

Computer Vision 2 WS 2018/19

Part 4 – Template-based Tracking II 23.10.2018


Prof. Dr. Bastian Leibe

RWTH Aachen University, Computer Vision Group
<http://www.vision.rwth-aachen.de>



Course Outline

- Single-Object Tracking
 - Background modeling
 - Template based tracking
 - Tracking by online classification
 - Tracking-by-detection
- Bayesian Filtering
- Multi-Object Tracking
- Visual Odometry
- Visual SLAM & 3D Reconstruction
- Deep Learning for Video Analysis



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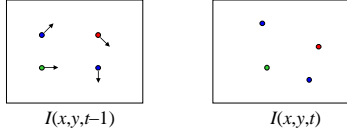
Topics of This Lecture

- Recap: Lucas-Kanade Optical Flow
 - Brightness Constancy constraint
 - LK flow estimation
 - Coarse-to-fine estimation
 - KLT feature tracking
- Template Tracking
 - LK derivation for templates
 - Warping functions
 - General LK image registration
- Applications

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Recap: Estimating Optical Flow



- Optical Flow
 - Given two subsequent frames, estimate the apparent motion field $u(x,y)$ and $v(x,y)$ between them.
- Key assumptions
 - **Brightness constancy**: projection of the same point looks the same in every frame.
 - **Small motion**: points do not move very far.
 - **Spatial coherence**: points move like their neighbors.

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Recap: Lucas-Kanade Optical Flow

- Use all pixels in a $K \times K$ window to get more equations.
- Least squares problem:

$$\begin{bmatrix} I_x(p_1) & I_y(p_1) \\ I_x(p_2) & I_y(p_2) \\ \vdots & \vdots \\ I_x(p_{25}) & I_y(p_{25}) \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = - \begin{bmatrix} I_t(p_1) \\ I_t(p_2) \\ \vdots \\ I_t(p_{25}) \end{bmatrix} \quad A \quad d = b$$

25×2 2×1 25×1
- Minimum least squares solution given by solution of

$$(A^T A) d = A^T b$$


2×2 2×1 2×1

Recall the Harris detector!

$$\begin{bmatrix} \sum I_x I_x & \sum I_x I_y \\ \sum I_x I_y & \sum I_y I_y \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = - \begin{bmatrix} \sum I_x I_t \\ \sum I_y I_t \end{bmatrix}$$

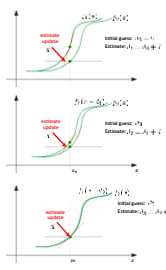
$A^T A$ $A^T b$

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Recap: Iterative LK Refinement

- Estimate velocity at each pixel using one iteration of LK estimation.
- Warp one image toward the other using the estimated flow field.
- Refine estimate by repeating the process.
- Iterative procedure
 - Results in subpixel accurate localization.
 - Converges for small displacements.



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Slide adapted from Steve Seitz



Recap: Coarse-to-fine Optical Flow Estimation

$u=1.25$ pixels
 $u=2.5$ pixels
 $u=5$ pixels
 $u=10$ pixels

Gaussian pyramid of image 1 Gaussian pyramid of image 2

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Recap: Coarse-to-fine Optical Flow Estimation

Run iterative LK
 Warp & upsample
 Run iterative LK

Gaussian pyramid of image 1 Gaussian pyramid of image 2

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Recap: Shi-Tomasi Feature Tracker (→KLT)

- Idea
 - Find good features using eigenvalues of second-moment matrix
 - Key idea: "good" features to track are the ones that can be tracked reliably.
- Frame-to-frame tracking
 - Track with LK and a pure *translation* motion model.
 - More robust for small displacements, can be estimated from smaller neighborhoods (e.g., 5×5 pixels).
- Checking consistency of tracks
 - Affine registration to the first observed feature instance.
 - Affine model is more accurate for larger displacements.
 - Comparing to the first frame helps to minimize drift.

