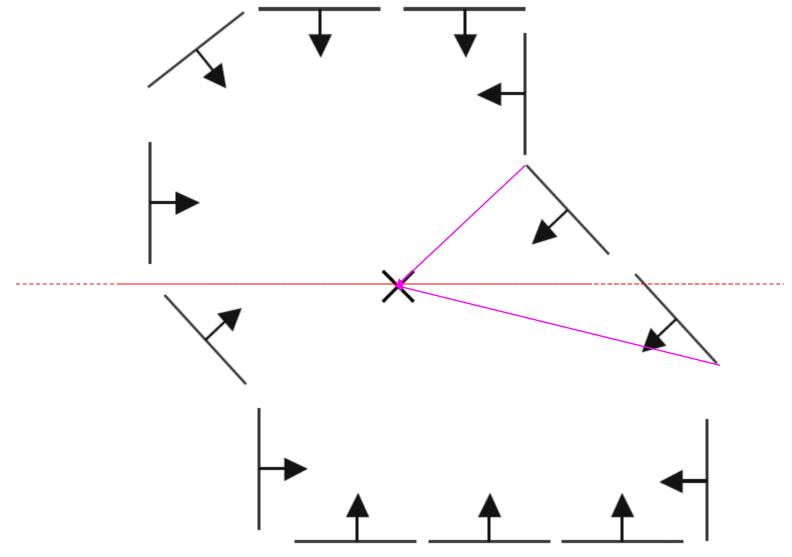




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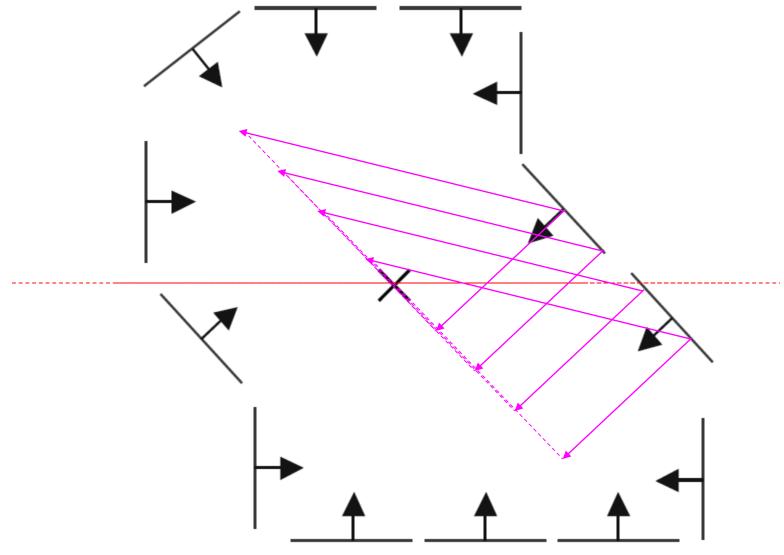
Example: Generalized Hough Transform



Displacement vectors for model points
Slide credit: Svetlana Lazebnik

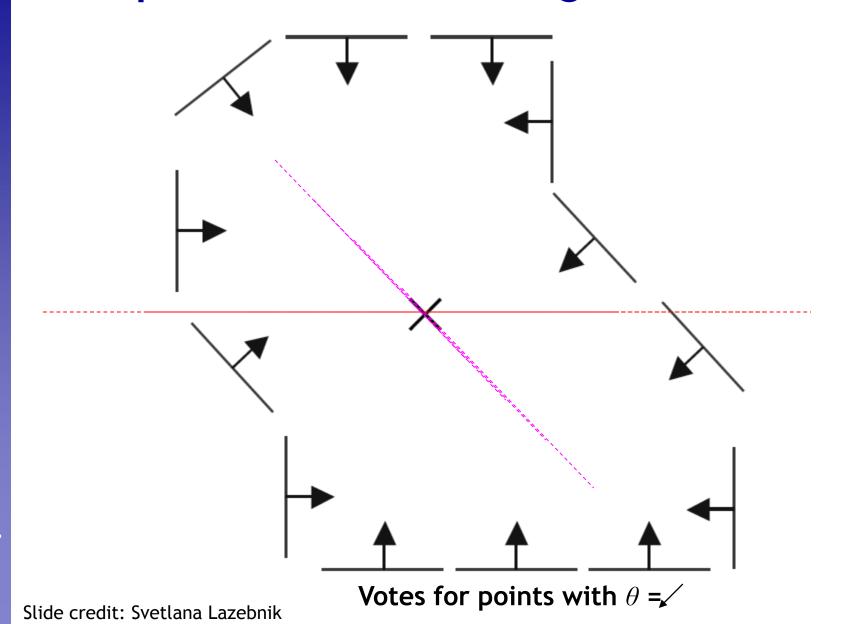
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Example: Generalized Hough Transform



Range of voting locations for test point Slide credit: Svetlana Lazebnik



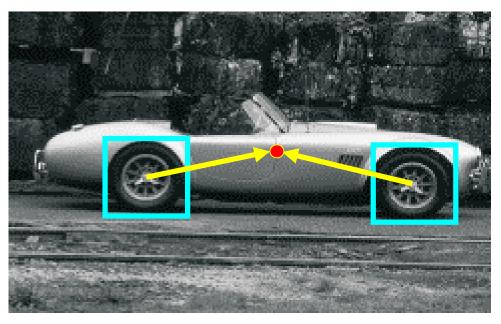


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Application in Recognition

 Instead of indexing displacements by gradient orientation, index by "visual codeword".



Training image



Visual codeword with displacement vectors

B. Leibe, A. Leonardis, and B. Schiele, <u>Robust Object Detection with Interleaved</u>
<u>Categorization and Segmentation</u>, International Journal of Computer Vision, Vol. 77(1-3), 2008.



Application in Recognition

 Instead of indexing displacements by gradient orientation, index by "visual codeword".



Test image

We'll hear more about this in later lectures...



Topics of This Lecture

- Segmentation and grouping
 - Gestalt principles
 - Image Segmentation
- Segmentation as clustering
 - k-Means
 - Feature spaces
- Probabilistic clustering
 - Mixture of Gaussians, EM
- Model-free clustering
 - Mean-Shift clustering



Examples of Grouping in Vision



Determining image regions



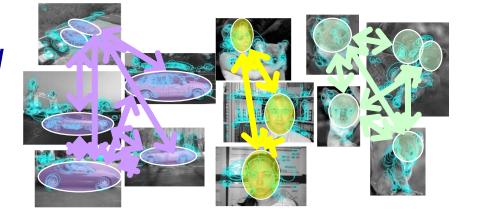
Grouping video frames into shots



Figure-ground

What things should be grouped?

What cues indicate groups?

