

Machine Learning – Lecture 16

Convolutional Neural Networks II

18.12.2017

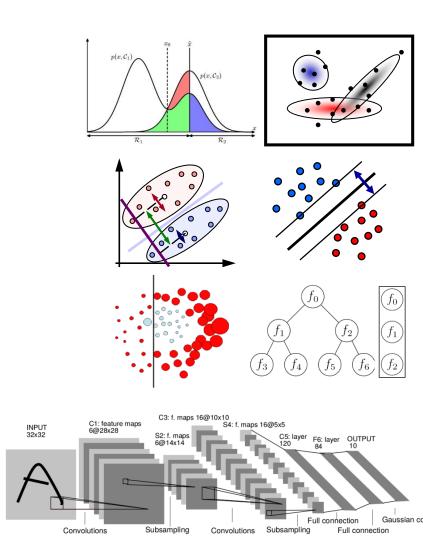
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Course Outline

- Fundamentals
 - Bayes Decision Theory
 - Probability Density Estimation
- Classification Approaches
 - Linear Discriminants
 - Support Vector Machines
 - Ensemble Methods & Boosting
 - Random Forests
- Deep Learning
 - Foundations
 - Convolutional Neural Networks
 - Recurrent Neural Networks



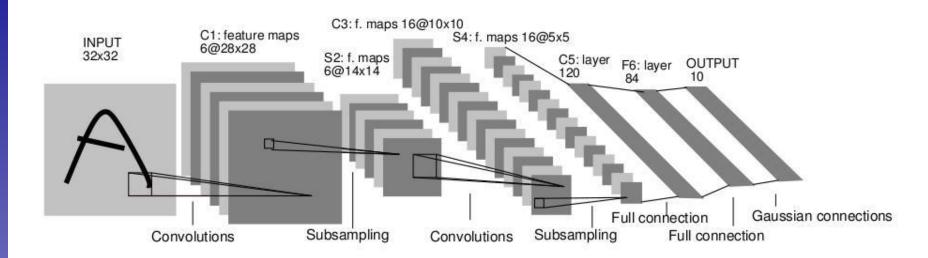


Topics of This Lecture

- Recap: CNNs
- CNN Architectures
 - LeNet
 - AlexNet
 - VGGNet
 - GoogLeNet
 - ResNets
- Visualizing CNNs
 - Visualizing CNN features
 - Visualizing responses
 - Visualizing learned structures
- Applications



Recap: Convolutional Neural Networks

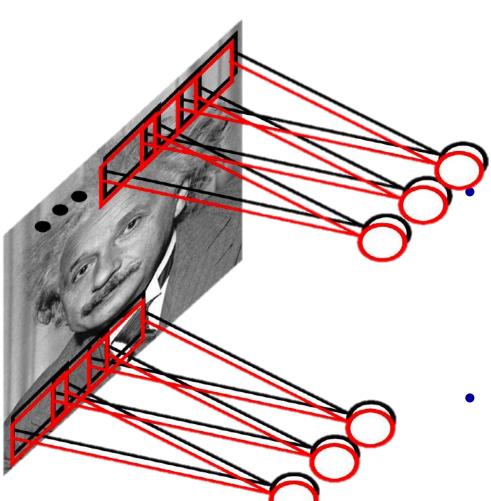


- Neural network with specialized connectivity structure
 - Stack multiple stages of feature extractors
 - Higher stages compute more global, more invariant features
 - Classification layer at the end

Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, <u>Gradient-based learning applied to document recognition</u>, Proceedings of the IEEE 86(11): 2278–2324, 1998.



Recap: Intuition of CNNs



Slide adapted from Marc'Aurelio Ranzato

Convolutional net

- Share the same parameters across different locations
- Convolutions with learned kernels

Learn *multiple* filters

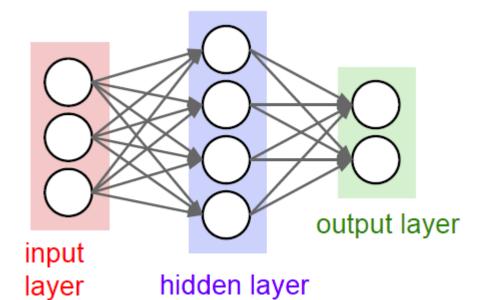
- E.g. 1000×1000 image100 filters10×10 filter size
- ⇒ only 10k parameters
- Result: Response map
 - > size: 1000×1000×100
 - Only memory, not params!

5

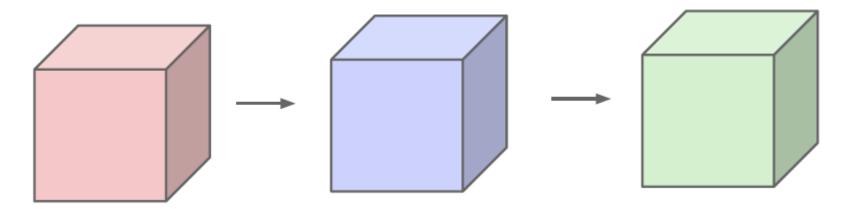


Important Conceptual Shift

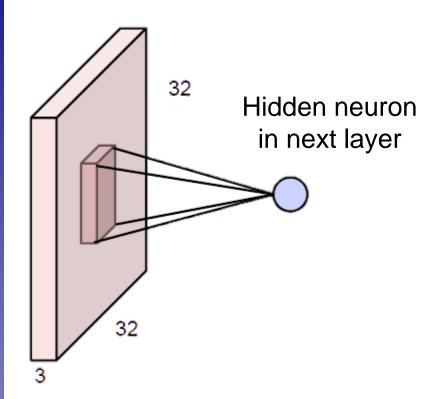
Before



Now:







Example

image: 32×32×3 volume

Before: Full connectivity

 $32 \times 32 \times 3$ weights

Now: Local connectivity

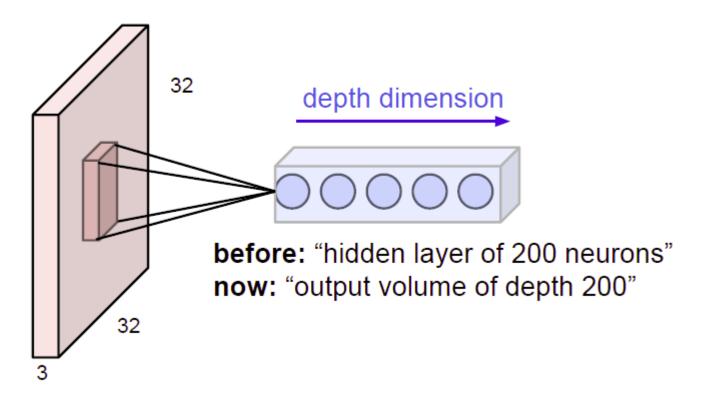
One neuron connects to, e.g.,

 $5 \times 5 \times 3$ region.

 \Rightarrow Only $5 \times 5 \times 3$ shared weights.

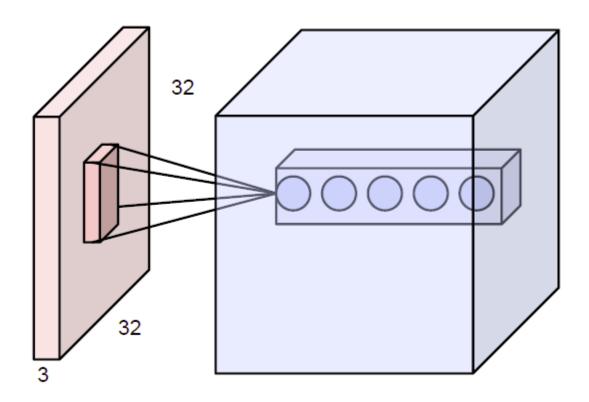
- Note: Connectivity is
 - > Local in space $(5 \times 5 \text{ inside } 32 \times 32)$
 - But full in depth (all 3 depth channels)



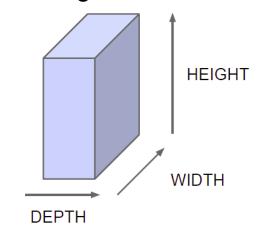


- All Neural Net activations arranged in 3 dimensions
 - Multiple neurons all looking at the same input region, stacked in depth



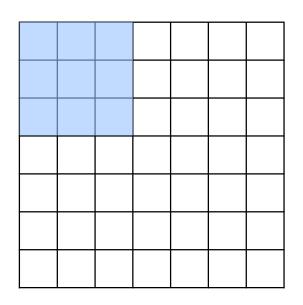


Naming convention:



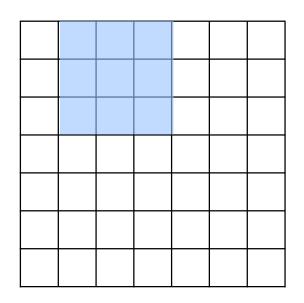
- All Neural Net activations arranged in 3 dimensions
 - Multiple neurons all looking at the same input region, stacked in depth
 - Form a single $[1 \times 1 \times depth]$ depth column in output volume.





