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Computer Vision - Lecture 17

Epipolar Geometry & Stereo Basics

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Course Outline

- Image Processing Basics
- Segmentation & Grouping
- Object Recognition
- Local Features & Matching
- Object Categorization
- 3D Reconstruction
 - Epipolar Geometry and Stereo Basics
 - Camera calibration & Uncalibrated Reconstruction
 - Multi-view Stereo
- Optical Flow

4

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Recap: R-CNN for Object Detection

Classify regions with SVMs

Forward each region through ConvNet

Warped image regions

Regions of Interest (RoI) from a proposal method (~2k)

Input image

Slide credit: Ross Girshick

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Recap: Faster R-CNN

- One network, four losses
 - Remove dependence on external region proposal algorithm.
 - Instead, infer region proposals from same CNN.
 - Feature sharing
 - Joint training

⇒ Object detection in a single pass becomes possible.

Classification loss

Bounding-box regression loss

RoI pooling

Region Proposal Network

feature map

Image

Slide credit: Ross Girshick

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Recap: Fully Convolutional Networks

- CNN
- FCN
- Intuition
 - Think of FCNs as performing a sliding-window classification, producing a heatmap of output scores for each class

convolutionalization

tabby cat heatmap

Image source: Long, Shelhamer, Darrell

8

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Recap: Semantic Image Segmentation




- Encoder-Decoder Architecture
 - Problem: FCN output has low resolution
 - Solution: perform upsampling to get back to desired resolution
 - Use skip connections to preserve higher-resolution information

Image source: Newell et al

9

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Recap: FCNs for Human Pose Estimation

- Input data**
 - Image
 
 - Keypoints
 
 - Labels
 
- Task setup**
 - Annotate images with keypoints for skeleton joints
 - Define a target disk around each keypoint with radius r
 - Set the ground-truth label to 1 within each such disk
 - Infer heatmaps for the joints as in semantic segmentation

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Discriminative Face Embeddings

- Learning an embedding using a Triplet Loss Network
 - Present the network with triplets of examples
 - Negative
 
 - Anchor
 
 - Positive
 
 - Apply triplet loss to learn an embedding $f(\cdot)$ that groups the positive example closer to the anchor than the negative one.

$$\|f(x_i^a) - f(x_i^p)\|_2^2 < \|f(x_i^a) - f(x_i^n)\|_2^2$$

12

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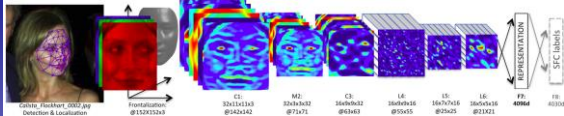
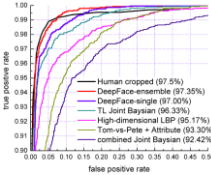
Topics of This Lecture

- Geometric vision**
 - Visual cues
 - Stereo vision
- Epipolar geometry**
 - Depth with stereo
 - Geometry for a simple stereo system
 - Case example with parallel optical axes
 - General case with calibrated cameras
- Stereopsis & 3D Reconstruction**
 - Correspondence search
 - Additional correspondence constraints
 - Possible sources of error
 - Applications

14

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Other Tasks: Face Verification

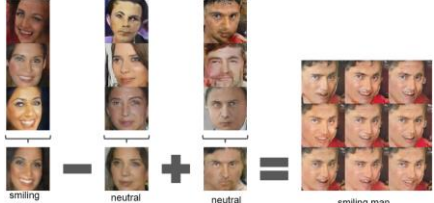



Method	True Positive Rate (at 0.1 FPR)
Human cropped	97.5%
DeepFace-ensemble	97.35%
DeepFace-ensemble	97.35%
TL Joint Bayesian	96.33%
High-dimensional LBP	95.17%
Toni vs. Pate + Attributes	93.32%
combined Joint Bayesian	92.42%

11

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Vector Arithmetics in Embedding Space


- Learned embeddings often preserve linear regularities between concepts
 - Analogy questions can be answered through simple algebraic operations with the vector representation of words.
 - E.g., $\text{vec}(\text{"King"}) - \text{vec}(\text{"Man"}) + \text{vec}(\text{"Woman"}) \approx \text{vec}(\text{"Queen"})$
 - E.g.,
 

13

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Geometric vision

- Goal: Recovery of 3D structure**
 - What cues in the image allow us to do this?