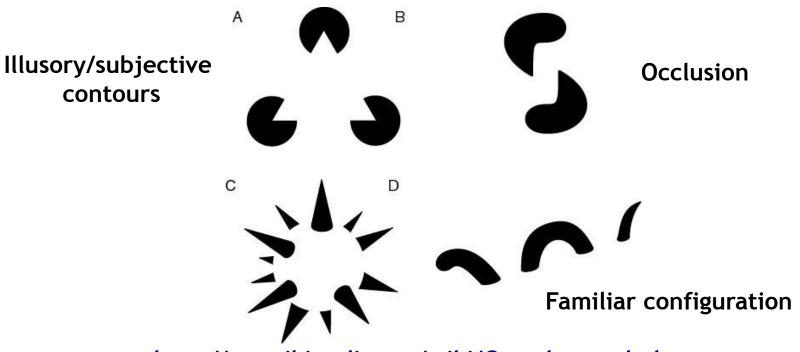


Object-level grouping



The Gestalt School

- Grouping is key to visual perception
- Elements in a collection can have properties that result from relationships
 - "The whole is greater than the sum of its parts"



http://en.wikipedia.org/wiki/Gestalt_psychology

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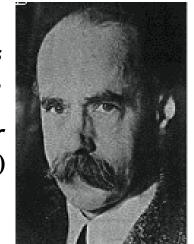


Gestalt Theory

- Gestalt: whole or group
 - Whole is greater than sum of its parts
 - Relationships among parts can yield new properties/features
- Psychologists identified series of factors that predispose set of elements to be grouped (by human visual system)

"I stand at the window and see a house, trees, sky. Theoretically I might say there were 327 brightnesses and nuances of colour. Do I have "327"? No. I have sky, house, and trees."

Max Wertheimer (1880-1943)



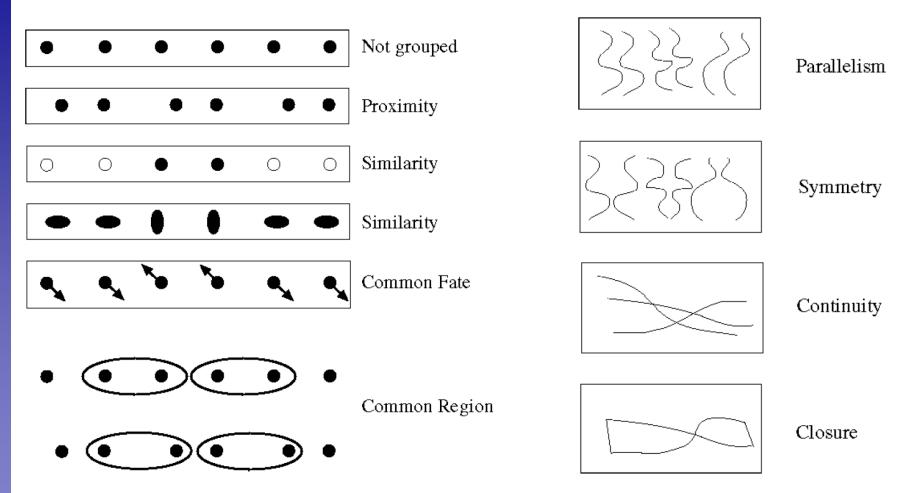
Untersuchungen zur Lehre von der Gestalt,

Psychologische Forschung, Vol. 4, pp. 301-350, 1923

http://psy.ed.asu.edu/~classics/Wertheimer/Forms/forms.htm

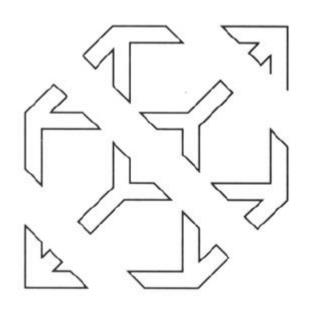


Gestalt Factors

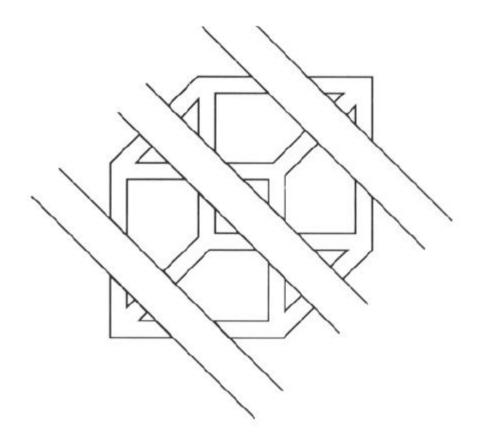


 These factors make intuitive sense, but are very difficult to translate into algorithms.



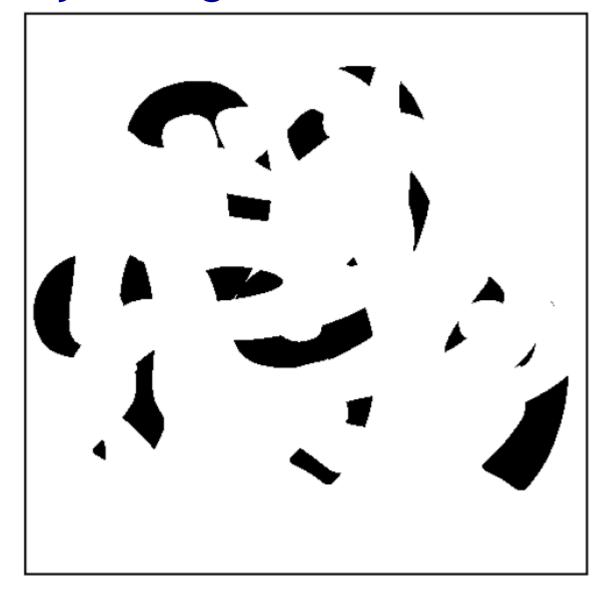






Continuity, explanation by occlusion











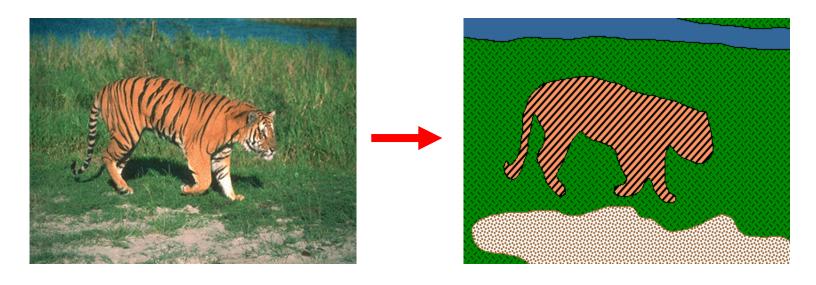
The Ultimate Gestalt?





Image Segmentation

Goal: identify groups of pixels that go together





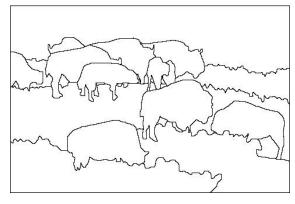
The Goals of Segmentation

Separate image into coherent "objects"

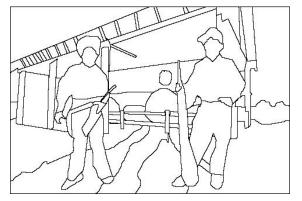
Image



Human segmentation







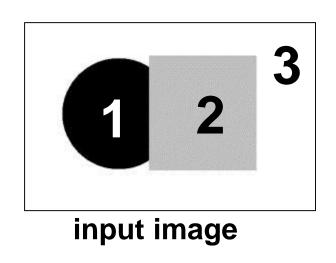


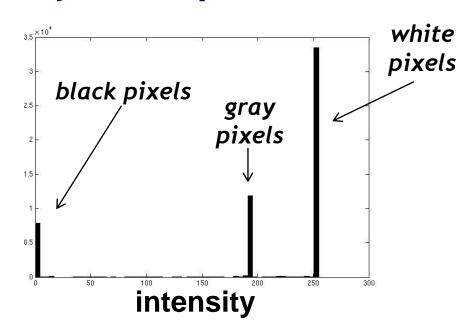
Topics of This Lecture

- Segmentation and grouping
 - Gestalt principles
 - Image Segmentation
- Segmentation as clustering
 - k-Means
 - Feature spaces
- Probabilistic clustering
 - Mixture of Gaussians, EM
- Model-free clustering
 - Mean-Shift clustering