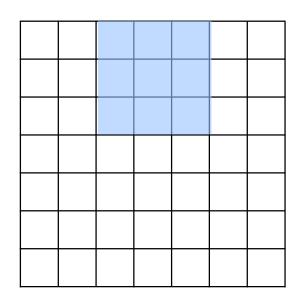
Example: 7×7 input assume 3×3 connectivity stride 1





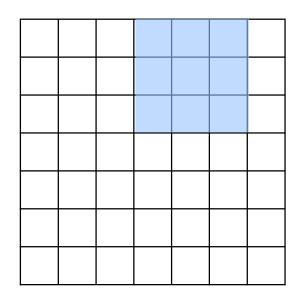
Example: 7×7 input assume 3×3 connectivity stride 1





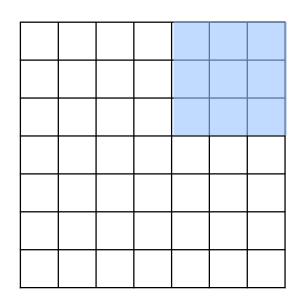
Example: 7×7 input assume 3×3 connectivity stride 1





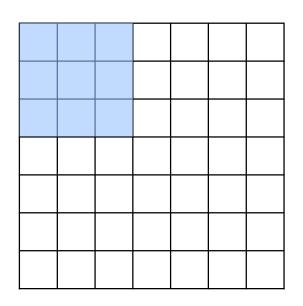
Example: 7×7 input assume 3×3 connectivity stride 1





Example: 7×7 input assume 3×3 connectivity stride 1 $\Rightarrow 5 \times 5$ output



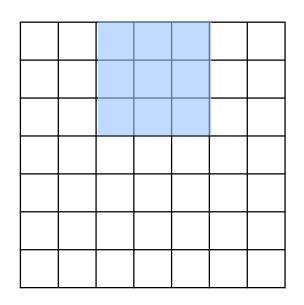


Example: 7×7 input assume 3×3 connectivity stride 1

 \Rightarrow 5×5 output

What about stride 2?





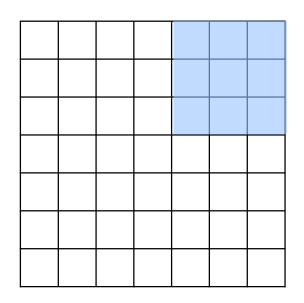
Example: 7×7 input

 7×7 input assume 3×3 connectivity stride 1

 \Rightarrow 5×5 output

What about stride 2?





Example:

 7×7 input assume 3×3 connectivity stride 1

 \Rightarrow 5×5 output

What about stride 2?

 \Rightarrow 3×3 output



0	0	0	0	0		
0						
0						
0						
0						

Example:

 7×7 input assume 3×3 connectivity stride 1

 \Rightarrow 5×5 output

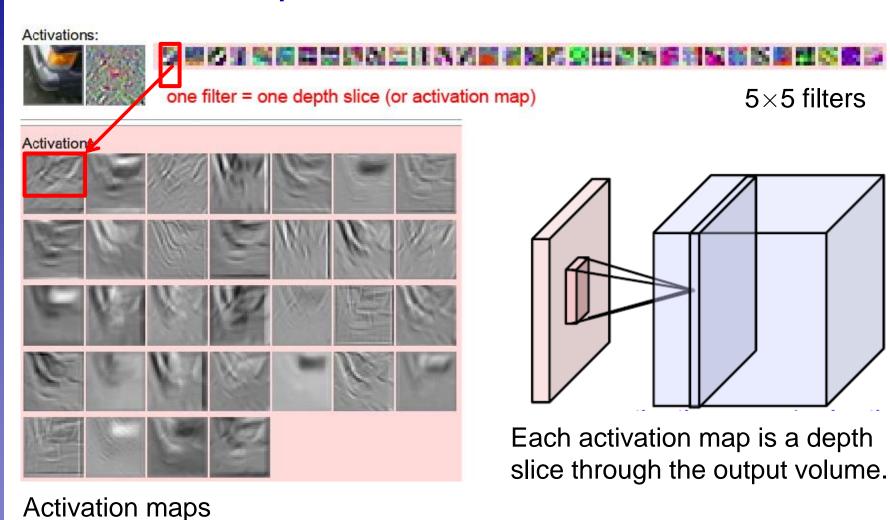
What about stride 2?

 \Rightarrow 3×3 output

- Replicate this column of hidden neurons across space, with some stride.
- In practice, common to zero-pad the border.
 - Preserves the size of the input spatially.

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Activation Maps of Convolutional Filters

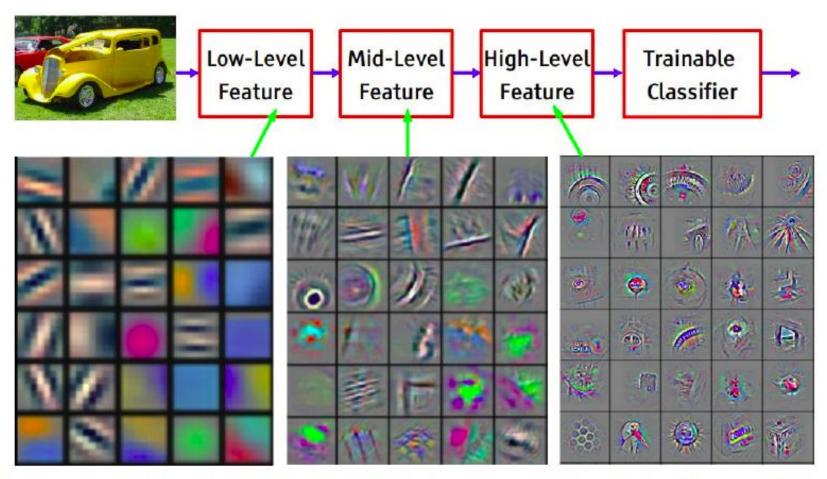


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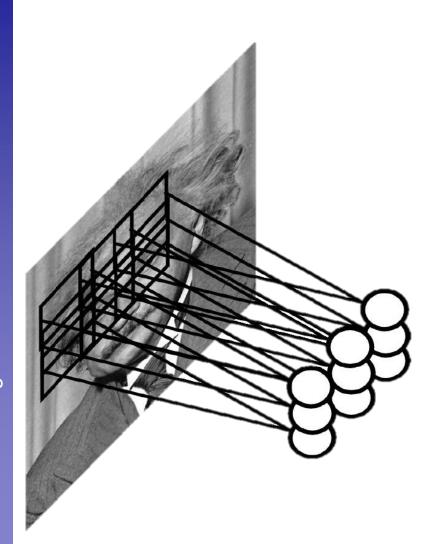
Effect of Multiple Convolution Layers



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]



Convolutional Networks: Intuition

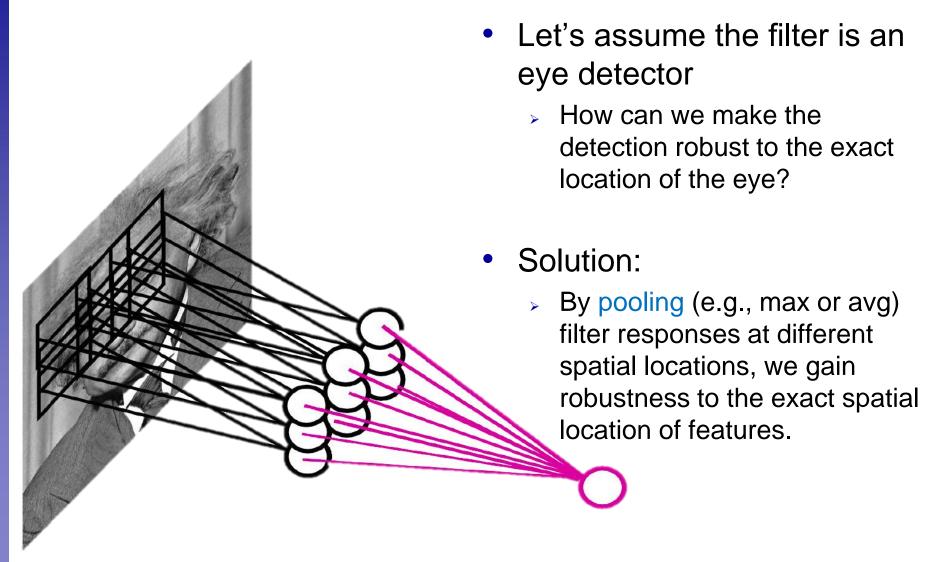


- Let's assume the filter is an eye detector
 - How can we make the detection robust to the exact location of the eye?