J. Shi and C. Tomasi. [Good Features to Track](#). CVPR 1994.

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Lucas-Kanade Template Tracking

80x50 pixels

- Traditional LK
 - Typically run on small, corner-like features (e.g., 5×5 patches) to compute optical flow (→ KLT).
 - However, there is no reason why we can't use the same approach on a larger window around the tracked object.

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Basic LK Derivation for Templates

$$E(u, v) = \sum_x [I(x + u, y + v) - T(x, y)]^2$$

Template model

Current frame

(u, v) = hypothesized location of template in current frame

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Basic LK Derivation for Templates

- Taylor expansion

$$E(u, v) = \sum_{\mathbf{x}} [I(x+u, y+v) - T(x, y)]^2$$

$$\approx \sum_{\mathbf{x}} [I(x, y) + uI_x(x, y) + vI_y(x, y) - T(x, y)]^2$$

$$= \sum_{\mathbf{x}} [uI_x(x, y) + vI_y(x, y) + D(x, y)]^2 \quad \text{with } D = I - T$$
- Taking partial derivatives

$$\frac{\partial E}{\partial u} = 2 \sum_{\mathbf{x}} [uI_x(x, y) + vI_y(x, y) + D(x, y)] I_x(x, y) \stackrel{!}{=} 0$$


$$\frac{\partial E}{\partial v} = 2 \sum_{\mathbf{x}} [uI_x(x, y) + vI_y(x, y) + D(x, y)] I_y(x, y) \stackrel{!}{=} 0$$
- Equation in matrix form

$$\sum_{\mathbf{x}} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} = \sum_{\mathbf{x}} \begin{bmatrix} I_x D \\ I_y D \end{bmatrix} \Rightarrow \text{Solve via least-squares}$$

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One Problem With This...

- Problematic Assumption
 - Assumption of constant flow (pure translation) for all pixels in a larger window is unreasonable for long periods of time.



- However...
 - We can easily generalize the LK approach to other 2D parametric motion models (like affine or projective) by introducing a "warp" function \mathbf{W} with parameters \mathbf{p} .

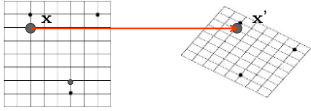
$$E(u, v) = \sum_{\mathbf{x}} [I(x+u, y+v) - T(x, y)]^2$$

$$E(\mathbf{p}) = \sum_{\mathbf{x}} [I(\mathbf{W}([x, y]; \mathbf{p})) - T([x, y])]^2$$

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Geometric Image Warping

- The warp $\mathbf{W}(\mathbf{x}; \mathbf{p})$ describes the geometric relationship between two images



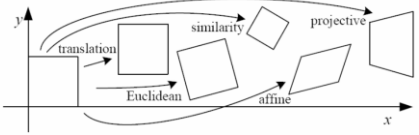
Input Image Transformed Image

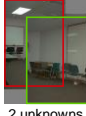

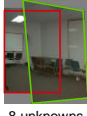

$$\mathbf{x}' = \mathbf{W}(\mathbf{x}; \mathbf{p}) = \begin{bmatrix} W_x(\mathbf{x}; \mathbf{p}) \\ W_y(\mathbf{x}; \mathbf{p}) \end{bmatrix}$$

Parameters of the warp

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Example Warping Functions



Translation	Affine	Perspective	3D rotation
			
2 unknowns	6 unknowns	8 unknowns	3 unknowns

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Example Warping Functions

- Translation

$$\mathbf{W}([x, y]; \mathbf{p}) = \begin{bmatrix} x + p_1 \\ y + p_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & p_1 \\ 0 & 1 & p_2 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
- Affine

$$\mathbf{W}([x, y]; \mathbf{p}) = \begin{bmatrix} x + p_1x + p_3y + p_5 \\ y + p_2x + p_4y + p_6 \end{bmatrix} = \begin{bmatrix} 1 + p_1 & p_3 & p_5 \\ p_2 & 1 + p_4 & p_6 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
- Perspective

$$\mathbf{W}([x, y]; \mathbf{p}) = \frac{1}{p_7x + p_8y + 1} \begin{bmatrix} x + p_1x + p_3y + p_5 \\ y + p_2x + p_4y + p_6 \end{bmatrix}$$

- Note: Other parametrizations are possible; the above ones are just particularly convenient here.