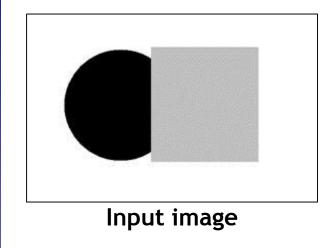
Image Segmentation: Toy Example

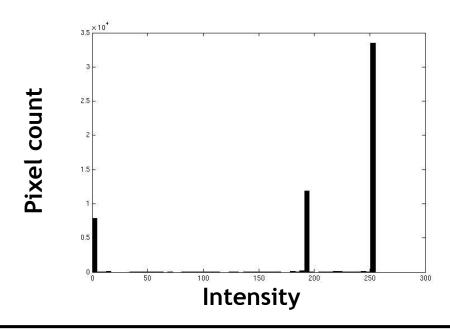


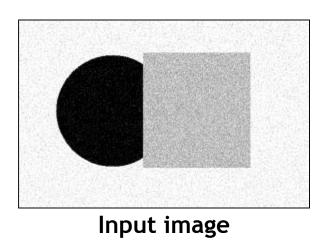


- These intensities define the three groups.
- We could label every pixel in the image according to which of these primary intensities it is.
 - > i.e., segment the image based on the intensity feature.
- What if the image isn't quite so simple?

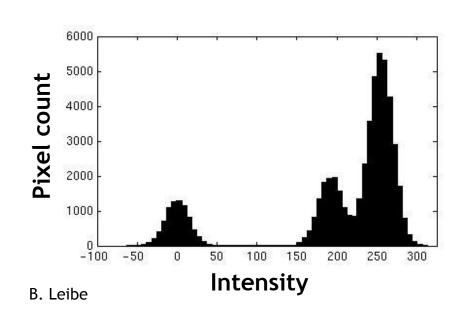
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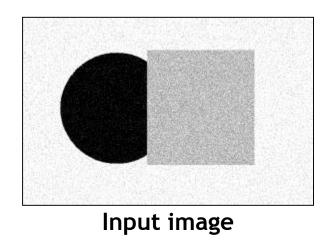


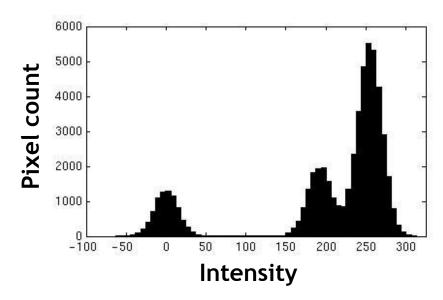


Slide credit: Kristen Grauman

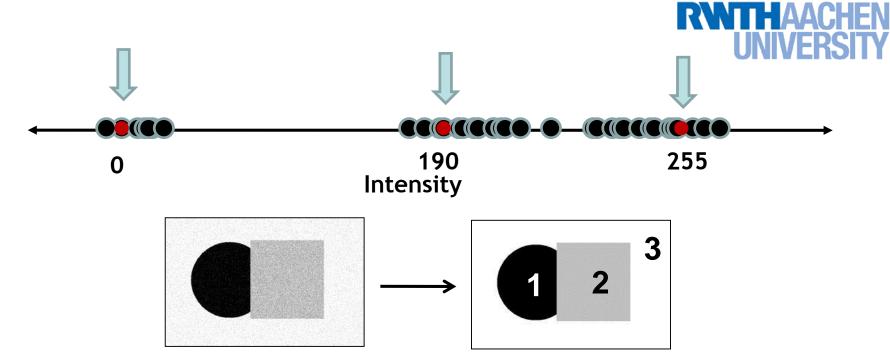








- Now how to determine the three main intensities that define our groups?
- We need to cluster.



- Goal: choose three "centers" as the representative intensities, and label every pixel according to which of these centers it is nearest to.
- Best cluster centers are those that minimize SSD between all points and their nearest cluster center c_i :

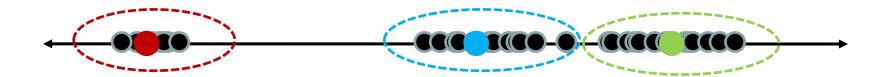
$$\sum_{\text{clusters } i} \sum_{\text{points p in cluster } i} ||p - c_i||^2$$

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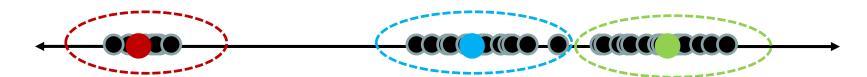


Clustering

- With this objective, it is a "chicken and egg" problem:
 - If we knew the cluster centers, we could allocate points to groups by assigning each to its closest center.



If we knew the group memberships, we could get the centers by computing the mean per group.





K-Means Clustering

- Basic idea: randomly initialize the k cluster centers, and iterate between the two steps we just saw.
 - 1. Randomly initialize the cluster centers, $c_1, ..., c_K$
 - 2. Given cluster centers, determine points in each cluster
 - For each point p, find the closest c_i. Put p into cluster i
 - 3. Given points in each cluster, solve for c_i
 - Set c_i to be the mean of points in cluster i
 - 4. If c_i have changed, repeat Step 2

Properties

- Will always converge to some solution
- Can be a "local minimum"
 - Does not always find the global minimum of objective function:

$$\sum_{\text{clusters } i} \sum_{\text{points p in cluster } i} ||p - c_i||^2$$



Segmentation as Clustering



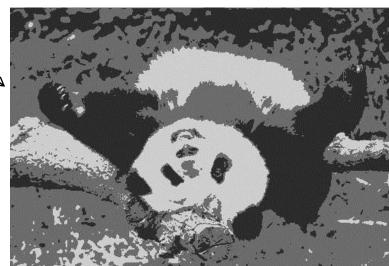


K=3



```
img_as_col = double(im(:));
cluster_membs = kmeans(img_as_col, K);

labelim = zeros(size(im));
for i=1:k
   inds = find(cluster_membs==i);
   meanval = mean(img_as_column(inds));
   labelim(inds) = meanval;
end
```





K-Means++

- Can we prevent arbitrarily bad local minima?
- 1. Randomly choose first center.
- **2.** Pick new center with prob. proportional to $||p-c_i||^2$
 - (Contribution of p to total error)
- 3. Repeat until k centers.
- Expected error = O(log k) * optimal

Arthur & Vassilvitskii 2007



Feature Space

- Depending on what we choose as the feature space, we can group pixels in different ways.
- Grouping pixels based on intensity similarity



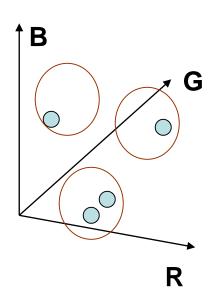


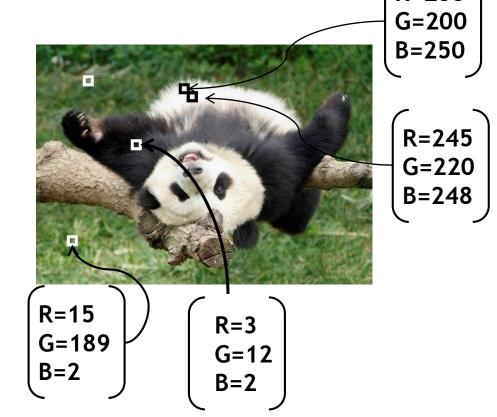
Feature space: intensity value (1D)

Feature Space

Depending on what we choose as the feature space, we can group pixels in different ways.