Image source: Yann LeCun



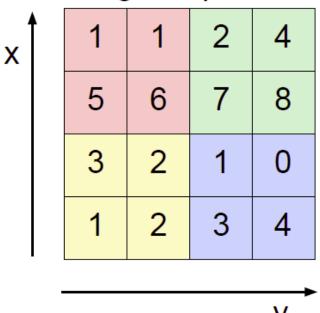
Convolutional Networks: Intuition





Max Pooling

Single depth slice



max pool with 2x2 filters and stride 2

6	8
3	4

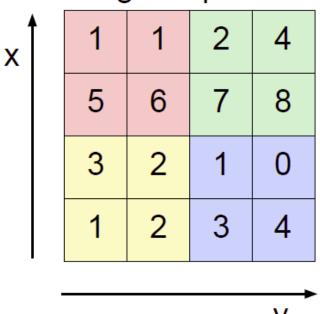
• Effect:

- Make the representation smaller without losing too much information
- Achieve robustness to translations



Max Pooling

Single depth slice



max pool with 2x2 filters and stride 2

6	8
3	4

Note

Pooling happens independently across each slice, preserving the number of slices.



CNNs: Implication for Back-Propagation

- Convolutional layers
 - Filter weights are shared between locations
 - ⇒ Gradients are added for each filter location.

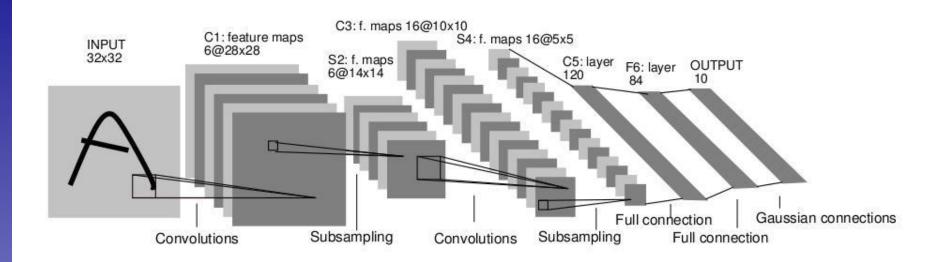


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CNN Architectures: LeNet (1998)



- Early convolutional architecture
 - 2 Convolutional layers, 2 pooling layers
 - Fully-connected NN layers for classification
 - Successfully used for handwritten digit recognition (MNIST)

Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, <u>Gradient-based learning applied to document recognition</u>, Proceedings of the IEEE 86(11): 2278–2324, 1998.



ImageNet Challenge 2012

ImageNet

- ~14M labeled internet images
- 20k classes
- Human labels via Amazon Mechanical Turk

Challenge (ILSVRC)

- 1.2 million training images
- 1000 classes
- Goal: Predict ground-truth class within top-5 responses



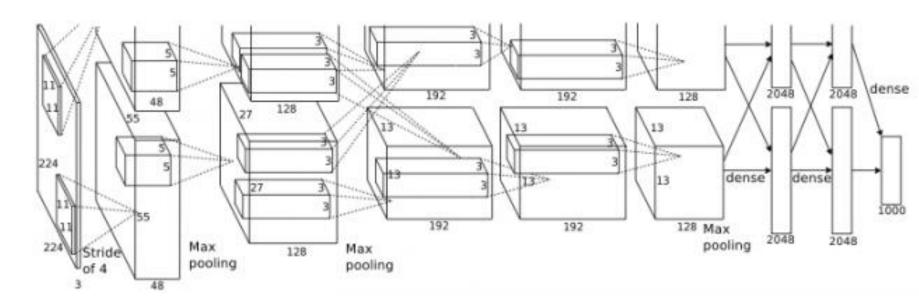




[Deng et al., CVPR'09]



CNN Architectures: AlexNet (2012)

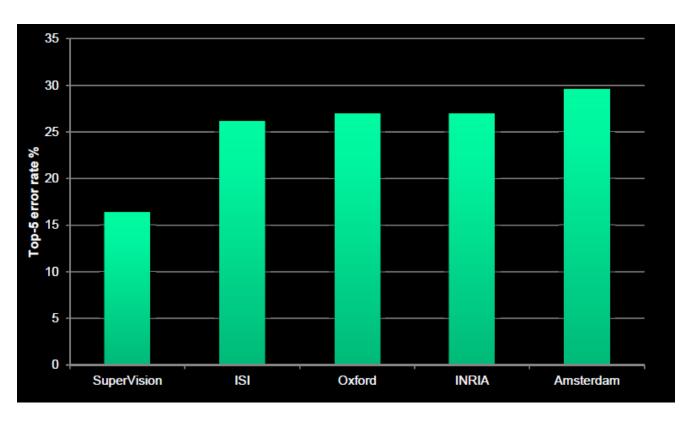


- Similar framework as LeNet, but
 - Bigger model (7 hidden layers, 650k units, 60M parameters)
 - More data (10⁶ images instead of 10³)
 - GPU implementation
 - Better regularization and up-to-date tricks for training (Dropout)

A. Krizhevsky, I. Sutskever, and G. Hinton, <u>ImageNet Classification with Deep Convolutional Neural Networks</u>, NIPS 2012.



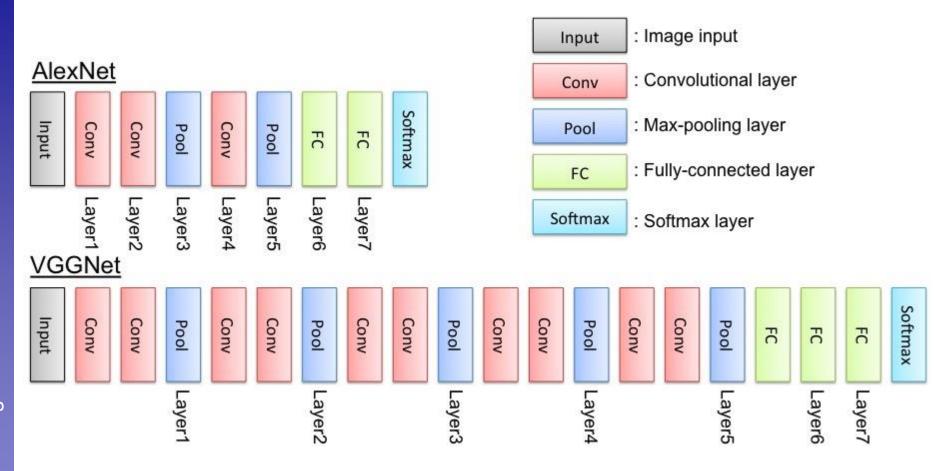
ILSVRC 2012 Results



- AlexNet almost halved the error rate
 - > 16.4% error (top-5) vs. 26.2% for the next best approach
 - ⇒ A revolution in Computer Vision
 - Acquired by Google in Jan '13, deployed in Google+ in May '13

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CNN Architectures: VGGNet (2014/15)



K. Simonyan, A. Zisserman, <u>Very Deep Convolutional Networks for Large-Scale Image Recognition</u>, ICLR 2015

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CNN Architectures: VGGNet (2014/15)

Main ideas

- Deeper network
- Stacked convolutional layers with smaller filters (+ nonlinearity)
- Detailed evaluation of all components

Results

Improved ILSVRC top-5 error rate to 6.7%.