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General LK Image Registration

- Goal
 - Find the warping parameters \mathbf{p} that minimize the sum-of-squares intensity difference between the template image and the warped input image.
- LK formulation
 - Formulate this as an optimization problem

$$\arg \min_{\mathbf{p}} \sum_{\mathbf{x}} [I(\mathbf{W}(\mathbf{x}; \mathbf{p})) - T(\mathbf{x})]^2$$
 - We assume that an initial estimate of \mathbf{p} is known and iteratively solve for increments to the parameters $\Delta \mathbf{p}$:

$$\arg \min_{\Delta \mathbf{p}} \sum_{\mathbf{x}} [I(\mathbf{W}(\mathbf{x}; \mathbf{p} + \Delta \mathbf{p})) - T(\mathbf{x})]^2$$

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Step-by-Step Derivation

- Key to the derivation
 - Taylor expansion around $\Delta \mathbf{p}$

$$I(\mathbf{W}(\mathbf{x}; \mathbf{p} + \Delta \mathbf{p})) \approx I(\mathbf{W}(\mathbf{x}; \mathbf{p})) + \nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \Delta \mathbf{p} + \mathcal{O}(\Delta \mathbf{p}^2)$$
 - Using pixel coordinates $\mathbf{x} = [x, y]$

$$I(\mathbf{W}([x, y]; \mathbf{p} + \Delta \mathbf{p})) \approx I(\mathbf{W}([x, y]; p_1, \dots, p_n))$$

$$+ \begin{bmatrix} \frac{\partial I}{\partial x} \frac{\partial W_x}{\partial p_1} & \frac{\partial I}{\partial y} \frac{\partial W_y}{\partial p_1} \end{bmatrix}_{p_1} \Delta p_1$$

$$+ \begin{bmatrix} \frac{\partial I}{\partial x} \frac{\partial W_x}{\partial p_2} & \frac{\partial I}{\partial y} \frac{\partial W_y}{\partial p_2} \end{bmatrix}_{p_2} \Delta p_2$$

$$+ \dots$$

$$+ \begin{bmatrix} \frac{\partial I}{\partial x} \frac{\partial W_x}{\partial p_n} & \frac{\partial I}{\partial y} \frac{\partial W_y}{\partial p_n} \end{bmatrix}_{p_n} \Delta p_n$$

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Step-by-Step Derivation

- Rewriting this in matrix notation

$$I(\mathbf{W}([x, y]; \mathbf{p} + \Delta \mathbf{p})) \approx I(\mathbf{W}([x, y]; p_1, \dots, p_n))$$

$$+ \begin{bmatrix} \frac{\partial I}{\partial x} & \frac{\partial I}{\partial y} \end{bmatrix} \begin{bmatrix} \frac{\partial W_x}{\partial p_1} \\ \frac{\partial W_y}{\partial p_1} \end{bmatrix}_{p_1} \Delta p_1$$

$$+ \begin{bmatrix} \frac{\partial I}{\partial x} & \frac{\partial I}{\partial y} \end{bmatrix} \begin{bmatrix} \frac{\partial W_x}{\partial p_2} \\ \frac{\partial W_y}{\partial p_2} \end{bmatrix}_{p_2} \Delta p_2$$

$$+ \dots$$

$$+ \begin{bmatrix} \frac{\partial I}{\partial x} & \frac{\partial I}{\partial y} \end{bmatrix} \begin{bmatrix} \frac{\partial W_x}{\partial p_n} \\ \frac{\partial W_y}{\partial p_n} \end{bmatrix}_{p_n} \Delta p_n$$