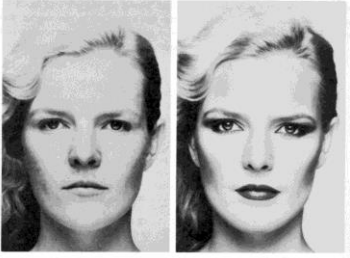


15

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Visual Cues

- Shading



Merle Norman Cosmetics, Los Angeles

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Visual Cues

- Shading
- Texture



The Visual Cliff, by William Vandivert, 1960

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Visual Cues

- Shading
- Texture
- Focus



From *The Art of Photography*, Canon

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Visual Cues

- Shading
- Texture
- Focus
- Perspective



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Visual Cues

- Shading
- Texture
- Focus
- Perspective
- Motion



Figures from L. Zhang

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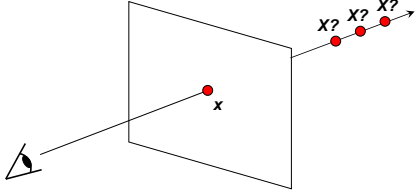
20

Slide credit: Steve Seitz, Kristen Grauman <http://www.brainconnection.com/teasers/2main-illusion/motion-shape>

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Our Goal: Recovery of 3D Structure

- We will focus on perspective and motion
- We need *multi-view geometry* because recovery of structure from one image is inherently ambiguous



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To Illustrate This Point...

- Structure and depth are inherently ambiguous from single views.




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Stereo Vision




http://www.well.com/~jim/stereo/stereo_list.html

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What Is Stereo Vision?

- Generic problem formulation: given several images of the same object or scene, compute a representation of its 3D shape

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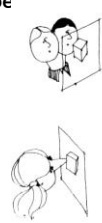
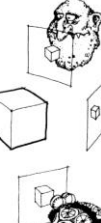

24

Slide credit: Svetlana Lazebnik, Steve Seitz, B. Leibe

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What Is Stereo Vision?

- Generic problem formulation: given several images of the same object or scene, compute a representation of its 3D shape

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What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image

Image 1






Image 2



Dense depth map



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What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
 - Humans can do it




Stereograms: Invented by Sir Charles Wheatstone, 1838

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What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
 - Humans can do it



Autostereograms: <http://www.magiceye.com>

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What Is Stereo Vision?

- Narrower formulation: given a calibrated binocular stereo pair, fuse it to produce a depth image.
 - Humans can do it



Autostereograms: <http://www.magiceye.com>


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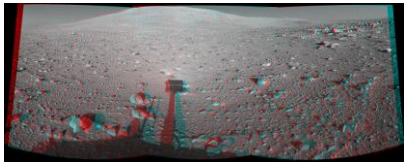
Application of Stereo: Robotic Exploration



Nomad robot searches for meteorites in Antarctica



Real-time stereo on Mars



30

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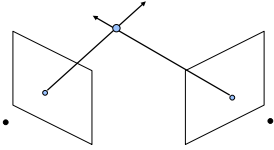
31

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Depth with Stereo: Basic Idea



- Basic Principle: Triangulation
 - Gives reconstruction as intersection of two rays
 - Requires
 - Camera pose (calibration)
 - Point correspondence

32

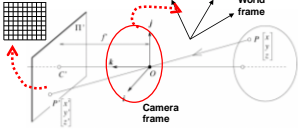
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Camera Calibration



Extrinsic parameters:
Camera frame ↔ Reference frame

Intrinsic parameters:
Image coordinates relative to camera ↔ Pixel coordinates

- Parameters
 - Extrinsic: rotation matrix and translation vector
 - Intrinsic: focal length, pixel sizes (mm), image center point, radial distortion parameters

We'll assume for now that these parameters are given and fixed.

33

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Geometry for a Simple Stereo System

- First, assuming parallel optical axes, known camera parameters (i.e., calibrated cameras):

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Geometry for a Simple Stereo System

- Assume parallel optical axes, known camera parameters (i.e., calibrated cameras). We can triangulate via:

Similar triangles (p_l, P, p_r) and (O_l, P, O_r):

$$\frac{T - (x_r - x_l)}{Z - f} = \frac{T}{Z}$$

$$Z = f \frac{T}{x_r - x_l}$$

“disparity” → $x_r - x_l$

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Depth From Disparity

Image $I(x, y)$

Disparity map $D(x, y)$

Image $I'(x', y')$

$$(x', y') = (x + D(x, y), y)$$

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General Case With Calibrated Cameras

- The two cameras need not have parallel optical axes.

vs.

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Stereo Correspondence Constraints

p

p'?