ConvNet Configuration					
A	A-LRN	В	С	D	Е
11 weight	11 weight	13 weight	16 weight	16 weight	19 weight
layers	layers	layers	layers	layers	layers
	input $(224 \times 224 \text{ RGB imag})$				
conv3-64	conv3-64	conv3-64	conv3-64	conv3-64	conv3-64
	LRN	conv3-64	conv3-64	conv3-64	conv3-64
			pool		
conv3-128	conv3-128	conv3-128	conv3-128	conv3-128	conv3-128
		conv3-128	conv3-128	conv3-128	conv3-128
	•	max	pool		
conv3-256	conv3-256	conv3-256	conv3-256	conv3-256	conv3-256
conv3-256	conv3-256	conv3-256	conv3-256	conv3-256	conv3-256
			conv1-256	conv3-256	conv3-256
					conv3-256
		max	pool		
conv3-512	conv3-512	conv3-512	conv3-512	conv3-512	conv3-512
conv3-512	conv3-512	conv3-512	conv3-512	conv3-512	conv3-512
			conv1-512	conv3-512	conv3-512
					conv3-512
		max	pool		
conv3-512	conv3-512	conv3-512	conv3-512	conv3-512	conv3-512
conv3-512	conv3-512	conv3-512	conv3-512	conv3-512	conv3-512
			conv1-512	conv3-512	conv3-512
					conv3-512
maxpool				, used	
FC-4096			iviaini	/ used	
FC-4096					
FC-1000					
soft-max					



Comparison: AlexNet vs. VGGNet

Receptive fields in the first layer

AlexNet: 11×11, stride 4

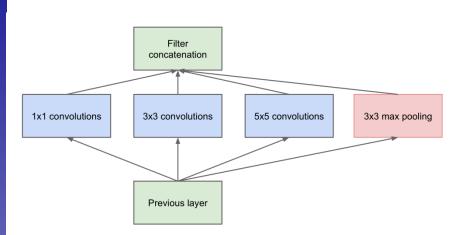
Zeiler & Fergus: 7×7, stride 2

VGGNet: 3×3, stride 1

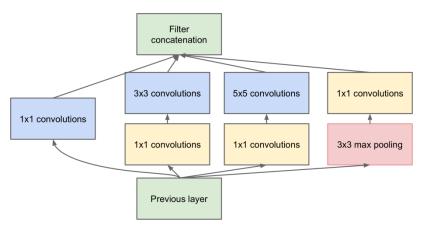
Why that?

- If you stack a 3×3 on top of another 3×3 layer, you effectively get a 5×5 receptive field.
- \rightarrow With three 3×3 layers, the receptive field is already 7×7.
- > But much fewer parameters: $3.3^2 = 27$ instead of $7^2 = 49$.
- In addition, non-linearities in-between 3×3 layers for additional discriminativity.

CNN Architectures: GoogLeNet (2014/2015)



(a) Inception module, naïve version



(b) Inception module with dimension reductions

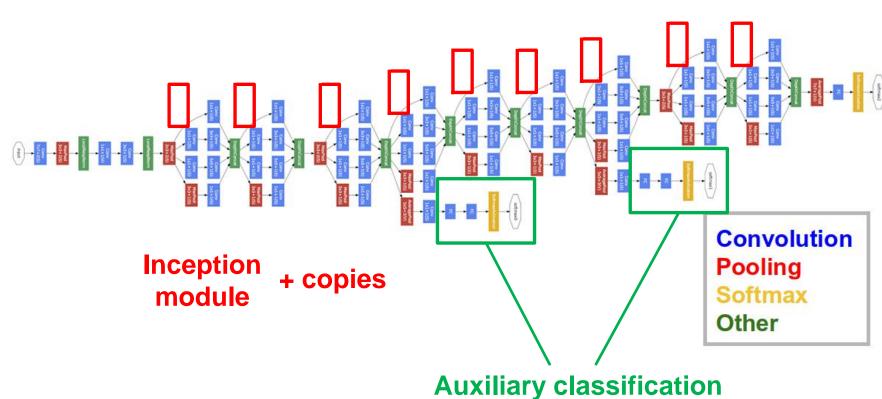
Main ideas

- "Inception" module as modular component
- Learns filters at several scales within each module

C. Szegedy, W. Liu, Y. Jia, et al, <u>Going Deeper with Convolutions</u>, arXiv:1409.4842, 2014, CVPR'15, 2015.



GoogLeNet Visualization



Auxiliary classification outputs for training the lower layers (deprecated)



Results on ILSVRC

Method	ton 1 val arror (%)	top-5 val. error (%)	ton 5 tost error (%)
	top-1 val. error (70)	top-3 val. error (%)	top-3 test error (%)
VGG (2 nets, multi-crop & dense eval.)	23.7	6.8	6.8
VGG (1 net, multi-crop & dense eval.)	24.4	7.1	7.0
VGG (ILSVRC submission, 7 nets, dense eval.)	24.7	7.5	7.3
GoogLeNet (Szegedy et al., 2014) (1 net)	_	7.	.9
GoogLeNet (Szegedy et al., 2014) (7 nets)	-	6.	.7
MSRA (He et al., 2014) (11 nets)	-	-	8.1
MSRA (He et al., 2014) (1 net)	27.9	9.1	9.1
Clarifai (Russakovsky et al., 2014) (multiple nets)	-	-	11.7
Clarifai (Russakovsky et al., 2014) (1 net)	_	-	12.5
Zeiler & Fergus (Zeiler & Fergus, 2013) (6 nets)	36.0	14.7	14.8
Zeiler & Fergus (Zeiler & Fergus, 2013) (1 net)	37.5	16.0	16.1
OverFeat (Sermanet et al., 2014) (7 nets)	34.0	13.2	13.6
OverFeat (Sermanet et al., 2014) (1 net)	35.7	14.2	-
Krizhevsky et al. (Krizhevsky et al., 2012) (5 nets)	38.1	16.4	16.4
Krizhevsky et al. (Krizhevsky et al., 2012) (1 net)	40.7	18.2	-

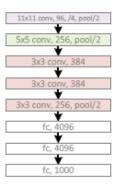
- VGGNet and GoogLeNet perform at similar level
 - Comparison: human performance ~5% [Karpathy]

http://karpathy.github.io/2014/09/02/what-i-learned-from-competing-against-a-convnet-on-imagenet/

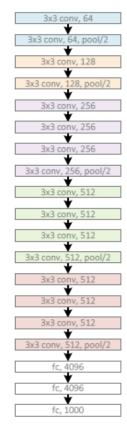
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Newer Developments: Residual Networks

AlexNet, 8 layers (ILSVRC 2012)



VGG, 19 layers (ILSVRC 2014)



GoogleNet, 22 layers (ILSVRC 2014)



Newer Developments: Residual Networks

AlexNet, 8 layers (ILSVRC 2012)



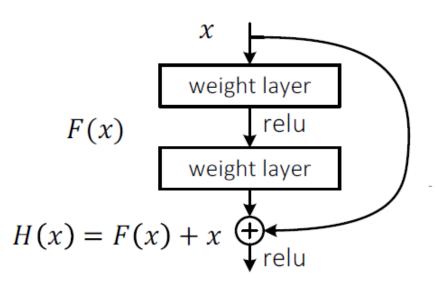
VGG, 19 layers (ILSVRC 2014)

B. Leibe



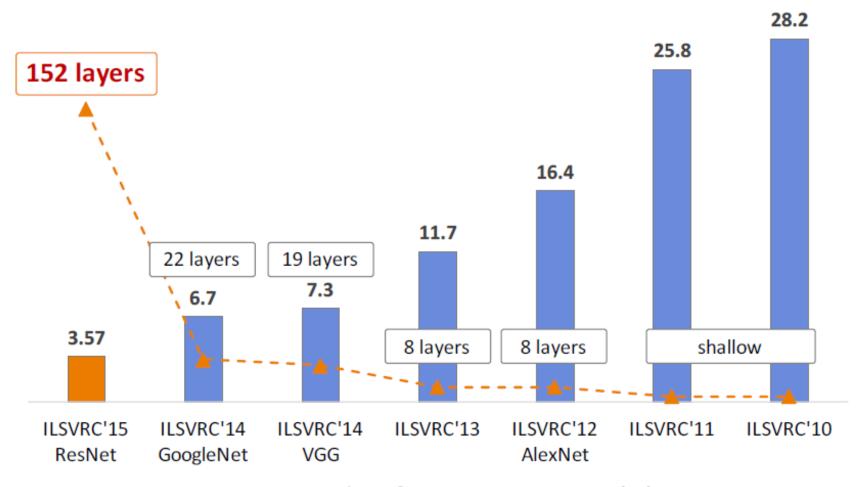
ResNet, 152 layers (ILSVRC 2015)

- Core component
 - Skip connections bypassing each layer
 - Better propagation of gradients to the deeper layers
 - We'll analyze this mechanism in more detail later...