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Step-by-Step Derivation

- And further collecting the derivative terms

$$I(\mathbf{W}([x, y]; \mathbf{p} + \Delta \mathbf{p})) \approx I(\mathbf{W}([x, y]; p_1, \dots, p_n))$$

$$+ \begin{bmatrix} \frac{\partial I}{\partial x} & \frac{\partial I}{\partial y} \end{bmatrix} \begin{bmatrix} \frac{\partial W_x}{\partial p_1} & \frac{\partial W_x}{\partial p_2} & \dots & \frac{\partial W_x}{\partial p_n} \\ \frac{\partial W_y}{\partial p_1} & \frac{\partial W_y}{\partial p_2} & \dots & \frac{\partial W_y}{\partial p_n} \end{bmatrix} \begin{bmatrix} \Delta p_1 \\ \Delta p_2 \\ \vdots \\ \Delta p_n \end{bmatrix}$$

Gradient
Jacobian
Increment parameters to solve for

$$\nabla I \quad \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \quad \Delta \mathbf{p}$$
- Written in matrix form

$$I(\mathbf{W}(\mathbf{x}; \mathbf{p} + \Delta \mathbf{p})) \approx I(\mathbf{W}(\mathbf{x}; \mathbf{p})) + \nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \Delta \mathbf{p}$$

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Example: Jacobian of Affine Warp

- General equation of Jacobian

$$\frac{\partial \mathbf{W}}{\partial \mathbf{p}} = \begin{bmatrix} \frac{\partial W_x}{\partial p_1} & \frac{\partial W_x}{\partial p_2} & \dots & \frac{\partial W_x}{\partial p_n} \\ \frac{\partial W_y}{\partial p_1} & \frac{\partial W_y}{\partial p_2} & \dots & \frac{\partial W_y}{\partial p_n} \end{bmatrix}$$
- Affine warp function (6 parameters)

$$\mathbf{W}([x, y]; \mathbf{p}) = \begin{bmatrix} 1 + p_1 & p_3 & p_5 \\ p_2 & 1 + p_4 & p_6 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
- Result

$$\frac{\partial \mathbf{W}}{\partial \mathbf{p}} = \frac{\partial}{\partial \mathbf{p}} \begin{bmatrix} x + p_1x + p_3y + p_5 \\ p_2x + y + p_4y + p_6 \end{bmatrix}$$

$$= \begin{bmatrix} x & 0 & y & 0 & 1 & 0 \\ 0 & x & 0 & y & 0 & 1 \end{bmatrix}$$

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Minimizing the Registration Error

- Optimization function after Taylor expansion

$$\arg \min_{\Delta \mathbf{p}} \sum_{\mathbf{x}} \left[I(\mathbf{W}(\mathbf{x}; \mathbf{p})) + \nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \Delta \mathbf{p} - T(\mathbf{x}) \right]^2$$
- Minimizing this function
 - How?

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Minimizing the Registration Error

- Optimization function after Taylor expansion

$$\arg \min_{\Delta \mathbf{p}} \sum_{\mathbf{x}} \left[I(\mathbf{W}(\mathbf{x}; \mathbf{p})) + \nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \Delta \mathbf{p} - T(\mathbf{x}) \right]^2$$
- Minimizing this function
 - Taking the partial derivative and setting it to zero

$$\frac{\partial}{\partial \Delta \mathbf{p}} \stackrel{!}{=} 0 \rightarrow 2 \sum_{\mathbf{x}} \left[\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \right]^T \left[I(\mathbf{W}(\mathbf{x}; \mathbf{p})) + \nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \Delta \mathbf{p} - T(\mathbf{x}) \right] \stackrel{!}{=} 0$$
 - Closed-form solution for $\Delta \mathbf{p}$ (Gauss-Newton):

$$\Delta \mathbf{p} = \mathbf{H}^{-1} \sum_{\mathbf{x}} \left[\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \right]^T \left[T(\mathbf{x}) - I(\mathbf{W}(\mathbf{x}; \mathbf{p})) \right]$$
 - where \mathbf{H} is the Hessian

$$\mathbf{H} = \sum_{\mathbf{x}} \left[\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \right]^T \left[\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \right]$$

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Inverse Compositional LK Algorithm