 Grouping pixels based on color similarity





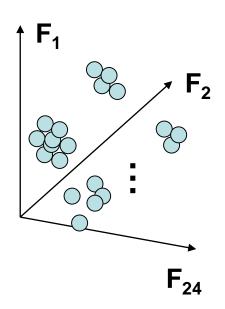
Feature space: color value (3D)

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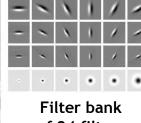


Segmentation as Clustering

- Depending on what we choose as the *feature space*, we can group pixels in different ways.
- Grouping pixels based on texture similarity







of 24 filters

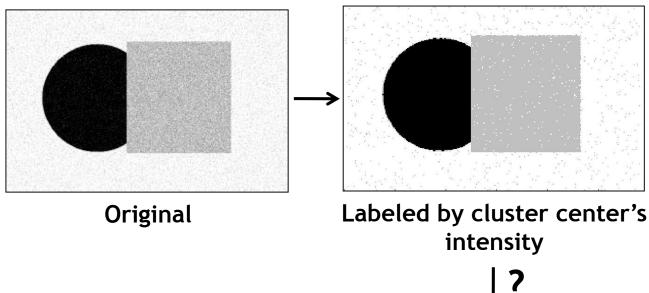
Feature space: filter bank responses (e.g., 24D)

Slide credit: Kristen Grauman

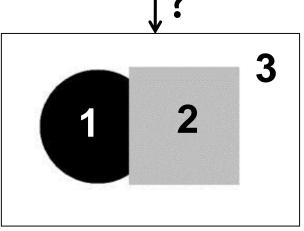


Smoothing Out Cluster Assignments

Assigning a cluster label per pixel may yield outliers:



How can we ensure they are spatially smooth?

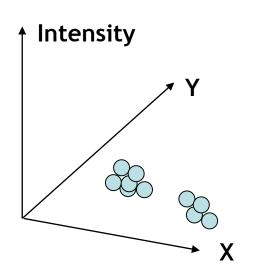


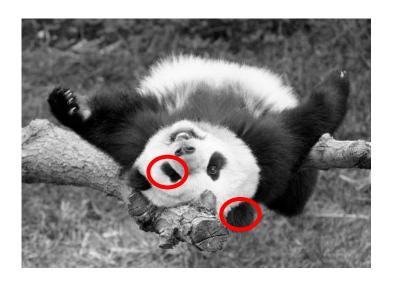
B. Leibe



Segmentation as Clustering

- Depending on what we choose as the feature space, we can group pixels in different ways.
- Grouping pixels based on intensity+position similarity



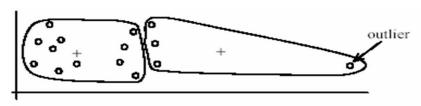


⇒ Simple way to encode both *similarity* and *proximity*.

Summary K-Means

Pros

- Simple, fast to compute
- Converges to local minimum of within-cluster squared error



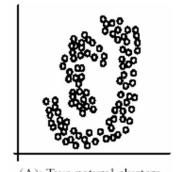
(A): Undesirable clusters

Cons/issues

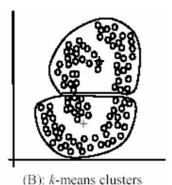
- Setting k?
- Sensitive to initial centers
- Sensitive to outliers
- Detects spherical clusters only
- Assuming means can be computed



(B): Ideal clusters



(A): Two natural clusters



.



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- Model-free clustering
 - Mean-Shift clustering

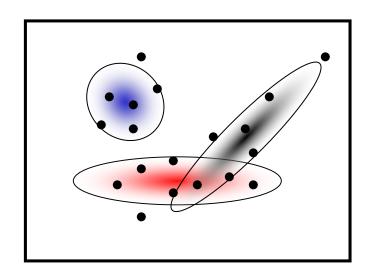


Probabilistic Clustering

- Basic questions
 - \triangleright What's the probability that a point x is in cluster m?
 - What's the shape of each cluster?
- K-means doesn't answer these questions.
- Basic idea
 - Instead of treating the data as a bunch of points, assume that they are all generated by sampling a continuous function.
 - This function is called a generative model.
 - > Defined by a vector of parameters heta



Mixture of Gaussians



- One generative model is a mixture of Gaussians (MoG)
 - ightarrow K Gaussian blobs with means $oldsymbol{\mu}_j$, cov. matrices $oldsymbol{\Sigma}_j$, dim. D

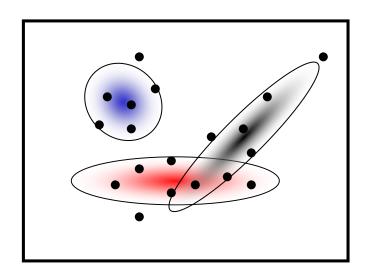
$$p(\mathbf{x}|\theta_j) = \frac{1}{(2\pi)^{D/2} |\mathbf{\Sigma}_j|^{1/2}} \exp\left\{-\frac{1}{2} (\mathbf{x} - \boldsymbol{\mu}_j)^{\mathrm{T}} \mathbf{\Sigma}_j^{-1} (\mathbf{x} - \boldsymbol{\mu}_j)\right\}$$

- ightarrow Blob j is selected with probability π_j
- ightarrow The likelihood of observing ${f x}$ is a weighted mixture of Gaussians

$$p(\mathbf{x}|\theta) = \sum_{j=1}^{\infty} \pi_j p(\mathbf{x}|\theta_j) \qquad \theta = (\pi_1, \boldsymbol{\mu}_1, \boldsymbol{\Sigma}_1, \dots, \pi_M, \boldsymbol{\mu}_M, \boldsymbol{\Sigma}_M)$$



Expectation Maximization (EM)



- Goal
 - \rightarrow Find blob parameters θ that maximize the likelihood function:

$$p(data|\theta) = \prod_{n=1}^{N} p(\mathbf{x}_n|\theta)$$

- Approach:
 - 1. E-step: given current guess of blobs, compute ownership of each point
 - 2. M-step: given ownership probabilities, update blobs to maximize likelihood function
 - 3. Repeat until convergence

EM Algorithm

- See lecture

 Machine Learning!
- Expectation-Maximization (EM) Algorithm
 - E-Step: softly assign samples to mixture components

$$\gamma_j(\mathbf{x}_n) \leftarrow \frac{\pi_j \mathcal{N}(\mathbf{x}_n | \boldsymbol{\mu}_j, \boldsymbol{\Sigma}_j)}{\sum_{k=1}^K \pi_k \mathcal{N}(\mathbf{x}_n | \boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)} \quad \forall j = 1, \dots, K, \quad n = 1, \dots, N$$