ImageNet Performance



ImageNet Classification top-5 error (%)

Understanding the ILSVRC Challenge

- Imagine the scope of the problem!
 - 1000 categories
 - 1.2M training images
 - 50k validation images
- This means...
 - Speaking out the list of category names at 1 word/s...
 - ...takes 15mins.
 - Watching a slideshow of the validation images at 2s/image... ...takes a full day (24h+).
 - Watching a slideshow of the training images at 2s/image... ...takes a full month.



rier, Airedaie, airimer, airsnip, aidatross, aingator fizard, aip, aitar, ambulance, American alligator, American black bear, American chameleon, American coot, American egret, American lobster, American Staffordshire terrier, amphibian, analog clock, anemone fish, Angora, ant, apiary, Appenzeller, apron, Arabian camel, Arctic fox, armadillo, artichoke, ashcan, assault rifle, Australian terrier, axolotl, baboon, backpack, badger, bagel, bakery, balance beam, bald eagle, balloon, ballplayer, ballpoint, banana, Band Aid, banded gecko, banjo, bannister, barbell, barber chair, barbershop, barn, barn spider, barometer, barracouta, barrel, barrow, baseball, basenji, basketball, basset, bassinet, bassoon, bath towel, bathing cap, bathtub, beach wagon, beacon, beagle, beaker, bearskin, beaver, Bedlington terrier, bee, bee eater, beer bottle, beer glass, bell cote, bell pepper, Bernese mountain dog, bib, bicycle-built-for-two, bighorn, bikini, binder, binoculars, birdhouse, bison, bittern, black and gold garden spider, black grouse, black stork, black swan, black widow, black-and-tan coonhound, black-footed ferret, Blenheim spaniel, bloodhound, bluetick, boa constrictor, boathouse, bobsled, bolete, bolo tie, bonnet, book jacket, bookcase, bookshop, Border collie, Border terrier, borzoi, Boston bull, bottlecap, Bouvier des Flandres, bow, bow tie, box turtle, boxer, Brabancon griffon, brain coral, brambling, brass, brassiere, breakwater, breastplate, briard, Brittany spaniel, broccoli, broom, brown bear, bubble, bucket, buckeye, buckle, bulbul, bull mastiff, bullet train, bulletproof vest, bullfrog, burrito, bustard, butcher shop, butternut squash, cab, cabbage butterfly, cairn, caldron, can opener, candle, cannon, canoe, capuchin, car mirror, car wheel, carbonara, Cardigan, cardigan, cardoon, carousel, carpenter's kit, carton, cash machine, cassette, cassette player, castle, catamaran, cauliflower, CD player, cello, cellular telephone, centipede, chain, chain mail, chain saw, chainlink fence, chambered nautilus, cheeseburger, cheetah, Chesapeake Bay retriever, chest, chickadee, chiffonier, Chihuahua, chime, chimpanzee, china cabinet, chiton, chocolate sauce, chow, Christmas stocking, church, cicada, cinema, cleaver, cliff, cliff dwelling, cloak, clog, clumber, cock, cocker spaniel, cockroach, cocktail shaker, coffee mug, coffeepot, coho, coil, collie, colobus, combination lock, comic book, common iguana, common newt, computer keyboard, conch, confectionery, consomme, container ship, convertible, coral fungus, coral reef, corkscrew, corn, cornet, coucal, cougar, cowboy boot, cowboy hat, coyote, cradle, crane, crane, crash helmet, crate, crayfish, crib, cricket, Crock Pot, croquet ball, crossword puzzle, crutch, cucumber, cuirass, cup, curly-coated retriever, custard apple, daisy, dalmatian, dam, damselfly, Dandie Dinmont, desk, desktop computer, dhole, dial telephone, diamondback, diaper, digital clock, digital watch, dingo, dining table, dishrag, dishwasher, disk brake, Doberman, dock, dogsled, dome, doormat, dough, dowitcher, dragonfly, drake, drilling platform, drum, drumstick, dugong, dumbbell, dung beetle, Dungeness crab, Dutch oven, ear, earthstar, echidna, eel, eft, eggnog, Egyptian cat, electric fan, electric guitar, electric locomotive, electric ray, English foxhound, English setter, English springer, entertainment center, EntleBucher, envelope, Eskimo dog, espresso, espresso maker, European fire salamander, European gallinule, face powder, feather boa, fiddler crab, fig, file, fire engine, fire screen, fireboat, flagpole, flamingo, flatcoated retriever, flatworm, flute, fly, folding chair, football helmet, forklift, fountain, fountain pen, four-poster, fox squirrel, freight car, French bulldog, French horn, French loaf, frilled lizard, frying pan, fur coat, gar, garbage truck, garden spider, garter snake, gas pump, gasmask, gazelle, German shepherd, German short-haired pointer, geyser, giant panda, giant schnauzer, gibbon, Gila monster, go-kart, goblet, golden retriever, goldfinch, goldfish, golf ball, golfcart, gondola, gong, goose, Gordon setter, gorilla, gown, grand piano, Granny Smith, grasshopper. Great Dane, great grev owl. Great Pvrenees, great white shark.





More Finegrained Classes





Quirks and Limitations of the Data Set



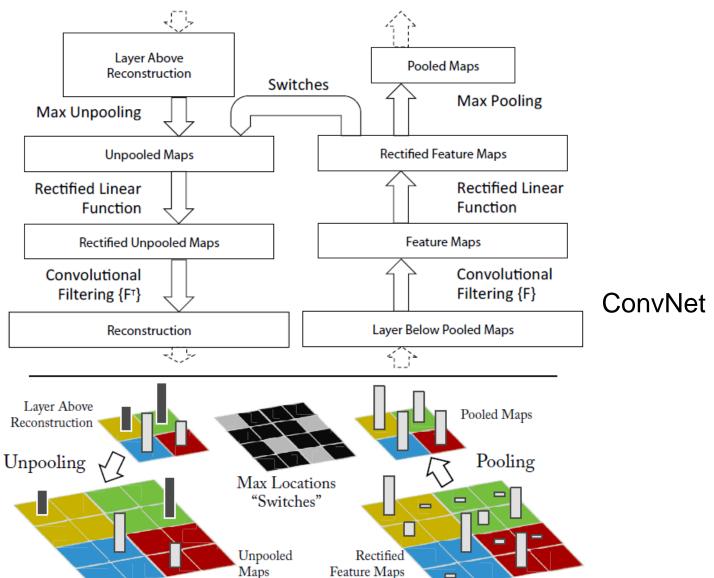
- Generated from WordNet ontology
 - Some animal categories are overrepresented
 - E.g., 120 subcategories of dog breeds
- ⇒ 6.7% top-5 error looks all the more impressive