- Iterate
 - Warp I to obtain $I(\mathbf{W}([x, y]; \mathbf{p}))$
 - Compute the error image $T([x, y]) - I(\mathbf{W}([x, y]; \mathbf{p}))$
 - Warp the gradient ∇I with $\mathbf{W}([x, y]; \mathbf{p})$
 - Evaluate $\frac{\partial \mathbf{W}}{\partial \mathbf{p}}$ at $([x, y]; \mathbf{p})$ (Jacobian)
 - Compute steepest descent images $\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}}$
 - Compute Hessian matrix $\mathbf{H} = \sum_x \left[\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \right]^T \left[\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \right]$
 - Compute $\sum_x \left[\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \right]^T [T([x, y]) - I(\mathbf{W}([x, y]; \mathbf{p}))]$
 - Compute $\Delta \mathbf{p} = \mathbf{H}^{-1} \sum_x \left[\nabla I \frac{\partial \mathbf{W}}{\partial \mathbf{p}} \right]^T [T([x, y]) - I(\mathbf{W}([x, y]; \mathbf{p}))]$
 - Update the parameters $\mathbf{p} \leftarrow \mathbf{p} + \Delta \mathbf{p}$
- Until $\Delta \mathbf{p}$ magnitude is negligible

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Inverse Compositional LK Algorithm Visualization

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Discussion LK Alignment

- Pros
 - All pixels get used in matching
 - Can get sub-pixel accuracy (important for good mosaicking)
 - Fast and simple algorithm
 - Applicable to Optical Flow estimation, stereo disparity estimation, parametric motion tracking, etc.
- Cons
 - Prone to local minima.
 - Relatively small movement.
 - ⇒ Good initialization necessary

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Side Note

- LK Registration needs a good initialization
 - Taylor expansion corresponds to a linearization around the initial position \mathbf{p} .
 - This linearization is only valid in a small neighborhood around \mathbf{p} .
- When tracking templates...
 - We typically use the previous frame's result as initialization.
 - ⇒ The higher the frame rate, the smaller the warp will be.
 - ⇒ This means we get better results and need fewer LK iterations.
 - ⇒ *Tracking becomes easier (and faster!) with higher frame rates.*

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Discussion

- Beyond 2D Tracking/Registration
 - So far, we focused on registration between 2D images.
 - The same ideas can be used when performing registration between a 3D model and the 2D image (model-based tracking).
 - The approach can also be extended for dealing with articulated objects and for tracking in subspaces.
- ⇒ We will come back to this in later lectures when we talk about model-based 3D tracking...

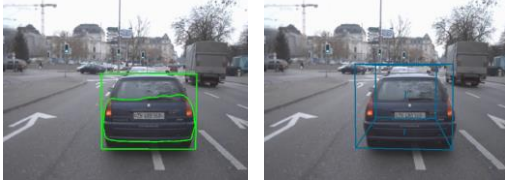
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Topics of This Lecture

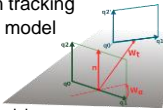
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Example of a More Complex Warping Function



- Encode geometric constraints into region tracking
 - Constrained homography transformation model
 - Translation parallel to the ground plane
 - Rotation around the ground plane normal
 - $\mathbf{W}(x) = \mathbf{W}_{obj} \mathbf{P} \mathbf{W}_t \mathbf{W}_a \mathbf{Q} x$
- ⇒ Input for high-level tracker with car steering model.



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IE, Horbert, D. Mitzel, B. Leibe, DAGM'10

References and Further Reading

- The original paper by Lucas & Kanade
 - B. Lucas and T. Kanade. [An iterative image registration technique with an application to stereo vision](#). In *Proc. IJCAI*, pp. 674–679, 1981.
- A more recent paper giving a better explanation
 - S. Baker, I. Matthews. [Lucas-Kanade 20 Years On: A Unifying Framework](#). In *IJCV*, Vol. 56(3), pp. 221-255, 2004.
- The original KLT paper by Shi & Tomasi
 - J. Shi and C. Tomasi. [Good Features to Track](#). CVPR 1994.

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