M-Step: re-estimate the parameters (separately for each mixture component) based on the soft assignments

$$\hat{N}_j \leftarrow \sum_{n=1}^N \gamma_j(\mathbf{x}_n)$$
 = soft number of samples labeled j
 $\hat{\pi}_j^{ ext{new}} \leftarrow \frac{\hat{N}_j}{N}$
 $\hat{\mu}_j^{ ext{new}} \leftarrow \frac{1}{\hat{N}_j} \sum_{n=1}^N \gamma_j(\mathbf{x}_n) \mathbf{x}_n$
 $\hat{\Sigma}_j^{ ext{new}} \leftarrow \frac{1}{\hat{N}_j} \sum_{n=1}^N \gamma_j(\mathbf{x}_n) (\mathbf{x}_n - \hat{\boldsymbol{\mu}}_j^{ ext{new}}) (\mathbf{x}_n - \hat{\boldsymbol{\mu}}_j^{ ext{new}})^{ ext{T}}$

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Applications of EM

- Turns out this is useful for all sorts of problems
 - Any clustering problem
 - Any model estimation problem
 - Missing data problems
 - Finding outliers
 - Segmentation problems
 - Segmentation based on color
 - Segmentation based on motion
 - Foreground/background separation
 - • •

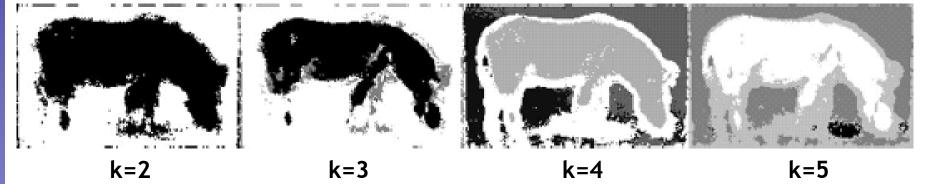


Segmentation with EM

Original image



EM segmentation results





Summary: Mixtures of Gaussians, EM

Pros

- Probabilistic interpretation
- Soft assignments between data points and clusters
- Generative model, can predict novel data points
- Relatively compact storage

Cons

- Local minima
 - k-means is NP-hard even with k=2
- Initialization
 - Often a good idea to start with some k-means iterations.
- Need to know number of components
 - Solutions: model selection (AIC, BIC), Dirichlet process mixture
- Need to choose generative model
- Numerical problems are often a nuisance

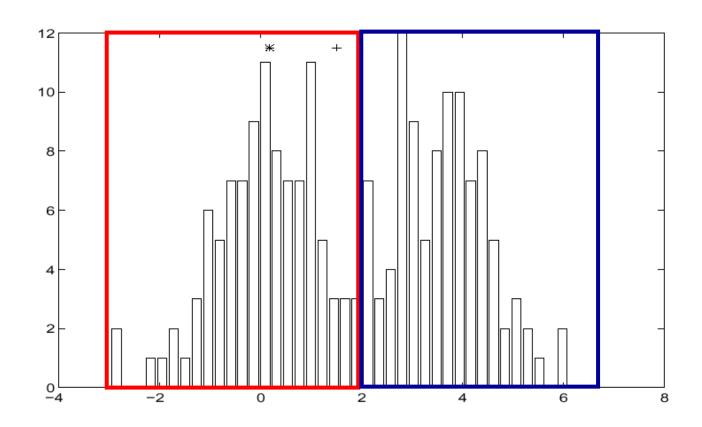


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Finding Modes in a Histogram

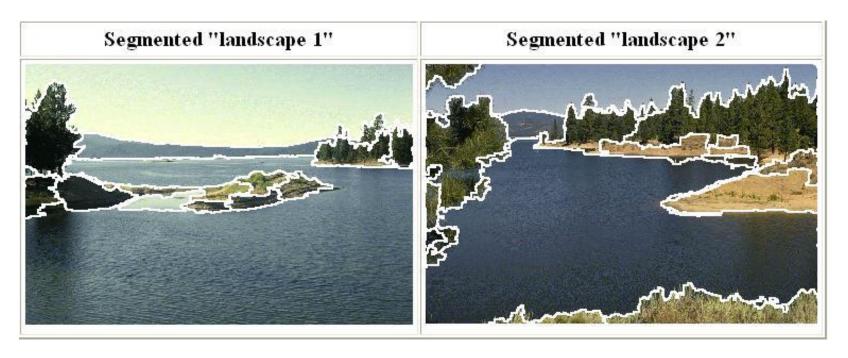


- How many modes are there?
 - Mode = local maximum of the density of a given distribution
 - Easy to see, hard to compute