Topics of This Lecture

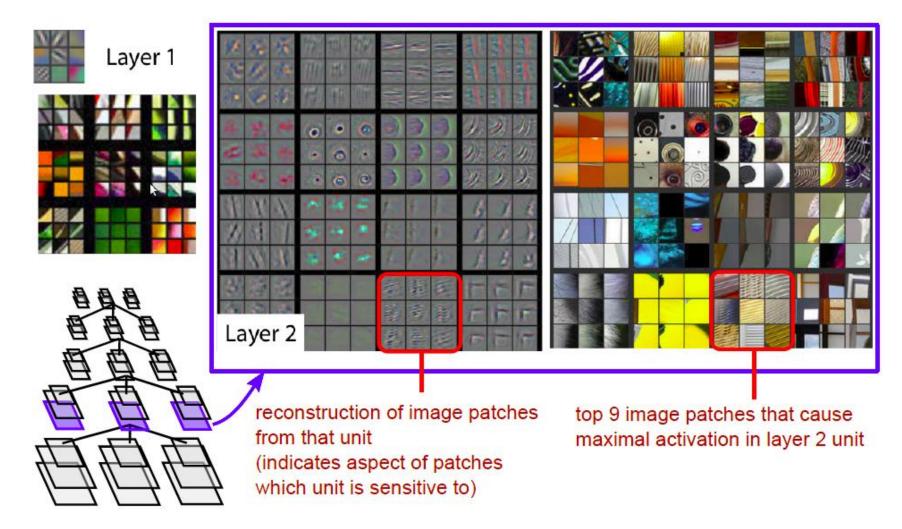
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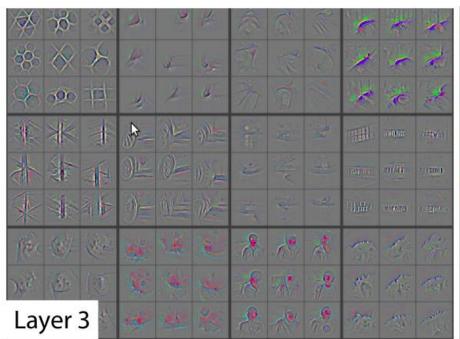
DeconvNet





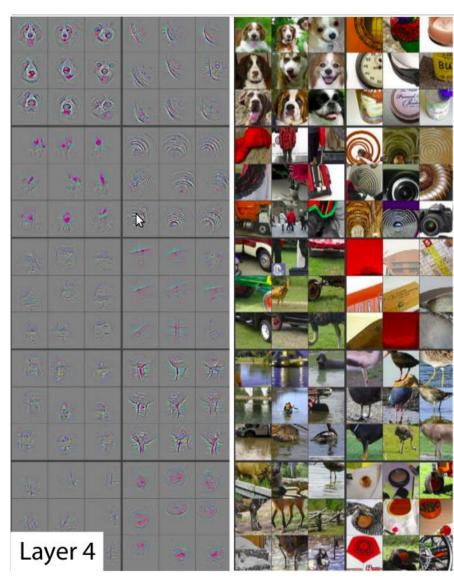
M. Zeiler, R. Fergus, <u>Visualizing and Understanding Convolutional Neural Networks</u>, ECCV 2014.

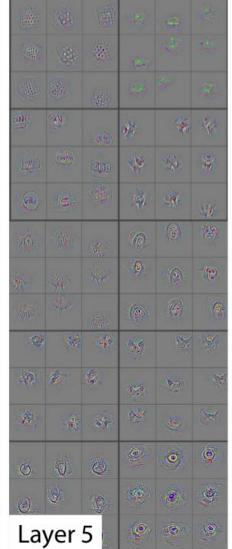
















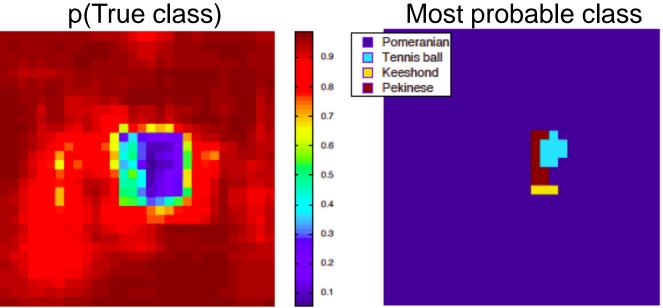
- Occlusion Experiment
 - Mask part of the image with an occluding square.
 - Monitor the output





Input image



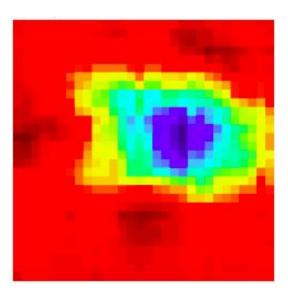


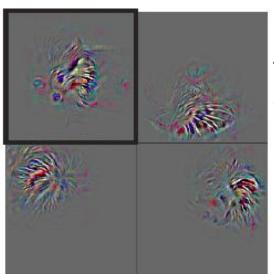


Input image



Total activation in most active 5th layer feature map

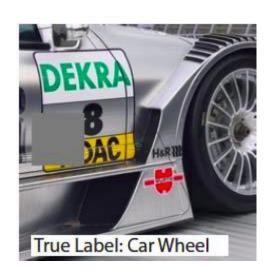


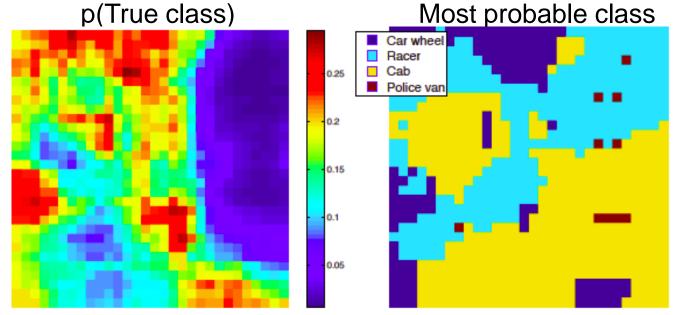


Other activations from the same feature map.



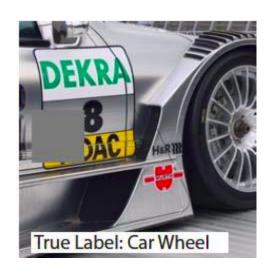
Input image



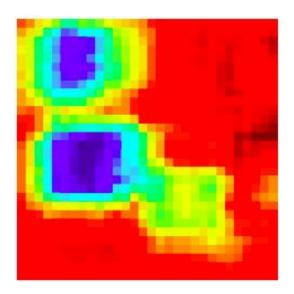








Total activation in most active 5th layer feature map



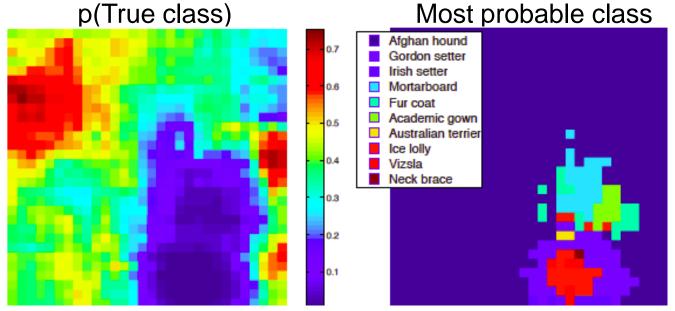


Other activations from the same feature map.



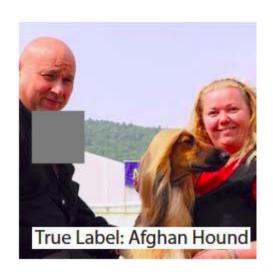
Input image



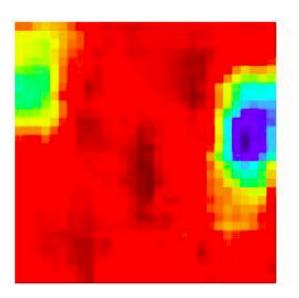


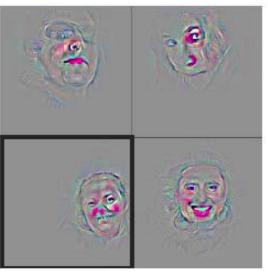


Input image



Total activation in most active 5th layer feature map

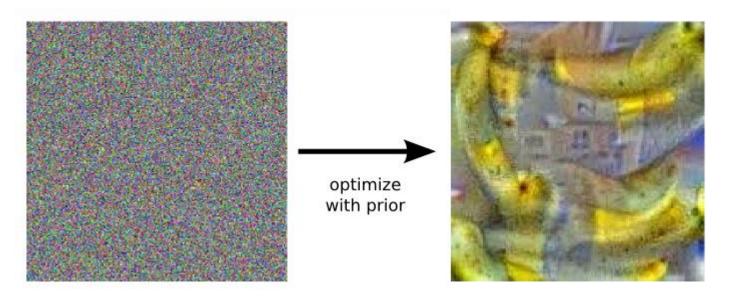




Other activations from the same feature map.



Inceptionism: Dreaming ConvNets



Idea

- Start with a random noise image.
- Enhance the input image such as to enforce a particular response (e.g., banana).
- Combine with prior constraint that image should have similar statistics as natural images.
- ⇒ Network hallucinates characteristics of the learned class.