- Given p in the left image, where can the corresponding point p' in the right image be?

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Stereo Correspondence Constraints

- Given p in the left image, where can the corresponding point p' in the right image be?

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Stereo Correspondence Constraints

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Stereo Correspondence Constraints

- Geometry of two views allows us to constrain where the corresponding pixel for some image point in the first view must occur in the second view.

- Epipolar constraint: Why is this useful?**
 - Reduces correspondence problem to 1D search along conjugate epipolar lines.

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Epipolar Geometry

- Epipolar Plane
- Baseline
- Epipoles
- Epipolar Lines

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Slide adapted from Marc Pollefeys

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Epipolar Geometry: Terms

- Baseline**
 - Line joining the camera centers
- Epipole**
 - Point of intersection of baseline with the image plane
- Epipolar plane**
 - Plane containing baseline and world point
- Epipolar line**
 - Intersection of epipolar plane with the image plane
- Properties**
 - All epipolar lines intersect at the epipole.
 - An epipolar plane intersects the left and right image planes in epipolar lines.

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Epipolar Constraint

- Potential matches for p have to lie on the corresponding epipolar line l' .
- Potential matches for p' have to lie on the corresponding epipolar line l .

<http://www.ai.sri.com/~luong/research/Meta3DViewer/EpipolarGeo.html>

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Example

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Example: Converging Cameras

As position of 3D point varies, epipolar lines "rotate" about the baseline

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Example: Motion Parallel With Image Plane

e at infinity e' at infinity

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Example: Forward Motion

- Epipole has same coordinates in both images.
- Points move along lines radiating from e : "Focus of expansion"

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Let's Formalize This!

- For a given stereo rig, how do we express the epipolar constraints algebraically?
- For this, we will need some linear algebra.
- But don't worry! We'll go through it step by step...

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Stereo Geometry With Calibrated Cameras

- If the rig is calibrated, we know:
 - How to rotate and translate camera reference frame 1 to get to camera reference frame 2.
 - Rotation: 3×3 matrix; translation: 3 vector.

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Rotation Matrix

$$\mathbf{R}_x(\alpha) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{bmatrix}$$

Express 3D rotation as series of rotations around coordinate axes by angles α, β, γ

$$\mathbf{R}_y(\beta) = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix}$$

Overall rotation is product of these elementary rotations:

$$\mathbf{R}_z(\gamma) = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

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3D Rigid Transformation

$$\begin{bmatrix} X' \\ Y' \\ Z' \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} + \begin{bmatrix} T_x \\ T_y \\ T_z \end{bmatrix}$$

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

53

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Stereo Geometry With Calibrated Cameras

• Camera-centered coordinate systems are related by known rotation \mathbf{R} and translation \mathbf{T} :

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

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Excursion: Cross Product

$$\vec{a} \times \vec{b} = \vec{c}$$

$$\vec{a} \cdot \vec{c} = 0$$

$$\vec{b} \cdot \vec{c} = 0$$

- Vector cross product takes two vectors and returns a third vector that's perpendicular to both inputs.
- So here, c is perpendicular to both a and b , which means the dot product is 0.

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From Geometry to Algebra

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

$$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{X}') = \mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X})$$

$$0 = \mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X})$$

$$\underbrace{\mathbf{T} \times \mathbf{X}'}_{\text{Normal to the plane}} = \mathbf{T} \times \mathbf{R}\mathbf{X} + \mathbf{T} \times \mathbf{T}$$

$$= \mathbf{T} \times \mathbf{R}\mathbf{X}$$

56

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Matrix Form of Cross Product

$$\vec{a} \times \vec{b} = \vec{c}$$

$$\vec{a} \cdot \vec{c} = 0$$

$$\vec{b} \cdot \vec{c} = 0$$

“skew symmetric” matrix

$$[a_{\times}] = \begin{bmatrix} 0 & -a_z & a_y \\ a_z & 0 & -a_x \\ -a_y & a_x & 0 \end{bmatrix}$$

$$\vec{a} \times \vec{b} = [a_{\times}] \vec{b}$$

57

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From Geometry to Algebra

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

$$\mathbf{T} \times \mathbf{X}' = \mathbf{T} \times \mathbf{R}\mathbf{X} + \mathbf{T} \times \mathbf{T}$$

$$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{X}') = \mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X})$$

$$0 = \mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X})$$

Normal to the plane
 $= \mathbf{T} \times \mathbf{R}\mathbf{X}$

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Essential Matrix

$$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X}) = 0$$

$$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X}) = 0$$

Let $\mathbf{E} = \mathbf{T} \times \mathbf{R}$

$$\mathbf{X}'^T \mathbf{E} \mathbf{X} = 0$$

- This holds for the rays p and p' that are parallel to the camera-centered position vectors X and X' , so we have: $\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$
- \mathbf{E} is called the **essential matrix**, which relates corresponding image points [Longuet-Higgins 1981]

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Essential Matrix and Epipolar Lines

$$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$$

Epipolar constraint: if we observe point p in one image, then its position p' in second image must satisfy this equation.