Mean-Shift Segmentation

 An advanced and versatile technique for clusteringbased segmentation

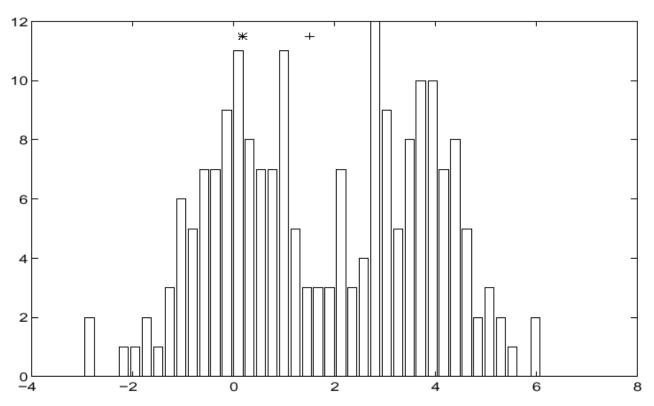


http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html

D. Comaniciu and P. Meer, <u>Mean Shift: A Robust Approach toward Feature Space Analysis</u>, PAMI 2002.

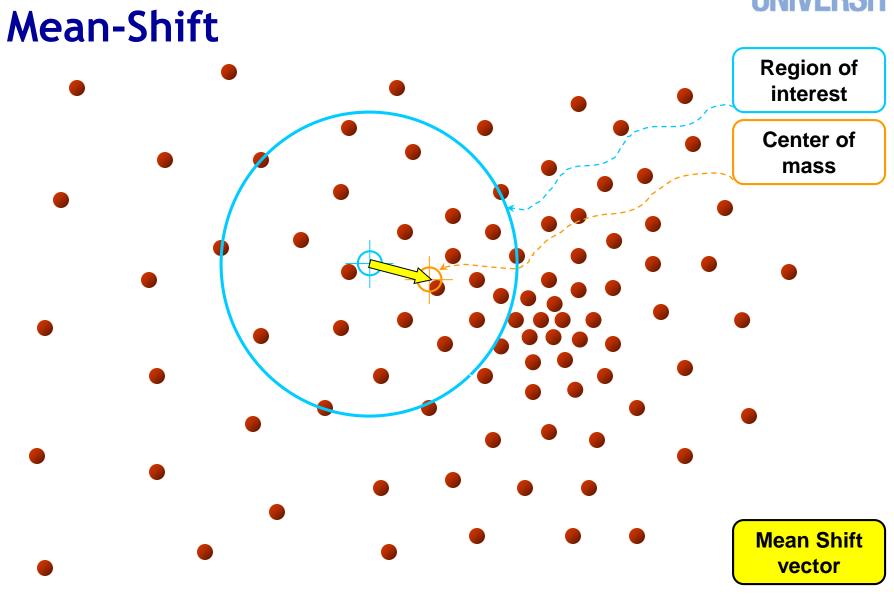


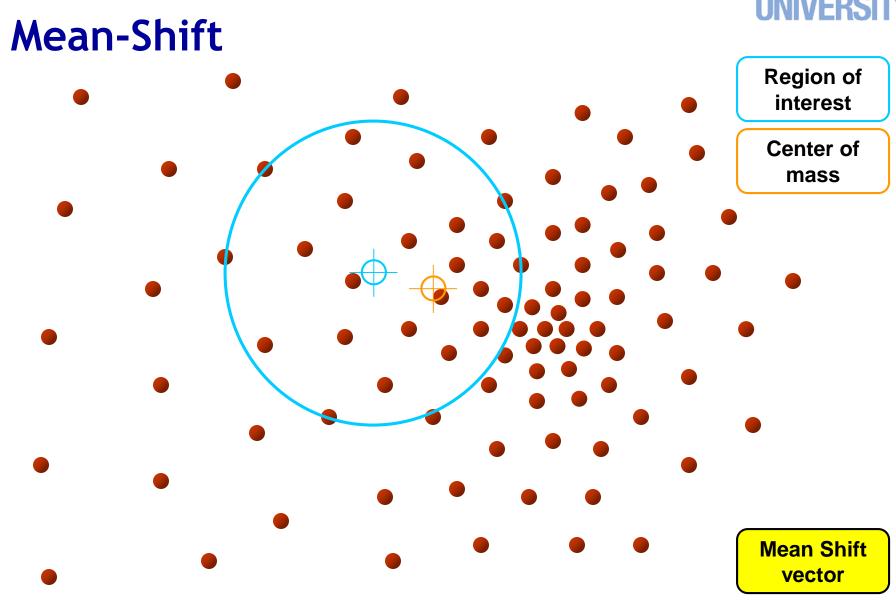
Mean-Shift Algorithm



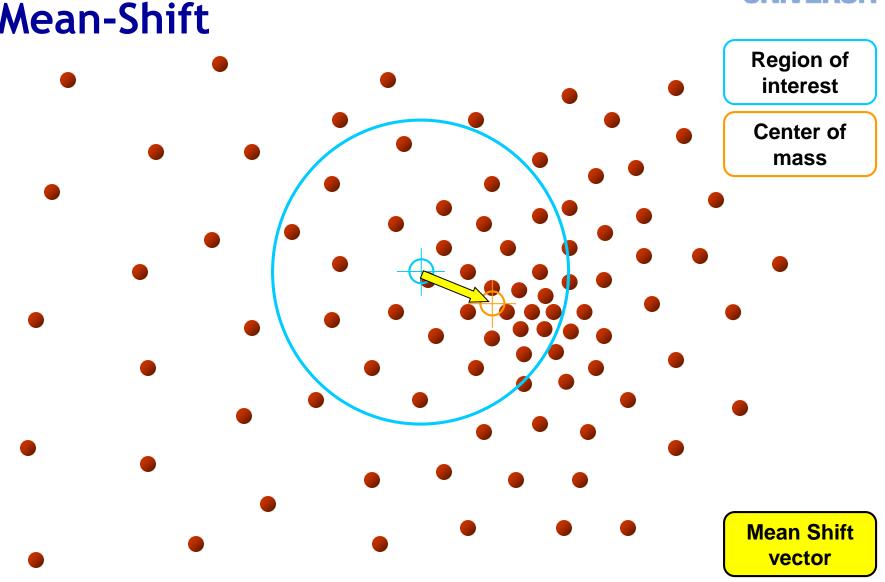
Iterative Mode Search

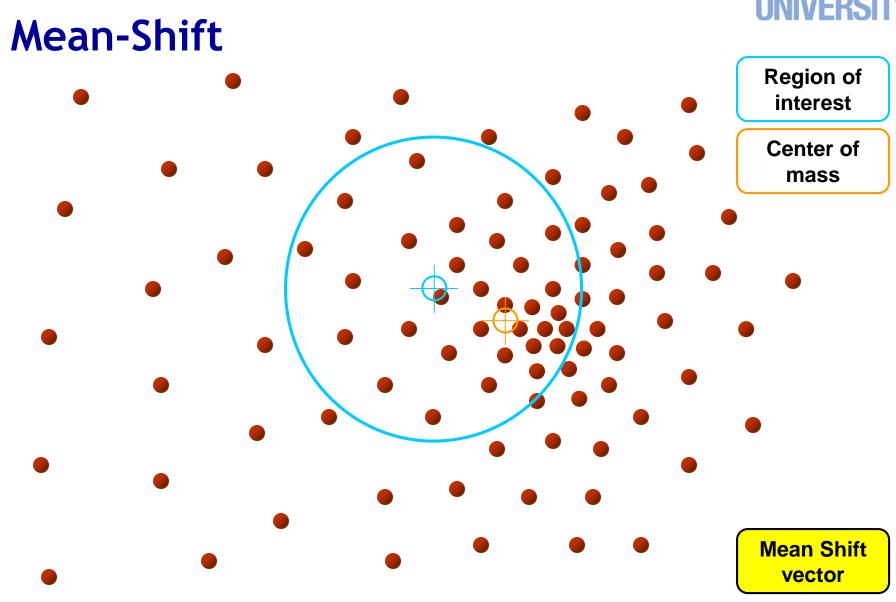
- Initialize random seed, and window W
- Calculate center of gravity (the "mean") of W: $\sum xH(x)$ $x \in W$
- Shift the search window to the mean
- Repeat Step 2 until convergence