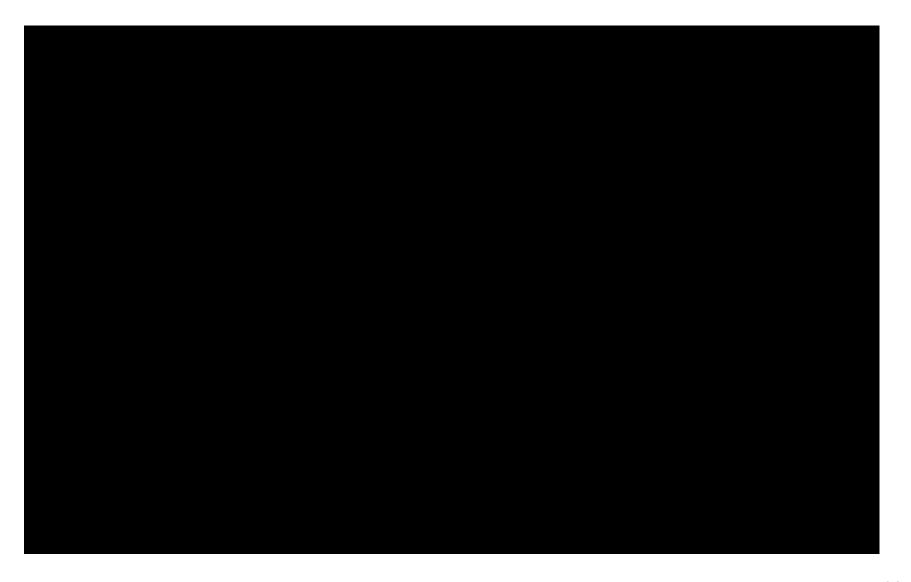
Inceptionism: Dreaming ConvNets

Results





Inceptionism: Dreaming ConvNets



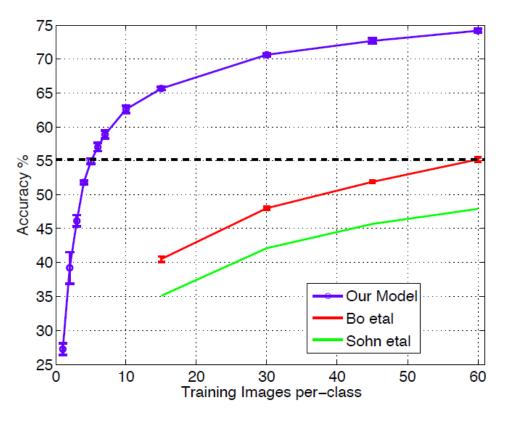


Topics of This Lecture

- Recap: CNNs
- CNN Architectures
 - LeNet
 - AlexNet
 - VGGNet
 - GoogLeNet
- Visualizing CNNs
 - Visualizing CNN features
 - Visualizing responses
 - Visualizing learned structures
- Applications



The Learned Features are Generic



state of the art level (pre-CNN)

- Experiment: feature transfer
 - Train network on ImageNet
 - Chop off last layer and train classification layer on CalTech256
 - ⇒ State of the art accuracy already with only 6 training images



Other Tasks: Detection

R-CNN: Regions with CNN features

warped region



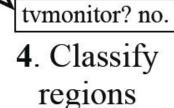
1. Input image



2. Extract region proposals (~2k)



3. Compute CNN features



person? yes.

aeroplane? no.

- Results on PASCAL VOC Detection benchmark
 - > Pre-CNN state of the art: 35.1% mAP [Uijlings et al., 2013]

33.4% mAP DPM

> R-CNN: 53.7% mAP

R. Girshick, J. Donahue, T. Darrell, and J. Malik, <u>Rich Feature Hierarchies for Accurate Object Detection and Semantic Segmentation</u>, CVPR 2014



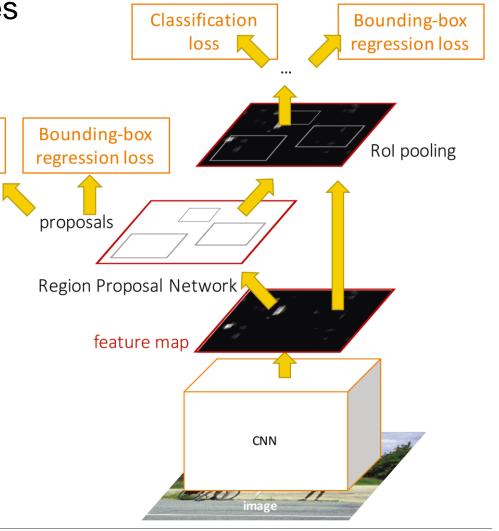
Most Recent Version: Faster R-CNN

loss

- One network, four losses
 - Remove dependence on external region proposal algorithm.
 Classification

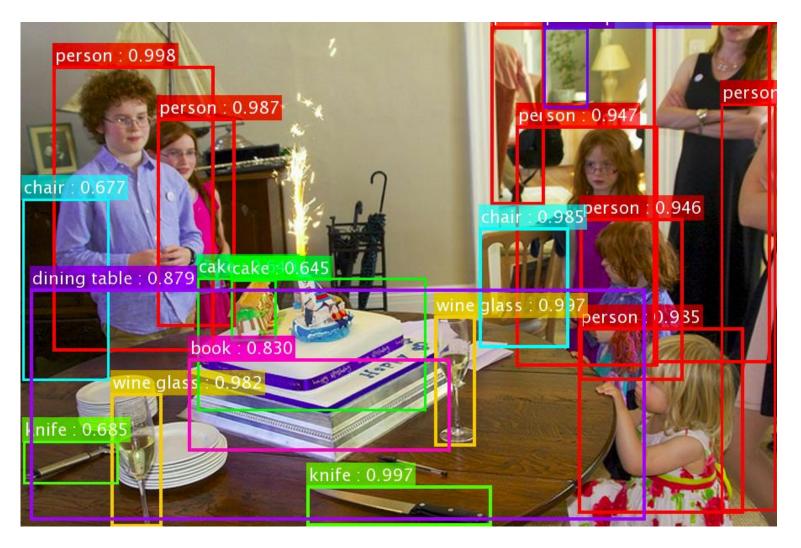
 Instead, infer region proposals from same CNN.

- Feature sharing
- Joint training
- ⇒ Object detection in a single pass becomes possible.
- \Rightarrow mAP improved to >70%





Faster R-CNN (based on ResNets)

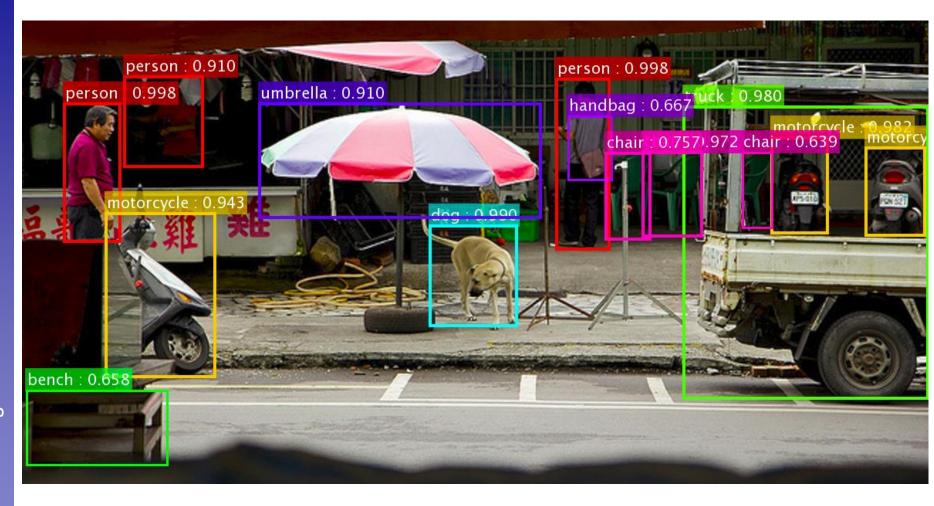


K. He, X. Zhang, S. Ren, J. Sun, <u>Deep Residual Learning for Image Recognition</u>, CVPR 2016.

B. Leibe



Faster R-CNN (based on ResNets)