$\mathbf{l}' = \mathbf{E} \mathbf{p}$ is the coordinate vector representing the epipolar line for point p (i.e., the line is given by: $\mathbf{l}'^T \mathbf{x} = 0$)

$\mathbf{l} = \mathbf{E}^T \mathbf{p}'$ is the coordinate vector representing the epipolar line for point p'

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Essential Matrix: Properties

- Relates image of corresponding points in both cameras, given rotation and translation.
- Assuming intrinsic parameters are known

$$\mathbf{E} = \mathbf{T} \times \mathbf{R}$$

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Essential Matrix Example: Parallel Cameras

$$\mathbf{R} = \mathbf{I}$$

$$\mathbf{T} = [-d, 0, 0]^T$$

$$\mathbf{E} = [\mathbf{T} \times] \mathbf{R}$$

$$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$$

For the parallel cameras, image of any point must lie on same horizontal line in each image plane.

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Essential Matrix Example: Parallel Cameras

$$\mathbf{R} = \mathbf{I}$$

$$\mathbf{T} = [-d, 0, 0]^T$$

$$\mathbf{E} = [\mathbf{T} \times] \mathbf{R} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & d \\ 0 & -d & 0 \end{bmatrix}$$

$$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$$

$$\begin{bmatrix} x' & y' & f \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & d \\ 0 & -d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ f \end{bmatrix} = 0$$

$$\Leftrightarrow \begin{bmatrix} x' & y' & f \end{bmatrix} \begin{bmatrix} 0 \\ df \\ -dy \end{bmatrix} = 0$$

$$\Leftrightarrow y = y'$$


For the parallel cameras, image of any point must lie on same horizontal line in each image plane.

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More General Case

Image $I(x,y)$



Disparity map $D(x,y)$





Image $I'(x',y')$



$(x', y') = (x + D(x, y), y)$

What about when cameras' optical axes are not parallel?

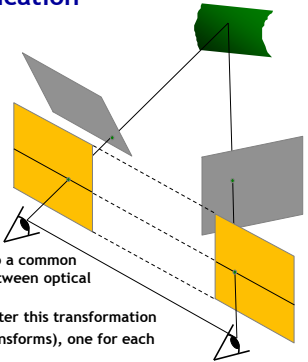
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Stereo Image Rectification

- In practice, it is convenient if image scanlines are the epipolar lines.



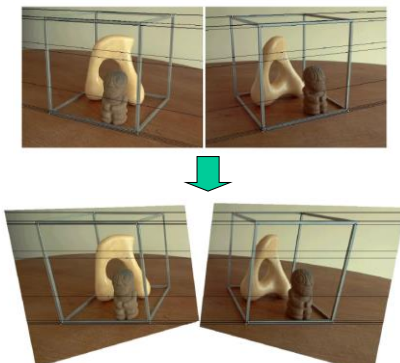
- Algorithm**
 - Reproject image planes onto a common plane parallel to the line between optical centers
 - Pixel motion is horizontal after this transformation
 - Two homographies (3×3 transforms), one for each input image reprojection

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Slide adapted from Li Zhang, C. Loop & Z. Zhang, Computing Rectifying Homographies for Stereo Vision, CVPR'99

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Stereo Image Rectification: Example



Source: Aljoshia Efros

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Stereo Reconstruction

- Main Steps**
 - Calibrate cameras
 - Rectify images
 - Compute disparity**
 - Estimate depth

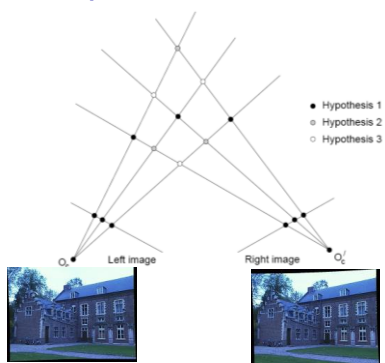


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Correspondence Problem




Multiple match hypotheses satisfy epipolar constraint, but which is correct?