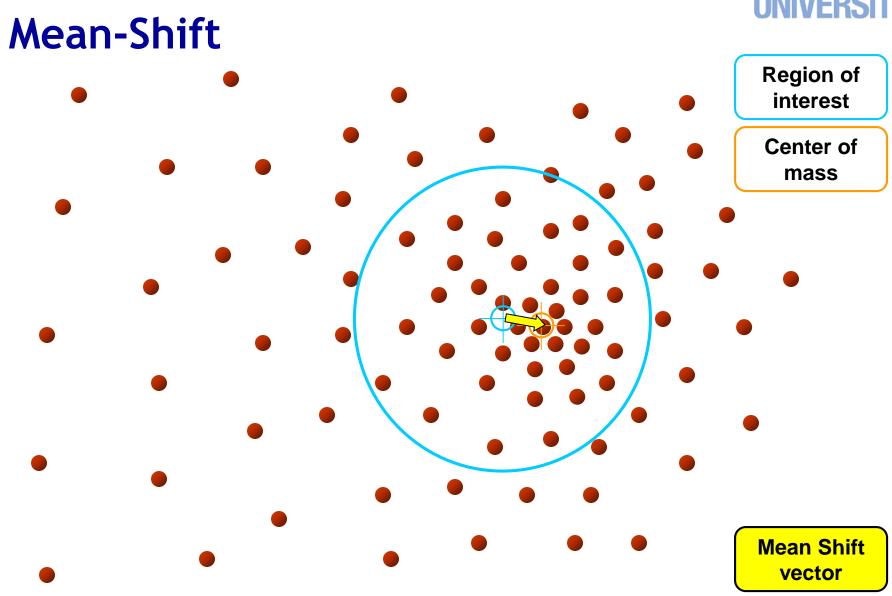




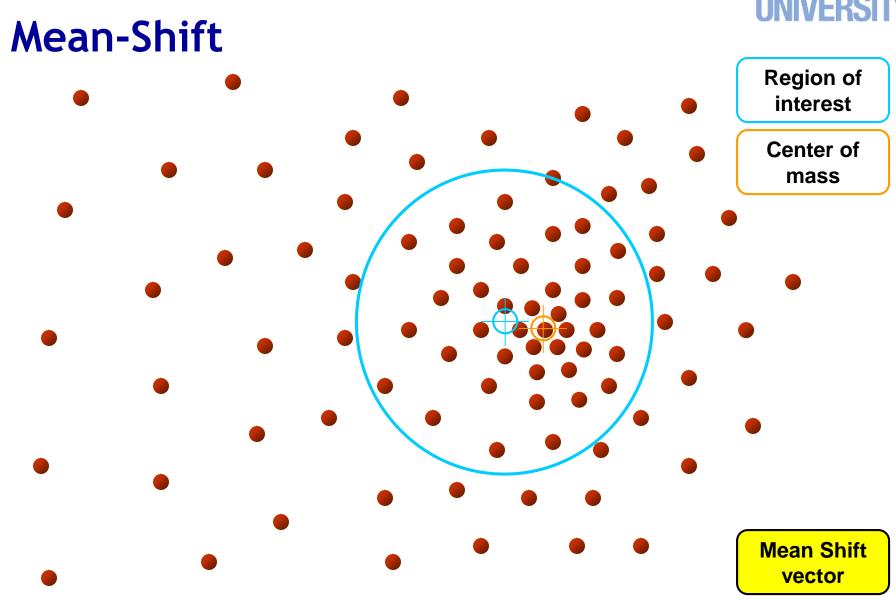




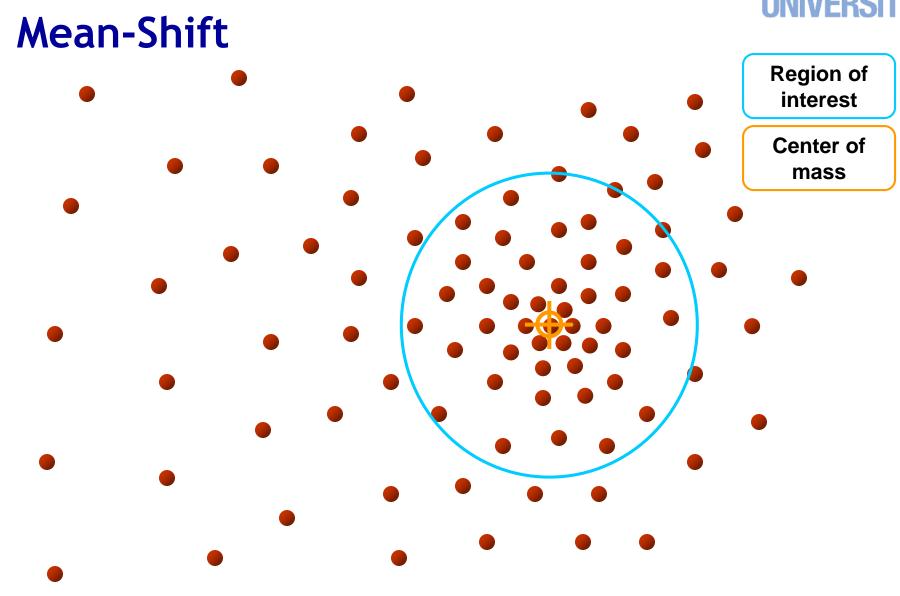






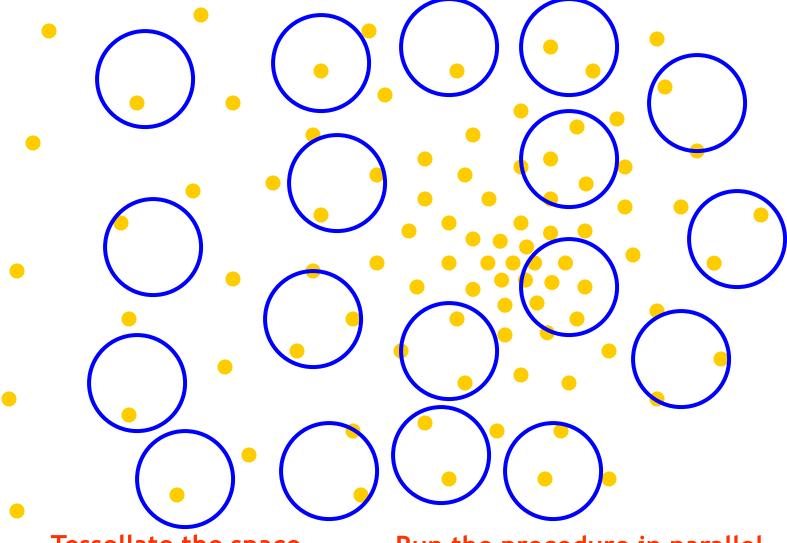








Real Modality Analysis

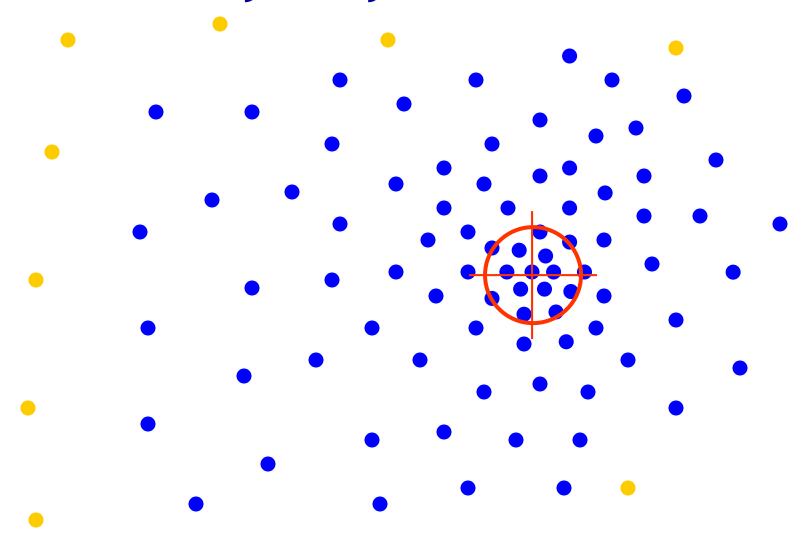


Tessellate the space with windows

Run the procedure in parallel



Real Modality Analysis

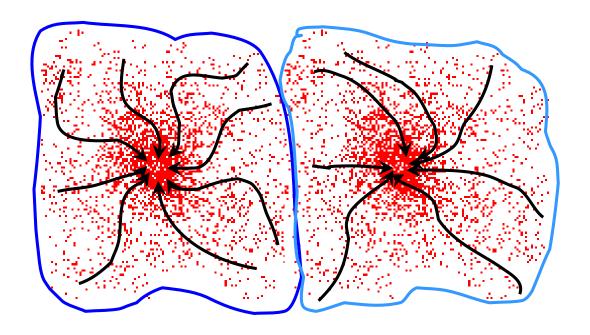


The blue data points were traversed by the windows towards the mode.