K. He, X. Zhang, S. Ren, J. Sun, <u>Deep Residual Learning for Image Recognition</u>, CVPR 2016.

B. Leibe

RWTHAACHEN UNIVERSITY

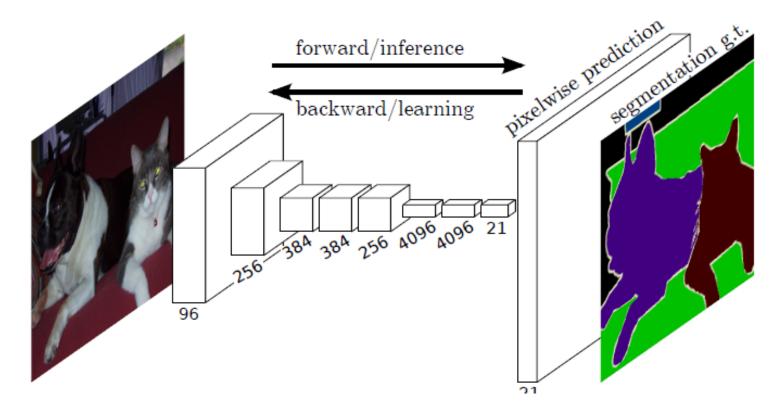
YOLO



J. Redmon, S. Divvala, R. Girshick, A. Farhadi, <u>You Only Look Once: Unified</u>, <u>Real-Time Object Detection</u>, CVPR 2016.



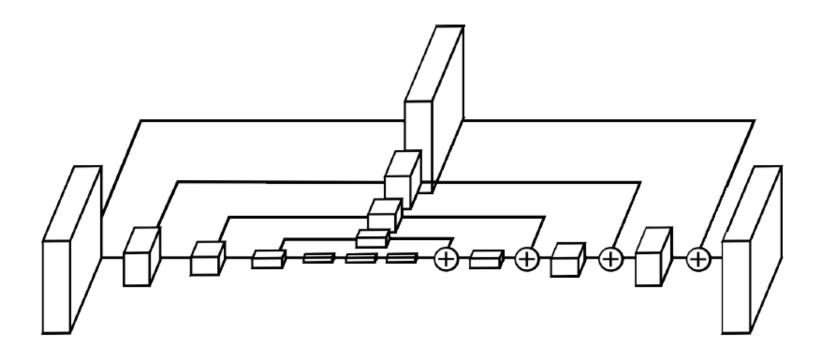
Semantic Image Segmentation



- Perform pixel-wise prediction task
 - Usually done using Fully Convolutional Networks (FCNs)
 - All operations formulated as convolutions
 - Advantage: can process arbitrarily sized images



Semantic Image Segmentation



- Encoder-Decoder Architecture
 - Problem: FCN output has low resolution
 - Solution: perform upsampling to get back to desired resolution
 - Use skip connections to preserve higher-resolution information



Semantic Segmentation

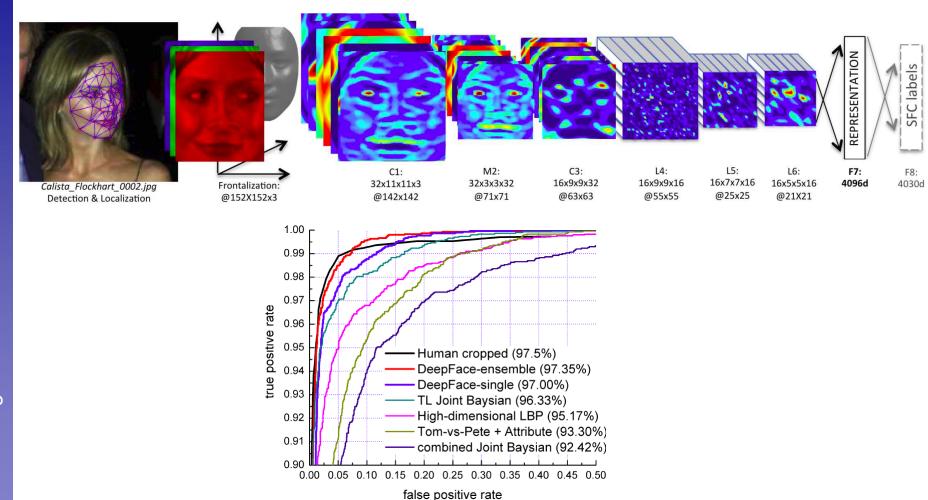


[Pohlen, Hermans, Mathias, Leibe, CVPR 2017]

- More recent results
 - Based on an extension of ResNets



Other Tasks: Face Verification



Y. Taigman, M. Yang, M. Ranzato, L. Wolf, <u>DeepFace: Closing the Gap to Human-Level Performance in Face Verification</u>, CVPR 2014

Slide credit: Svetlana Lazebnik



Commercial Recognition Services

• E.g., clarifai

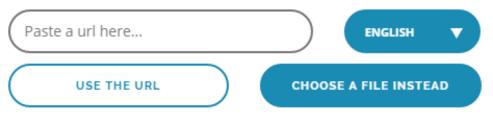






Try it out with your own media

Upload an image or video file under 100mb or give us a direct link to a file on the web.

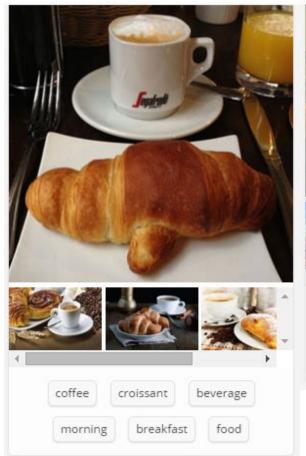


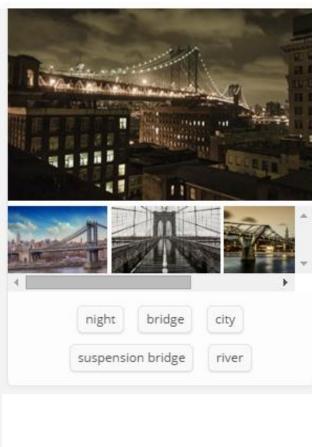
*By using the demo you agree to our terms of service

- Be careful when taking test images from Google Search
 - Chances are they may have been seen in the training set...



Commercial Recognition Services











References and Further Reading

LeNet

Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner, <u>Gradient-based</u> <u>learning applied to document recognition</u>, Proceedings of the IEEE 86(11): 2278–2324, 1998.

AlexNet

A. Krizhevsky, I. Sutskever, and G. Hinton, <u>ImageNet Classification</u> with <u>Deep Convolutional Neural Networks</u>, NIPS 2012.

VGGNet

K. Simonyan, A. Zisserman, <u>Very Deep Convolutional Networks for Large-Scale Image Recognition</u>, ICLR 2015

GoogLeNet

C. Szegedy, W. Liu, Y. Jia, et al, <u>Going Deeper with Convolutions</u>, arXiv:1409.4842, 2014.



References and Further Reading

ResNet

K. He, X. Zhang, S. Ren, J. Sun, <u>Deep Residual Learning for Image</u> <u>Recognition</u>, CVPR 2016.



References

ReLu

X. Glorot, A. Bordes, Y. Bengio, <u>Deep sparse rectifier neural</u> <u>networks</u>, AISTATS 2011.

Initialization

- X. Glorot, Y. Bengio, <u>Understanding the difficulty of training deep</u> <u>feedforward neural networks</u>, AISTATS 2010.
- K. He, X.Y. Zhang, S.Q. Ren, J. Sun, <u>Delving Deep into Rectifiers:</u> <u>Surpassing Human-Level Performance on ImageNet Classification</u>, ArXiV 1502.01852v1, 2015.
- A.M. Saxe, J.L. McClelland, S. Ganguli, <u>Exact solutions to the</u> <u>nonlinear dynamics of learning in deep linear neural networks</u>, ArXiV 1312.6120v3, 2014.



References and Further Reading

Batch Normalization

S. Ioffe, C. Szegedy, <u>Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift</u>, ArXiV 1502.03167, 2015.

Dropout

N. Srivastava, G. Hinton, A. Krizhevsky, I. Sutskever, R. Salakhutdinov, <u>Dropout: A Simple Way to Prevent Neural Networks from Overfitting</u>, JMLR, Vol. 15:1929-1958, 2014.