- Hypothesis 1
- Hypothesis 2
- Hypothesis 3



Left image



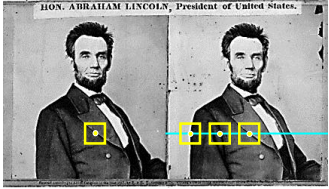
Right image

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Slide credit: Kristen Grauman B. Leibe Figure from Gee & Cicola, 1999

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Dense Correspondence Search



HON. ABRAHAM LINCOLN, President of United States.

- For each pixel in the first image
 - Find corresponding epipolar line in the right image
 - Examine all pixels on the epipolar line and pick the best match (e.g. SSD, correlation)
 - Triangulate the matches to get depth information
- This is easiest when epipolar lines are scanlines
 - ⇒ Rectify images first

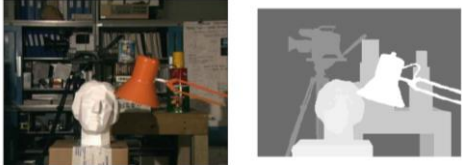
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adapted from Svetlana Lazebnik, Li Zhang

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Example: Window Search

- Data from University of Tsukuba



Scene Ground truth

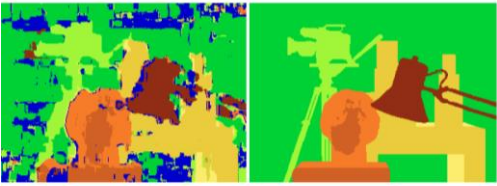
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Example: Window Search

- Data from University of Tsukuba




Window-based matching (best window size) Ground truth

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Effect of Window Size



$W = 3$ $W = 20$

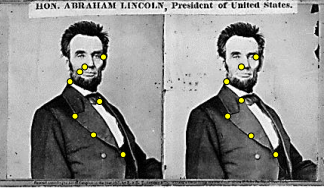
Want window large enough to have sufficient intensity variation, yet small enough to contain only pixels with about the same disparity.

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Alternative: Sparse Correspondence Search



HON. ABRAHAM LINCOLN, President of United States.

- Idea: Restrict search to sparse set of detected features
- Rather than pixel values (or lists of pixel values) use *feature descriptor* and an associated *feature distance*
- Still narrow search further by epipolar geometry

What would make good features?

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Dense vs. Sparse

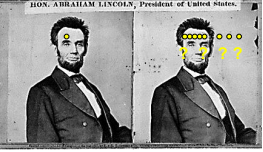
- Sparse
 - Efficiency
 - Can have more reliable feature matches, less sensitive to illumination than raw pixels
 - But...
 - Have to know enough to pick good features
 - Sparse information
- Dense
 - Simple process
 - More depth estimates, can be useful for surface reconstruction
 - But...
 - Breaks down in textureless regions anyway
 - Raw pixel distances can be brittle
 - Not good with very different viewpoints

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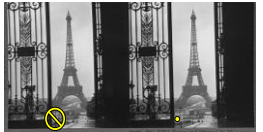
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Difficulties in Similarity Constraint



Untextured surfaces



Occlusions

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Possible Sources of Error?

- Low-contrast / textureless image regions
- Occlusions
- Camera calibration errors
- Violations of *brightness constancy* (e.g., specular reflections)
- Large motions

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Application: View Interpolation




Right Image

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Application: View Interpolation




Left Image

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Application: View Interpolation



Disparity

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Application: View Interpolation



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Application: Free-Viewpoint Video



<http://www.liberovision.com>

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83

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Summary: Stereo Reconstruction


- Main Steps
 - Calibrate cameras
 - Rectify images
 - Compute disparity
 - Estimate depth
- So far, we have only considered calibrated cameras...
- Next lecture
 - Uncalibrated cameras
 - Camera parameters
 - Revisiting epipolar geometry
 - Robust fitting




Left



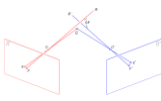
Right



Left



Right



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84


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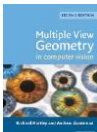
References and Further Reading

- Background information on epipolar geometry and stereopsis can be found in Chapters 10.1-10.2 and 11.1-11.3 of

D. Forsyth, J. Ponce,
Computer Vision - A Modern Approach.
Prentice Hall, 2003


- More detailed information (if you really want to implement 3D reconstruction algorithms) can be found in Chapters 9 and 10 of

R. Hartley, A. Zisserman
Multiple View Geometry in Computer Vision
2nd Ed., Cambridge Univ. Press, 2004



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85

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