Mean-Shift Clustering

- Cluster: all data points in the attraction basin of a mode
- Attraction basin: the region for which all trajectories lead to the same mode

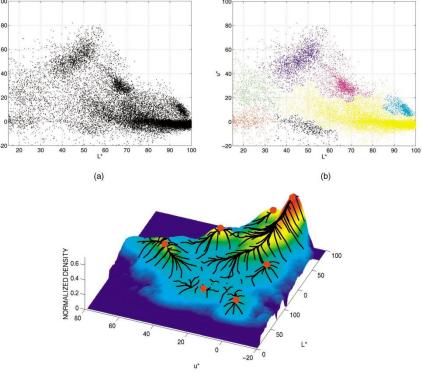




Mean-Shift Clustering/Segmentation

- Find features (color, gradients, texture, etc)
- Initialize windows at individual pixel locations
- Perform mean shift for each window until convergence
- Merge windows that end up near the same "peak" or

mode



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Mean-Shift Segmentation Results





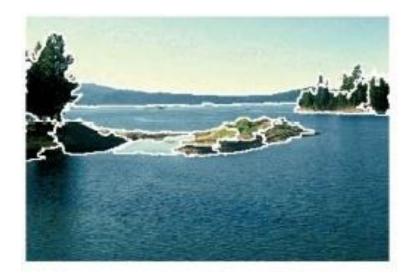




http://www.caip.rutgers.edu/~comanici/MSPAMI/msPamiResults.html

Slide credit: Svetlana Lazebnik

More Results









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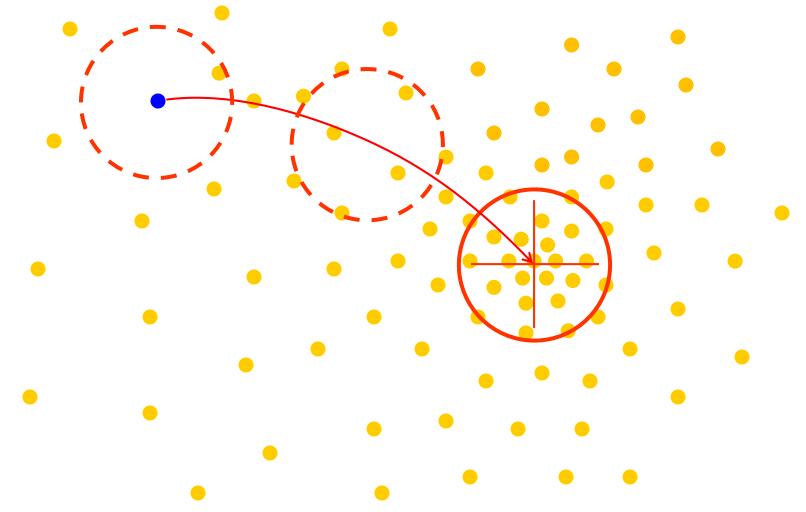
More Results



B. Leibe



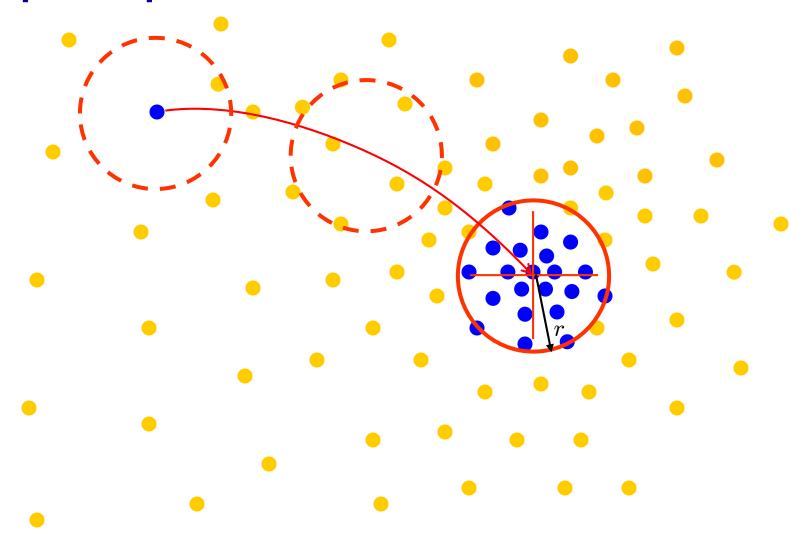
Problem: Computational Complexity



- Need to shift many windows...
- Many computations will be redundant.



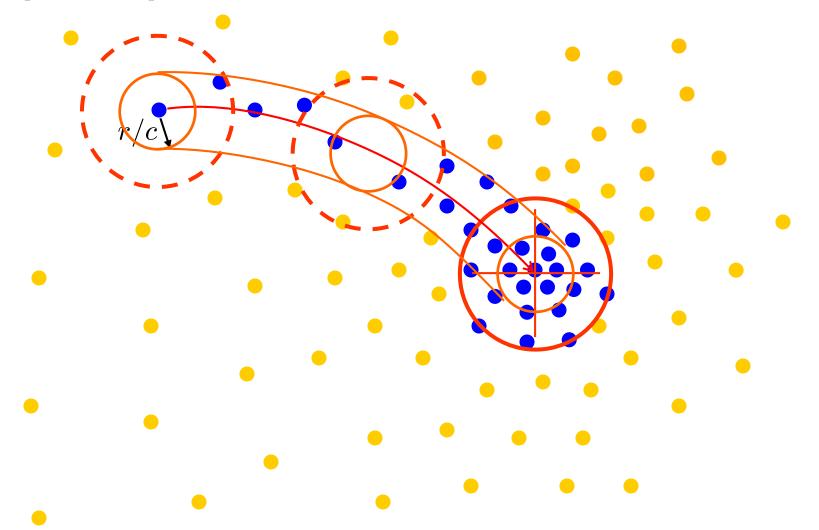
Speedups: Basin of Attraction



1. Assign all points within radius r of end point to the mode.



Speedups



2. Assign all points within radius r/c of the search path to the mode.



Summary Mean-Shift

Pros

- General, application-independent tool
- Model-free, does not assume any prior shape (spherical, elliptical, etc.) on data clusters
- Just a single parameter (window size h)
 - h has a physical meaning (unlike k-means)
- Finds variable number of modes
- Robust to outliers

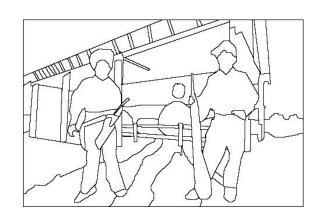
Cons

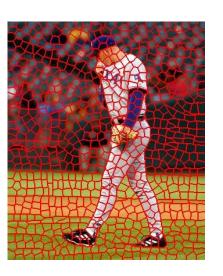
- Output depends on window size
- Window size (bandwidth) selection is not trivial
- Computationally (relatively) expensive (~2s/image)
- Does not scale well with dimension of feature space



Segmentation: Caveats

- We've looked at *bottom-up* ways to segment an image into regions, yet finding meaningful segments is intertwined with the recognition problem.
- Often want to avoid making hard decisions too soon
- Difficult to evaluate; when is a segmentation successful?







Generic Clustering

- We have focused on ways to group pixels into image segments based on their appearance
 - Find groups; "quantize" feature space
- In general, we can use clustering techniques to find groups of similar "tokens", provided we know how to compare the tokens.
 - E.g., segment an image into the types of motions present
 - > E.g., segment a video into the types of scenes (shots) present



References and Further Reading

- Background information on segmentation by clustering can be found in Chapter 14 of
 - D. Forsyth, J. Ponce,
 Computer Vision A Modern Approach.
 Prentice Hall, 2003
- More on the EM algorithm can be found in Chapter 16.1.2.

